Transmission of near-resonant light through a dense slab of cold atoms

Author(s): Corman, Laura; Ville, J.L.; Saint-Jalm, R.; Aidelsburger, Monika; Bienaimé, Tom; Nascimbène, Sylvain; Dalibard, Jean; Beugnon, Jérôme

Publication Date: 2017-11

Permanent Link: https://doi.org/10.3929/ethz-b-000220067


Rights / License: Creative Commons Attribution 4.0 International

This page was generated automatically upon download from the ETH Zurich Research Collection. For more information please consult the Terms of use.
Transmission of near-resonant light through a dense slab of cold atoms

L. Corman,* J. L. Ville, R. Saint-Jalm, M. Aidelsburger,† T. Bienaimé, S. Nascimbène, J. Dalibard, and J. Beugnon‡

Laboratoire Kastler Brossel, Collège de France, CNRS, ENS-PSL Research University, UPMC-Sorbonne Universités,
11 place Marcelin-Berthelot, 75005 Paris, France

(Received 30 June 2017; revised manuscript received 4 October 2017; published 27 November 2017)

The optical properties of randomly positioned, resonant scatterers is a fundamentally difficult problem to address across a wide range of densities and geometries. We investigate it experimentally using a dense cloud of rubidium atoms probed with near-resonant light. The atoms are confined in a slab geometry with a subwavelength thickness. We probe the optical response of the cloud as its density and hence the strength of the light-induced dipole-dipole interactions are increased. We also describe a theoretical study based on a coupled dipole simulation which is further complemented by a perturbative approach. This model reproduces qualitatively the experimental observation of a saturation of the optical depth, a broadening of the transition, and a blueshift of the resonance.

DOI: 10.1103/PhysRevA.96.053629

I. INTRODUCTION

The interaction of light with matter is a fundamental problem which is relevant for simple systems, such as an atom strongly coupled to photons [1–3], as well as for complex materials, whose optical properties provide information on their electronic structure and geometry [4]. This interaction can also be harnessed to create materials and devices with tailored properties, from quantum information systems such as memories [5] andnanophotonic optical isolators [6] to solar cells combining highly absorptive materials with transparent electrodes [7].

The slab geometry is especially appropriate to study light-matter interaction [8,9]. In the limit of a monolayer, two-dimensional (2D) materials exhibit fascinating optical properties. For simple direct band gap 2D semiconductors, the single-particle band structure implies that the transmission coefficient takes a universal value [10,11]. This was first measured for single-layer graphene samples [12], which have an optical transmission independent of the light frequency in the eV range, \(|T|e^2 = 1 - \pi \alpha\), where \(\alpha\) is the fine-structure constant [13,14]. The same value was recovered in InAs semiconductors [15]. This universality does not hold for more complex 2D materials, for instance when the Coulomb interaction plays a more important role [16].

Atomic gases represent in many respects an ideal test bed for investigating light-matter interaction. First, they can be arranged in regular arrays [17,18] or randomly placed [19] to tailor the optical properties of the system. Second, an atom always scatters light, in contrast with solid-state materials where the optical excitation can be absorbed and dissipated in a nonradiative way. Even for thin and much more dilute samples than solid-state systems, strong attenuation of the transmission can be observed at resonance. Third, inhomogeneous Doppler broadening can be made negligible using ultracold atomic clouds. Finally, the geometry and the density of the gases can be varied over a broad range.

In the dilute limit, such that the three-dimensional (3D) atomic density \(\rho\) and the light wave number \(k\) verify \(\rho k^{-3} \ll 1\), and for low optical depths, a photon entering the atomic medium does not recurrently interact with the same atom. Then, for a two-level atom, the transmission of a resonant probe beam propagating along the \(z\) axis is given by the Beer-Lambert law: \(|T|^2 = e^{-\tilde{\alpha} \rho dz}\), where \(\tilde{\alpha} = 6\pi\gamma^{-2}\) is the light cross section at the optical resonance [20]. At larger densities the transmission is strongly affected by the light-induced dipole-dipole coupling between neighboring atoms.

Modification of the atomic resonance line shape or super- and subradiance in dilute (but usually optically dense) and cold atomic samples have been largely investigated experimentally [21–30]. Recently, experiments have been performed in the dense regime studying nanometer-thick hot vapors [31] and mesoscopic cold clouds [32–35]. Interestingly, it has been found that the mean-field Lorentz-Lorenz shift is absent in cold systems where the scatterers remain fixed during the measurement. A small redshift is still observed for dense clouds in Refs. [32,34] but could be specific to the geometry of the system.

Achieving large densities is concomitant with a vanishingly small transmission \(T\). It is therefore desirable to switch to a 2D or thin slab geometry in order to investigate the physical consequences of these resonant interaction effects at the macroscopic level. Using a 2D geometry also raises a fundamental question inspired by the monolayer semiconductor case: can the light extinction through a plane of randomly positioned atoms be made arbitrarily large when increasing the atom density or does it remain finite, potentially introducing a maximum of light extinction through 2D random atomic samples independent of the atomic species of identical electronic spin?

In this article, we study the transmission of nearly resonant light through uniform slabs of atoms. We report experiments realized on a dense layer of atoms with a tunable density and thickness. For dense clouds, the transmission is strongly enhanced compared to the one expected from the single-atom
response. We also observe a broadening and a blueshift of the resonance line on the order of the natural linewidth. This blueshift contrasts with the mean-field Lorentz-Lorenz redshift and is a signature of the strongly correlated regime reached in our system because of dipole-dipole interactions [36]. In addition, we observe deviations of the resonance line shape from the single-atom Lorentzian behavior, especially in the wings where the transmission decays more slowly. We model this system with coupled dipole simulations complemented by a perturbative approach which qualitatively supports our observations. After describing our experimental system in Sec. II, we investigate theoretically light scattering for the observations. After describing our experimental system in Sec. II, we present our experimental results and compare them with theory. We conclude in Sec. V.

II. EXPERIMENTAL METHODS

A. Cloud preparation

We prepare a cloud of $^{87}$Rb atoms with typically $N = 1.3(2) \times 10^5$ atoms in the $|F = 1, m_F = -1\rangle$ state. The atoms are confined in an all-optical trap, described in more detail in [37], with a strong harmonic confinement in the vertical direction $z$ with frequency $\omega_z/2\pi = 2.3(2)$ kHz leading to a Gaussian density profile along this direction. The transverse confinement along the $x$ and $y$ directions is produced by a flat-bottom disk-shaped potential of diameter $2R = 40$ $\mu$m. For our initial cloud temperature $\approx 300$ nK, there is no extended phase coherence in the cloud [38]. Taking into account this finite temperature, we compute for an ideal Bose gas a rms thickness $\Delta z = 0.25(1)$ $\mu$m, or equivalently $k \Delta z = 2.0(1)$. This situation corresponds to $nk^{-\frac{3}{2}} \approx 1.5$, where $n = N/(\pi R^2)$ is the surface density and to a maximum density $\rho k^{-\frac{3}{2}} \approx 0.3$ at the trap center along $z$ where $\rho$ is the volume density. We tune the number of atoms that interact with light by partially transferring them to the $|F = 2, m_F = -2\rangle$ state using a resonant microwave transition. In this state, the atoms are sensitive to the probe excitation, contrary to the ones in the $|F = 1, m_F = -1\rangle$ state. In this temperature range the Doppler broadening is about three orders of magnitude smaller than the natural linewidth of the atomic transition.

The cloud thickness is varied in a controlled way using mainly the following two techniques. (i) Varying the vertical harmonic confinement by modifying the laser power in the blue-detuned lattice that traps the atoms, thus changing its frequency from $\omega_z/2\pi = 1.1(2)$ kHz to $\omega_z/2\pi = 2.3(2)$ kHz. Using the ideal Bose gas statistics in the tight harmonic trap, for a gas of $N = 1.3(2) \times 10^5$ atoms at a temperature of $T \approx 300$ nK, this corresponds to rms thicknesses between $0.3 \mu$m and $0.6 \mu$m. (ii) Allowing the atoms to expand for a short time after all traps have been switched off. The extent of the gas in the $xy$ direction does not vary significantly during the time of flight (duration between 0.7 ms and 4.7 ms). In that case, the rms thickness varies between $3 \mu$m and $25 \mu$m. For the densest clouds, the thickness is also influenced by the measurement itself. Indeed, the light-induced dipole-dipole forces between atoms lead to an increase of the size of the cloud during the probing. In the densest case, we estimate from measurements of the velocity distribution after an excitation with a duration of $\tau = 10 \mu$s that the thickness averaged over the pulse duration is increased by $\sim 20\%$. In some experiments, in which the signal is large enough, we limit this effect by reducing the probe duration $\tau$ to $3 \mu$s.

B. Transmission measurement

We probe the response of the cloud by measuring the transmission of a laser beam propagating along the $z$ direction (See Fig. 1). The light is linearly polarized along the $x$ axis and tuned close to the $|F = 2\rangle \rightarrow |F' = 3\rangle$ $D_2$ transition. The duration of the light pulse is fixed to $10 \mu$s for most experiments and we limit the imaging intensity $I$ to the weakly saturating regime with $0.075 < I/I_{\text{sat}} < 0.2$, where $I_{\text{sat}} \approx 1.67$ mW/cm$^2$ is the resonant saturation intensity. We define $\Delta I_{\text{sat}}$ as the detuning of the laser beam with respect to the single-atom resonance. The cloud intensity transmission $|T|^2$ is extracted by comparing images with and without atoms and we compute the optical depth $D = -\ln |T|^2$ (see Sec. II C). The numerical aperture of the optical system is limited on purpose to minimize the collection of fluorescence light from directions different from the propagation direction of the light beam.

C. Computation of the optical depth

We extract the optical depth ($D$) of the clouds by comparing pictures with and without atoms. The readout noise on the count number $N_{\text{count}}$ is $dN_{\text{count}} \approx 5$ per pixel. We subtract from these images equivalent pictures without any imaging pulse to remove the background counts and obtain two pictures $M_{\text{with}}$ and $M_{\text{without}}$. The typical noise on the count number per pixel is thus $dN = \sqrt{2}dN_{\text{count}} \approx 7$. 

053629-2
The magnification of the optical system is 11.25, leading to an effective pixel size in the plane of the atoms of 1.16 μm. The typical mean number of counts per pixel accumulated during the 10 μs imaging pulse is 80 on the picture without atoms. We optimize the signal-to-noise ratio by summing all the pixels in the region of interest for $M_{\text{with}}$ and $M_{\text{without}}$. This yields a total count number in the picture with atoms $N_{\text{with}}$ and without atoms $N_{\text{without}}$ from which we compute the optical depth: $D = -\ln(N_{\text{with}}/N_{\text{without}})$. The region of interest varies with the time of flight of the cloud. This region is a disk that ensures that we consider a part of the cloud with approximately constant density (with 15% rms fluctuations), comprising typically 200 pixels. With these imaging parameters we can reliably measure optical depths up to 4 but we conservatively fit only data for which $D < 3$. At low densities, the statistical error on $D$ due to the readout noise is about 0.01. At $D \sim 3$, it reaches 0.12.

D. Atom number calibration

As demonstrated in this article, dipole-dipole interactions strongly modify the response of the atomic cloud to resonant light and make an atom number calibration difficult. In this work, we measure the atom number with absorption imaging for different amounts of atoms transferred by a coherent microwave field from the $|F = 1, m_F = -1\rangle$ “dark” state to the $|F = 2, m_F = -2\rangle$ state in which the atoms are resonant with the linearly polarized probe light. We perform resonant Rabi oscillations for this coherent transfer and fit the measured atom number as a function of time by a sinus square function. We select points with an optical depth below 1, to limit the influence of dipole-dipole interactions. This corresponds to small microwave pulse area or to an area close to a 2π pulse, to make the fit more robust. From the measured optical depth $D$, we extract $nk^2 = (15/7)D/(6\pi)$. The factor 7/15 corresponds to the average of equally weighted squared Clebsch-Gordan coefficients for linearly polarized light resonant with the $F = 2$ to $F' = 3$ transition. This model does not take into account possible optical pumping effects that could lead to an unequal contribution from the different transitions and hence a systematic error on the determination of the atom number.

E. Experimental protocol

Our basic transmission measurements consist in scanning the detuning $\Delta \nu$ close to the $F = 2$ to $F' = 3$ resonance ($|\Delta \nu| < 30$ MHz) and in measuring the optical depth at a fixed density. The other hyperfine levels $F' = 2,1,0$ of the excited $5P_{3/2}$ level play a negligible role for this detuning range. The position of the single-atom resonance is independently calibrated using a dilute cloud. The precision on this calibration is of 0.03 $\Gamma_0$, where $\Gamma_0/2\pi = 6.1$ MHz is the atomic linewidth. The measured resonance curves are fitted with a Lorentzian function:

$$\Delta \nu \mapsto D_{\text{max}}/[1 + 4(\Delta \nu - \nu_0)^2 / \Gamma^2].$$

This function captures well the central shape of the curve for thin gases, as seen in the examples of Fig. 2. When increasing the atomic density we observe a broadening of the line $\Gamma > \Gamma_0$, a nonlinear increase of the maximal optical depth $D_{\text{max}}$, and a blueshift $\nu_0 > 0$. In Sec. IV we present the evolution of these fitted parameters for different densities and thicknesses. Note that in our analysis all points with values of $D$ above 3 are discarded to avoid potential systematic errors. Whereas this threshold has little influence for thin clouds (as shown in Fig. 2) for which the maximal optical depths are not large compared to the threshold, for thick gases this typically removes the measurements at detunings smaller than 1.5$\Gamma_0$. Hence, in this case, we consider the amplitude and the width of the fits to be not reliable and we use the position of the maximum of the resonance $\nu_0$ with caution.

We investigate the dependence of the fit parameters $D_{\text{max}}$, $\Gamma$, and $\nu_0$ for different atomic clouds in Sec. IV. These results are compared to the prediction from a theoretical model that we describe in the following section.

III. THEORETICAL DESCRIPTION

Light scattering by a dense sample of emitters is a complex many-body problem and it is quite challenging to describe. The slab geometry is a textbook situation which has been largely explored. A recent detailed study of the slab geometry can be found in Ref. [39]. We focus in this section first on a perturbative approach which is valid for low enough densities. We then report coupled dipole simulations following the method presented in [19] but extended with a finite-size scaling approach to address the situation of large slabs. We also discuss the regime of validity for these two approaches.

A. Perturbative approach

We describe here a semianalytical model accounting for the multiple scattering of light by a dilute atom sample, inspired from Ref. [40]. By taking into account multiple scattering processes between atom pairs, it provides the first correction to the Beer-Lambert law when decreasing the mean distance $l$ between nearest neighbors towards $k^{-3}$.
1. Index of refraction of a homogeneous system

In Ref. [40], the index of refraction of a homogeneous dilute atomic gas was calculated, taking into account the first nonlinear effects occurring when increasing the volume atom density. The small parameter governing the perturbative expansion is \( \rho k^{-3} \), where \( \rho \) is the atom density. At second order in \( \rho k^{-3} \) two physical effects contribute to the refraction index, namely the effect of the quantum statistics of atoms on their position distribution and the dipole-dipole interactions occurring between nearby atoms after one photon absorption. Here we expect the effect of quantum statistics to remain small, and thus neglect it hereafter (see Ref. [41] for recent measurement of this effect). Including the effect of multiple scattering processes between atom pairs, one obtains the following expression for the refractive index:

\[
n_{r} = 1 + \frac{\alpha\rho}{1 - \alpha\rho/3 + \beta\rho},
\]

where we introduced the atom polarizability \( \alpha = 6\pi i k^{-3} / (1 - 2i\delta/\Gamma) \) and the Green function \([G]\) of an oscillating dipole,

\[
G_{\theta\theta}(r) = \frac{\delta(\delta) \delta_{\theta\theta} + G_{\theta\theta}^\prime(r),}
G_{\theta\theta}^\prime(r) = \frac{k^3 e^{-\alpha}}{4\pi k r} \left( 1 + \frac{3i}{k r} - \frac{3}{(k r)^2} \right) \frac{r_{\alpha} r_{\beta}}{r^2} - \left( 1 + \frac{i}{k r} - \frac{1}{(k r)^2} \right) \delta_{\theta\theta},
\]

in which retardation effects are neglected [42]. Note that for a thermal atomic sample of Doppler width larger than \( \Gamma \), we expect an averaging of the coherent term \( \beta \) to zero due to the random Doppler shifts. When setting \( \beta = 0 \) in Eq. (2) we recover the common Lorentz-Lorenz shift of the atomic resonance [43]. We plot in Fig. 3 the imaginary part of the index of refraction as a function of the detuning \( \delta \), for a typical atom density used in the experiment (solid line), and compare with the single-atom response with (dotted line) and without (dashed line) Lorentz-Lorenz correction. The resonance line is modified by dipole-dipole interactions and we observe a blueshift of the position of the maximum of the resonance [44].

2. Transmission through an infinite slab with a Gaussian density profile

In order to account more precisely for the light absorption occurring in the experiment, we extend the perturbative analysis of light scattering to inhomogeneous atom distributions, for which the notion of index of refraction may not be well defined. The atom distribution is modeled by an average density distribution \( \rho(z) \) of infinite extent along \( x \) and \( y \), and depending on \( z \) only, as \( \rho(z) = \rho_0 \exp[-z^2/(2\Delta^2)] \). We describe the propagation of light along \( z \) in the atomic sample. The incoming electric field is denoted as \( E_0 e^{ikz} e^{-i\omega t} \). The total electric field, written as \( E(z) e^{-i\omega t} \), is given by the sum of the incoming field and the field radiated by the excited atomic dipoles:

\[
E(z) = E_0 e^{ikz} e^{-i\omega t} + \int d^3r' \rho(z') \frac{[G(r - r')] e^{ikz}}{\epsilon_0} d(z'),
\]

where \( d(z) \) is the dipole amplitude of an atom located at \( z \) and \( \epsilon_0 \) is the vacuum permittivity. The integral over \( x \) and \( y \) can be performed analytically, leading to the expression

\[
E(z) = E_0 e^{ikz} e^{-i\omega t} + \frac{i k}{2\epsilon_0} \int d z' \rho(z') e^{ikz - z'} d(z'),
\]

where \( d(z) \) is the dipole amplitude projected in the \( x, y \) plane.

The dipole amplitude can be calculated from the atom polarizability \( \alpha \) and the electric field at the atom position. Taking into account multiple light scattering between atom pairs, we obtain a self-consistent expression for the dipole amplitude, valid up to first order in atom density, as \( d(z) = d(z) e_x \), with

\[
d(z) = \alpha \epsilon_0 E_0 e^{ikz} + \int d^3r' \rho(z') \left( \frac{\alpha G}{1 - \alpha^2 G^2} \right)_{xx} (r - r') d(z') + \left( \frac{\alpha^2 G^2}{1 - \alpha^2 G^2} \right)_{xx} (r - r') d(z).\]

Note that the dipole amplitude also features a component along \( z \), but it would appear in the perturbative expansion in the atom density at higher orders.

The electric field and dipole amplitude are numerically computed by solving the linear system (6) and (7). The optical depth is then calculated as \( D = -\ln([E(z)]^2/[E_0]^2) \) for \( z \gg \Delta z \). The results of this approach will be displayed and quantitatively compared to coupled dipole simulations in the next subsection.

B. Coupled dipole simulations

1. Methods

Our second approach to simulate the experiments follows the description in Ref. [19] and uses a coupled dipole model.
We consider atoms with a $J = 0$ to $J = 1$ transition. For a given surface density $n$ and thickness $\Delta z$ we draw the positions of the $N$ atoms with a uniform distribution in the $xy$ plane and a Gaussian distribution along the $z$ direction. The number of atoms and hence the disk radius is varied to perform finite-size scaling. For a given detuning and a linear polarization along $x$ of the incoming field, we compute the steady-state value of each dipole $d_j$, which is induced by the sum of the contributions from the laser field and all the other dipoles in the system. The second contribution is obtained thanks to the tensor Green function $G$ giving the field radiated at position $\vec{r}$ by a dipole located at origin.

Practically, the values of the $N$ dipoles are obtained by numerically solving a set of $3N$ linear equations, which limits the atom number to a few thousands, a much lower value than in the experiment (where we have up to $10^5$ atoms). From the atom number to a few thousands, a much lower value than in the experiment (where we have up to $10^5$ atoms). From the atom number, we have developed a finite-size scaling approach to circumvent this limitation. We focus in the following on the atom number. We have developed a finite-size scaling approach to circumvent this limitation. We focus in the following on transmission measurements as in the experiment.

As the number of atoms used in the simulations is limited, it is important to verify the result of the simulations is independent of the atom number. In this work, we are mostly interested in the response of an infinitely large system in the $xy$ plane. It is indeed the situation considered in the perturbative approach and in the experimental system for which the diameter is larger than $300k^{-1}$ and where finite-size effects should be small. The atom number in the simulations is typically two orders of magnitude lower than in the experiment and finite-size effects could become important. For instance, some diffraction effects due to the sharp edge of the disk could play a role [39]. Consequently, we varied the atom number in the simulations and observed, for simulated clouds with small radii, a significant dependence of the simulation results on the atom number. We have developed a finite-size scaling approach to circumvent this limitation. We focus in the following on transmission measurements as in the experiment.

We show two examples of this finite-size scaling approach for $k\Delta z = 1.6$ in Fig. 4 and $k\Delta z = 80$ in Fig. 5. For low enough surface densities, the results of the simulations (maximal optical depth, width, shift, etc.) for different atom numbers in the simulation are aligned, when plotted as a function of $1/\sqrt{N_{\text{sim}}}$, and allow for the desired finite-size scaling. All the results presented in this section and in Sec. IV [45] are obtained by taking the extrapolation to an infinite system size, which corresponds to the offset of the linear fit in Figs. 4 and 5.

Interestingly, we observe in Fig. 4 for a thin cloud that considering a finite-size system only leads to a small underestimate of the blueshift of the resonance. However, for thicker slabs, such as in Fig. 5, we get, for finite systems, a small redshift and a narrowing of the line. Considering our experimental system, we have $1/\sqrt{N} \approx 0.003$, leading to a small correction according to the fits in Fig. 5. However, for such thick systems we are able to simulate only systems with low $nk^{-2}$, typically 0.1, whereas we can reach densities 15 times larger in the experiment, which could enhance finite-size effects. Simulation of thick and optically dense slabs is thus challenging and the crossover between the thin slab situation explored in this article and the thick regime is an interesting perspective of this work.

2. Role of the thickness and density of the cloud

We now investigate the results of coupled dipole simulations for different densities and thicknesses of the atomic cloud. We limit the study to low densities, for which the finite-size scaling approach works. It is important to note that the computed line shapes deviate significantly from a Lorentzian shape and become asymmetric. Consequently
there is not a unique definition for the center of the line and for its width. In our analysis, we fit the resonance lines around their maximum with a typical range of ±0.5 $\Gamma$. The shift thus corresponds to a variation of the position of the maximum of the line and the “width” characterizes the curvature of the line around its maximum. The results of these fits are reported in Fig. 6 as a function of surface density for different thicknesses. In these plots, we observe the same features as qualitatively described in Sec. II: a decrease of the maximal optical depth with respect to the single-atom response [Fig. 6(a)], a blueshift of the position of the maximum [Fig. 6(b)], and a broadening of the line [Fig. 6(c)]. For a fixed thickness, these effects increase with surface density and for a fixed surface density they are more pronounced for lower thicknesses. Note that we only explore here surface densities lower than 0.25 which is quite lower than the maximum experimental value (~1.5). Whereas our finite-size scaling approach can be well extended for very thin systems ($k\Delta z < 1$) it fails for thick and optically dense systems [46].

3. Comparison with the perturbative model

The perturbative approach is limited to low densities $\rho k^{-3} \ll 1$ but it gives the response of an infinitely expanded cloud in the transverse direction. Coupled dipole simulations can in principle address arbitrarily large densities but the number of atoms considered in a simulation is limited, and thus for a given density the size of the system is limited. Coupled dipole simulations are thus more relevant for thin and dense samples and the perturbative approach more suited for nonzero thickness samples.

In Fig. 7 we choose two illustrative examples to confirm, in the regime where both models could be used, that these two approaches are in quantitative agreement. In Fig. 7(a) we compare the maximum optical depth as a function of surface density for three different thicknesses. The perturbative approach is typically valid, for this set of thicknesses, up to $nk^{-2} \sim 0.1$. We investigate the shift of the position of the maximum in Fig. 7(b). We report, as a function of the inverse thickness $1/k\Delta z$, the slope $\gamma$ of the shift with density, $v_0 = \gamma nk^{-2}$, computed for surface densities below 0.1. The dotted line is the result from the perturbative approach, the solid line corresponds to coupled dipole simulations, and the dash-dotted line to the result for zero thickness. The perturbative approach approximates well coupled dipole simulations. This result also confirms that the finite-size scaling approach provides a good determination of the response of an infinite system in the $xy$ direction.

We have identified in this section the specific features of the transmission of light through a dense slab of atoms. We focus here on the transmission coefficient to show that we

---

**FIG. 6.** Coupled dipole simulations for different thicknesses. (a) Maximal optical depth; (b) position of the maximum of the line; (c) width of the resonance line. We report results for $k\Delta z = 0, 1.6, 8$, the darkest lines corresponding to the smallest thicknesses. The black dashed lines correspond to the single-atom response.

**FIG. 7.** Comparison between the coupled dipole simulations and the perturbative model. (a) Behavior of the optical depth at the single-atom resonance $D_0$ with surface density for different thicknesses ($k\Delta z = 0, 1.6, 3.2$, from bottom to top). Coupled dipole simulations are shown as solid lines, perturbative approach as dotted lines, and the dashed line is the Beer-Lambert prediction. (b) Slope $\gamma$ of the blueshift $v_0 = \gamma nk^{-2}$ as a function of the inverse thickness $1/k\Delta z$. The solid line is the result of the coupled dipole model, the dash-dotted line is the zero-thickness coupled dipole result ($1/k\Delta z \to \infty$), and the dotted line is the perturbative model.
Beer-Lambert prediction (narrow dashes) $D_{BL} = n \sigma_0$ and to the same prediction corrected by a factor 7/15 (large dashes). This factor is the average of the Clebsch-Gordan coefficients relevant for $\pi$-polarized light tuned close to the $|F = 2 \rangle \rightarrow |F' = 3 \rangle$ transition and, as discussed previously, it is included in the calibration of the atom number. At large surface densities, we observe an important deviation from this corrected Beer-Lambert prediction: we measure that $D_{max}$ seems to saturate around $D_{max} \approx 3.5$, whereas $D_{BL} \approx 13$ [47]. We also show the prediction of the coupled dipole model, as a solid line for the full range of surface densities at $k \Delta z = 0$ and as a dotted line for the numerically accessible range of surface densities at $k \Delta z = 2.4$. The coupled dipole simulation at $k \Delta z = 0$ shows the same trend as in the experiment but with $D_{max}$ now bounded by 2. A reason could be the nonzero thickness of the atomic slab. In order to test this hypothesis, we investigated the influence of probing duration for the largest density. For such a density we could decrease the pulse duration while keeping a good enough signal-to-noise ratio [see inset in Fig. 2(b)]. For a shorter probing duration, hence for a smaller expansion of the cloud, $D_{max}$ decreases, in qualitative agreement with the expected effect of the finite thickness.

The saturation of the optical depth with density is a counterintuitive feature. It shows that increasing the surface density of an atomic layer does not lead to an increase of its optical depth. Coupled dipole simulations at $k \Delta z = 0$ even show that the system becomes slightly more transparent as the surface density is increased. This behavior may be explained qualitatively by the broadening of the distribution of resonance frequencies of the eigenmodes of this many-body system. A dense system scatters light for a large range of detunings but the cross section at a given detuning saturates or becomes lower as the surface density is increased.

We display in Fig. 8(b) the width $\Gamma$ of the Lorentzian fits for $k \Delta z = 2.4(6)$ along with coupled dipole simulation results [46]. We observe a broadening of the resonance line up to more than $3 \Gamma_0$. This broadening is confirmed by the simulation results for $k \Delta z = 0$ (solid line). Note that the exact agreement with the experimental data should be considered as coincidental. The range on which we can compute the broadening for $k \Delta z = 2.4$ (light dotted line) is too small to discuss a possible agreement.

We show in Fig. 8(c) the evolution of $v_0$ with density. A blueshift, reaching 0.2$\Gamma_0$ for the largest density, is observed. At the largest density, an even larger shift is observed when decreasing the pulse duration ($\approx 0.4 \Gamma_0$, not shown here). We also display the result of the coupled dipole model for the cases $k \Delta z = 2.4$ and $k \Delta z = 0$. Both simulations confirm the blueshift but predict a different behavior and a larger effect. In addition, we show the variation of $v_0$ for a thick cloud with $k \Delta z = 30(8)$. In that case we observe a marginally significant redshift [48].

The experimental observation of a blueshift is in stark contrast, both in amplitude and in sign, with the mean-field prediction of the Lorentz-Lorenz redshift $v_0/\Gamma_0 = -\pi \rho k^{-3} = -\sqrt{\pi/2} n k^{-2}/(k \Delta z)$, written here at the center of the cloud along $z$. The failure of the Lorentz-Lorenz prediction for cold atom systems has already been observed and discussed for instance in Refs. [30,34,36]. As discussed with the perturbative approach in Sec. III, the Lorentz-Lorenz

FIG. 8. Maximum optical depth (a), broadening (b), and frequency shift (c) of the resonance line for our thinnest samples with $k \Delta z = 2.4(6)$ (circles) and for thicker samples with $k \Delta z = 30(8)$ (squares). In (a) the shaded area represents the uncertainty in the frequency calibration of the single-atom resonance. In (a) and (b), the dark black solid (light blue dotted) line is the prediction of the coupled dipole model for $k \Delta z = 0$ ($k \Delta z = 2.4$) in its accessible range of densities. The dashed lines represent the single-atom response.

observe the same features in the experiment and we will make a quantitative comparison between our experimental findings and the results obtained with coupled dipole simulations. Our theoretical analysis is complemented by a study of the reflection coefficient of a strictly 2D gas detailed in Appendix.

IV. EXPERIMENTAL RESULTS

We show in Fig. 8 the results of the experiments introduced in Sec. II. The fitted $D_{max}$ for different surface densities is shown in Fig. 8(a). We compare these results to the
the Lorentzian shape expected for a single atom. We measure distributed scatterers. Consequently, we believe that it is an important and generic profile considered in this work, and also discussed in [44]. It is robust to a wide range of thicknesses and density, and while we computed it theoretically for a two-level system, it also shows up experimentally in a more complex atomic geometry in Ref. [34], where the size of the atomic cloud is comparable to \( \lambda \) and where diffraction effects may play an important role. As discussed in Sec. III, our observation of a blueshift is a general result which applies to the infinite slab. It is robust to a wide range of thicknesses and density, and while we computed it theoretically for a two-level system, it also shows up experimentally in a more complex atomic level structure. It was also predicted in Ref. [39] but for a uniform distribution along the \( z \) axis instead of the Gaussian profile considered in this work, and also discussed in [44]. Consequently, we believe that it is an important and generic feature of light scattering in a extended cloud of fixed randomly distributed scatterers.

Finally, we compare the line shape of the resonance with the Lorentzian shape expected for a single atom. We measure for \( nk^{-2} = 1.5(2) \), the optical depth at large detunings, and for various cloud thicknesses. We fit it with a power law on the red-detuned (blue-detuned) frequency interval with exponent \( \eta_r (\eta_b) \) as shown, for two examples, in Fig. 9(a). If the behavior were indeed Lorentzian, the exponents should be \(-2\) in the limit of large detuning. As seen in Fig. 4(c), for the thinnest gases, the fitted exponents are significantly different from the expected value and can reach values up to \(-1.3\), showing the strong influence of dipole-dipole interactions in our system. We show the result of coupled dipole simulations for \( k \Delta z = 0 \) in Fig. 4(b) along with their power-law fit. We extract the exponents \( \eta_r = -0.36(1) \) and \( \eta_b = -0.70(1) \) that are reported as solid lines in Fig. 4(c). Our experimental results interpolate between the single-atom case and the simulated 2D situation.

V. CONCLUSION

In summary we have studied the transmission of a macroscopic dense slab of atoms with uniform in-plane density and a transverse Gaussian density distribution. We observed a strong reduction of the maximum optical density and a broadening of the resonance line. More surprisingly, we showed the presence of a large blueshift of the resonance line and a deviation from Lorentzian behavior in the wings of the resonance line. These results are qualitatively confirmed by coupled dipole simulations and a perturbative approach of this scattering problem. We also confirm the difficulty already observed to obtain a quantitative agreement between coupled dipole simulations and experimental results in the dense regime [32,34]. Possible explanations for this discrepancy are (i) residual motion of the atoms during the probing due to the strong light-induced dipole-dipole interactions, (ii) a too large intensity used in the experiment which goes beyond the validity of the coupled dipole approach, and (iii) the influence of the complex atomic level structure. We were careful in this work to limit the influence of the two first explanations and the last possibility is likely to be the main limitation. The complex level structure leads to optical pumping effects during the probing and thus the scattering cross section of the sample is not well defined. A simple way to take into account the level structure is, as discussed in Sec. IV, to renormalize the scattering cross section by the average of the Clebsch-Gordan coefficients involved in the process. For \(^{87}\)Rb atoms this amounts to the factor \( 7/15 \) already discussed earlier. However, this is a crude approximation which neglects optical pumping effects during scattering and whose validity in the dense regime is not clear. Two approaches can be considered to remove this limitation. First, one can use another atomic species such as strontium or ytterbium bosonic isotopes which have a spin singlet ground state and in which almost exact two-level systems are available for some optical transitions.

![FIG. 9. Non-Lorentzian wings of the resonance line. (a) Two examples of the scaling of optical depth with \( \Delta v \) (blue side), in log-log scale, for \( k \Delta z = 2.4(6) \) (circles) and for \( k \Delta z = 350(90) \) (squares) and their power-law fit. (b) Coupled dipole simulations at zero thickness and for \( nk^{-2} = 1.5(2) \). The optical depth is plotted as a function of detuning (minus the detuning) from the resonance line, for the blue (circles) [red (squares)] side. The solid lines are power-law fits. (c) Experimental results for \( nk^{-2} = 1.5(2) \). Circles (squares) represent the fitted exponents \( \eta_r (\eta_b) \) to the far-detuned regions of the resonance line on the red and blue side, respectively. The fit function is \( \Delta v \rightarrow D(\Delta v) = A (\Delta v - v_b) \). The error on the fitted exponents is also determined using a bootstrap analysis. The horizontal dashed black line (\( \eta = -2 \)) emphasizes the expected asymptotic value for low densities for a Lorentzian line (at large detunings).](053629-8)
Scattering experiments on strontium clouds have been reported [25,30,49] but they did not explore the dense regime tackled in this work. The comparison with theory thus relies on modeling their inhomogeneous density distribution accurately. Second, an effective two-level system can be created in the widely used alkali-metal atoms by imposing a strong magnetic field which could separate the different transitions by several times the natural linewidth as demonstrated in some recent experiments on three-level systems [50,51]. This method could be in principle applied on our setup to create an effective two-level system and could help one to understand the aforementioned discrepancies.

Finally, we note that this article focuses on the steady-state transmission of a cloud illuminated by a uniform monochromatic beam. The slab geometry that we have developed here is of great interest for comparison between theory and experiments and our work opens interesting perspectives for extending this study to time-resolved experiments, to fluorescence measurements, or to spatially resolved propagation of light studies.

ACKNOWLEDGMENTS

We thank Vitaly Kresin, Klaus Mølmer, Janne Ruostekoski, Markus Greiner, Zoran Hadzibabic, and Wilhelm Zwerger for fruitful discussions. This work is supported by DIM NanoK, ERC (Synergy UQUAM). L.C. acknowledges the support from DGA. This project has received funding from the European Union’s Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie grant agreement No. 703926.

APPENDIX: REFLECTION COEFFICIENT OF A 2D GAS

Thanks to their large scattering cross section at resonance, arrays of atoms can be used to emit light with a controlled spatial pattern [52]. A single-atom mirror has been demonstrated [53] and, more generally, regular two-dimensional arrays of atoms have been considered for realizing controllable light absorbers [17] or mirrors [18] with atomic-sized thicknesses. For the disordered atomic samples considered in this article the strong decrease of the transmission because of dipole-dipole interactions could lead to a large reflection coefficient. For a strictly two-dimensional gas we show as a solid line in Fig. 10 the result of the coupled dipole model for the intensity reflection coefficient $|R|^2$ at resonance and at normal incidence as a function of density. This intensity reflection coefficient has a behavior with density similar to the optical depth $D$ (dotted line). The relation between these two quantities depends on the relative phase between the incoming and the reflected field. For a transmitted field in phase with the incident field we find, using the boundary condition $R + T = 1$, a lower bound for this reflection coefficient, $|R|^2 \geq (1 - |T|)^2$, shown as a dashed line in Fig. 10. The intensity reflection coefficient is close to this lower bound in the regime explored in this work. The maximum computed value for the reflection coefficient is close to 40%, which shows that a single disordered layer of individual atoms can significantly reflect an incoming light beam [54]. Note that for a non-2D sample light can be diffused at any angle. For our experimental thickness and the relevant densities the reflection coefficient is in practice much lower than the above prediction.

M. O. Araújo, I. Krešić, R. Kaiser, and W. Guerin, Superradiance

S. J. Roof, K. J. Kemp, M. D. Havey, and I. M. Sokolov, Ob-

A. Goban, C.-L. Hung, J. D. Hood, S.-P. Yu, J. A. Muniz, O.


S. J. Kroo, K. J. Kemp, M. D. Havey, and I. M. Sokolov, Ob-

The observed saturation is not due to our detection procedure. In the fitting procedure, we only select points with a measured optical depth below 3 to avoid any bias.

For thick clouds the expected optical depth of the cloud becomes larger than the maximal value we can detect. We then only fit the points with a measured optical depth below 3. From this fit we cannot estimate reliably the value of the maximum and width of the resonance line, but we can get an estimate of the “center” of the line which may deviate from the position of the maximum of the resonance for an asymmetric line shape.


We have investigated here only the behavior at normal incidence. A full characterization of such an atomic mirror is beyond the scope of this work.