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6 Abstract

 CO_2 clusters with 2 to 4300 molecules are characterized with mass spectrom-7 etry and infrared spectroscopy in the uniform postnozzle flow of Laval ex-8 pansions at constant temperatures of $\sim 29 \,\mathrm{K}$ and $\sim 43 \,\mathrm{K}$. The mass spectra 9 provide independent, accurate information on the cluster size distributions 10 and through magic numbers also on cluster structures. The experimental re-11 sults are complemented with force field, quantum chemical, and vibrational 12 exciton calculations. We find our data to be consistent with predominantly 13 fcc cuboctahedral structures for clusters with more than about 50 molecules. 14 Infrared spectra of cluster size distributions with average sizes above 140-220 15 molecules are completely dominated by the features from the larger cubocta-16 hedral clusters in the distribution. For very small clusters, exciton simulations 17 predict a pronounced broadening of the infrared band as soon as the average 18 cluster size exceeds about 5 molecules. The nucleation behavior of CO_2 un-19 der the present conditions is found to be barrierless in agreement with similar 20 trends previously observed for other compounds at very high supersaturation. 21

²² 1 Introduction

Weakly bound molecular aggregates play an important role in atmospheric processes 23 not only in the Earth's atmosphere but also in other planetary atmospheres. This in-24 cludes their role in the very first steps of aerosol and cloud formation; i. e. in nucleation 25 and early growth processes; which are still rather poorly understood. In the Martian 26 atmosphere, CO_2 clouds are the equivalent of H_2O clouds on Earth^{1,2,3,4}. In laboratory 27 studies, many different techniques have been used to generate and characterize weakly 28 bound molecular aggregates, also with the aim to learn more about nucleation and early 29 cluster growth. Infrared spectroscopy has proven to be particularly useful in this con-30 text, not only providing structural information on small clusters but also on the phase 31 and morphology of very large aggregates. Small oligomers are typically generated in 32 free supersonic or slit nozzle expansions and characterized with high resolution infrared 33 or Fourier transform infrared (FTIR) spectroscopy (see refs.^{5,6,7,8,9,10,11,12,13,14,15,16,17} and 34 references therein). An independent determination of the cluster size is usually not nec-35 essary for the very small clusters because the infrared spectra change pronouncedly from 36 cluster size to cluster size thus enabling unambiguous assignments. Very large aggregates, 37 containing billions of molecules, have been studied in collisional cooling cells with FTIR 38 spectroscopy^{1,18,19,20,21,22,23,24,25,26,27,28}. In this size range, the features in the infrared spec-39 tra are almost insensitive to the aggregate size so that sizing does not pose a particular 40 issue here^{29,30,31,32}. The formation of aggregates with less than $\sim 10^4$ molecules, how-41 ever, is very challenging in collisional cooling cells, so that this size range usually remains 42 unexplored. Laval expansions in combination with FTIR spectroscopy provide a mean 43 to bridge the gap between infrared studies of small oligomers and those performed in 44 collisional cooling cells on very large aggregates^{33,34,35,36,37,38,39}. When the expansion is 45 probed with infrared spectroscopy in the uniform postnozzle flow 34,39 it has the addi-46 tional advantage that the cluster temperature is well-known, similar to collisional cooling 47 cells. This is not the case in free supersonic or slit nozzle expansions where clusters are 48 not probed under thermal equilibrium conditions. However, the issue in the intermediate 49 cluster size range accessible by Laval expansions is the determination of the cluster size 50

distribution. Here, an independent accurate method for cluster sizing is essential because
the expansions produce broad size distributions and the infrared spectra are strongly
size-dependent.

To account for this, the present work combines Laval nozzle expansions with FTIR 54 spectroscopy and mass spectrometry, both of which probe the expansion in the uni-55 form postnozzle flow. For CO_2 aggregates, mass spectrometry offers several advantages. 56 Firstly, through the exact mass it provides information on the cluster size distribution; i. 57 e. on the mass and the relative abundance of clusters; and for each size on the number of 58 molecules per cluster. Secondly, magic number clusters appear in the mass spectra and 59 provide information on the cluster structure through geometrical analysis^{40,41,42}. It has 60 been shown in previous studies through the observation of so-called shell and subshell 61 closings that CO_2 clusters with more than about 25-55 molecules form cuboctahedral 62 shapes with an fcc crystal structure 40,41,42,43,44,45 . Furthermore, CO₂ clusters show very 63 distinct features in the mid-infrared region due to strong dipole coupling between the 64 different CO_2 molecules in the clusters, which is also referred to as vibrational exciton 65 $coupling^{31,46}$. As a consequence of the dominant dipole coupling, vibrational bands are 66 unusually sensitive to the internal structure and the morphology of the clusters. Here, we 67 focus on the asymmetric stretching band of the CO_2 clusters because it is the strongest 68 vibrational band with the biggest effects from exciton coupling. The experimental results 69 are complemented by vibrational exciton calculations, for which we use the information on 70 the cluster size distribution and cluster structure from mass spectrometry. The mass spec-71 tra cannot provide structural information for clusters with less than about 55 molecules. 72 In this size range, we use force field (FF) and density functional (DFT) calculations for 73 the determination of the cluster structures. 74

$_{75}$ 2 Experiment

Except for the infrared part, the experimental setup (Fig. 1) has been described in rot detail in previous publications^{47,48,49,50,51}. CO_2 clusters are generated in pulsed Laval

expansions and characterized in the uniform postnozzle flow by mass spectrometry and 78 Fourier transform infrared spectroscopy (FTIR). We use mass flow controllers to regulate 79 the flow of the carrier gas Ar (PanGas, 5.0) and the condensable gas CO₂ (PanGas, 4.5). 80 For the nucleation measurements, we add small amounts of CH_4 (Messer Schweiz, 5.5) 81 to the carrier gas in order to change the flow temperature slightly and thus the super-82 saturation in fine steps (see section 4.1). The gas mixture is supplied to the stagnation 83 volume (stagnation pressure p_0 , stagnation temperature T_0) by two feeding values (not 84 shown). The opening times of the values are $6 \,\mathrm{ms}$ and $41 \,\mathrm{ms}$ for the mass spectrometric 85 and the infrared spectroscopic measurements, respectively. From the stagnation volume, 86 the gas mixture is then expanded through the Laval nozzle into the first vacuum chamber. 87 The Laval nozzle generates a uniform flow at the nozzle exit, which is extended into the 88 postnozzle flow region by matching the pressure in the first vacuum chamber to the flow 89 pressure $p_{\rm F}$. The impact pressure $p_{\rm I}$ is measured as a function of the axial distance l with 90 pressure transducers. The flow temperature $T_{\rm F}$ is determined from p_0 and $p_{\rm I}$ using the 91 Rayleigh-Pitot relation, and assuming isentropic relations and ideal gas behavior^{50,51,52}. 92 In this work, we use two Laval nozzles with flow pressures $p_{\rm F}$ of 35 Pa and 33 Pa, respec-93 tively, and axially averaged flow temperatures of $\overline{T}_{\rm F}$ of 29.4 \pm 1.2 K and 42.6 \pm 1.6 K, 94 respectively. An additional Laval nozzle with $\overline{T}_{\rm F} = 47.5 \pm 1.2 \,{\rm K}$ and $p_{\rm F} = 40 \,{\rm Pa}$ is used 95 to record the gas phase spectra (CO₂ concentration 7%) in Figs. 4, 8a, 10a and 11a. The 96 Laval nozzle is mounted on a translation stage so that the axial distance l can be changed 97 in steps as small as 1 mm over the whole range of the stable postnozzle flow of $l_{\rm max}$ = 98 100 mm. This allows us to observe the temporal cluster evolution over a time scale of \sim 99 $200 \,\mu\text{s}$ with a temporal resolution of $\sim 2 \,\mu\text{s}$. The fixed positions of both the mass and the 100 infrared spectrometers required to perform two consecutive measurements to ensure that 101 the same region of the postnozzle flow is probed with both methods. For that purpose, 102 the Laval nozzle is moved between the two measurements so that the distance of the 103 nozzle exit to the infrared beam is identical to the distance of the nozzle exit to the skim-104 mer of the mass spectrometer. In other words, for the infrared measurements the axial 105 distance l is the nozzle exit to infrared beam distance, while for the mass spectrometric 106

studies l corresponds to the nozzle exit to skimmer distance (see Fig. 1).

For the mass spectrometric measurements, the central part of the Laval expansion is 108 sampled by a skimmer (1 mm diameter) into the mass spectrometer, where the neutral 109 clusters are ionized just above the first ionization threshold by single vacuum ultraviolet 110 (VUV) photons from a home-built, low fluence table top VUV laser^{47,48,49,53}. It has been 111 shown that this ionization method is a comparatively soft ionization method even for 112 weakly bound clusters^{54,55,56,57,58}. The VUV light is generated by resonance-enhanced 113 two-color four-wave mixing in a Kr gas expansion at $20 \text{ Hz}^{50,53}$. We use a photon en-114 ergy of $13.8 \,\mathrm{eV}$ (89.8 nm) which is close to the ionization threshold of CO_2 monomer 115 $(13.778 \text{ eV}, {}^{59})$. The photon flux is on the order of $\sim 10^{11}$ - 10^{12} photons/(cm²pulse). The 116 ions are then accelerated by a Wiley McLaren type mass spectrometer and detected by 117 a multichannel plate (MCP) detector. We use high extraction voltages up to 30 kV to 118 achieve high sensitivity. In addition, for the cluster studies the monomer ion is selectively 119 deflected by a pulsed electric field applied to a plate located in front of the MCP detector 120 to avoid saturation effects 48,50,51 . 121

The infrared measurements are performed with a Bruker IFS 66v/s FTIR spectrome-122 ter and a liquid nitrogen cooled HgCdTe (MCT) detector. The spectrometer, the infrared 123 beam path, and the detector chamber are evacuated to ~ 7 mbar and are connected to 124 the first vacuum chamber with two KBr windows (see Fig. 1). The infrared beam is 125 focused onto the center of the Laval expansion to maximize the signal from the clusters 126 located in the cold core of the Laval expansion. The pathlength (distance between the 127 two KBr windows) is $\sim 350 \,\mathrm{mm}$ and the width of the Laval expansion (cluster region) 128 is $\sim 10 \,\mathrm{mm}$. For the infrared measurements, the pulsed feeding values are triggered by 129 the FTIR spectrometer. The opening times of the pulsed values is increased to 41 ms 130 to match the minimum time required for recording an interferogram in the steady state 131 region of the pulsed Laval expansion, and the repetition rate was set to 10 Hz. Note that 132 the flow conditions remain identical to those for the mass spectrometric measurements. 133 The measurements are performed with the RapidScan option with a spectral resolution 134 of $1.5 \,\mathrm{cm}^{-1}$. Typically, 9600 interferograms are averaged and then Fourier transformed. 135

The spectra are then converted to absorbance spectra using spectra of the empty chamberas background.

The combination of low spectral resolution $(1.5 \,\mathrm{cm}^{-1})$ and low gas pressures (< 138 1 mbar) in the vacuum chamber leads to pronounced artifacts in the CO₂ gas phase 139 infrared spectra. This is exemplified in Fig. 2. The intrinsic line widths of the rotational 140 transitions of gaseous CO_2 are very narrow. Therefore, if spectra are recorded at low 141 total gas pressure, as in our Laval expansions ($< 1 \,\mathrm{mbar}$), with low spectral resolution 142 this results in false relative intensities of the different rotational transitions in the CO_2 143 gas phase spectra. Two examples for spectral resolutions of $1.5\,\mathrm{cm}^{-1}$ and $0.25\,\mathrm{cm}^{-1}$ are 144 shown in the top part of Fig. 2. Neither of these two spectra shows the correct intensity 145 distribution of gaseous CO_2 . As the bottom part shows, pressure broadening removes 146 these artifacts when the total pressure is increased to about 1 bar by addition of Ar gas. 147 The maximum resolution and the maximum pressure in the Laval expansion cannot be 148 increased beyond $1.5 \,\mathrm{cm}^{-1}$ and above 1 mbar (top black trace in Fig. 2) so that the gas 149 phase artifacts cannot be avoided. As a result of the limited resolution, subtraction of 150 gas phase contributions is difficult and (residual) gas phase contributions cannot be easily 151 distinguished from the broad cluster features. 152

153 **3** Calculations

¹⁵⁴ 3.1 FF and DFT calculations

For the force field (FF) calculations, the artificial bee colony (ABC) algorithm is 155 employed by using the ABCluster 1.5 program to generate hundreds to thousands of low 156 energy isomers of $(CO_2)_n$ clusters with n up to $600^{60,61}$. The CHARMM force field⁶² is 157 used for the CO_2 molecule (see Table S1 in in the Supporting Information). The struc-158 ture of the 15 energetically lowest lying isomers for each cluster size up to n = 38 is 159 further optimized with density functional theory (DFT). All DFT computations were 160 performed with the Gaussian09 program package⁶³. Three functionals - B3LYP^{64,65,66}, 161 B2PLYP-D⁶⁷, and M06-2X⁶⁸ - are tested for n = 1-4 (see Table S2 in in the Supporting 162

Information). Pople's 6-31+G(d) basis set is used for all the atoms up to n = 25 and 163 6-31G(d) for larger clusters up to $n = 38^{69}$. We found the three functionals to result 164 in minimum structures with essentially the same structural characteristics. This is in 165 agreement with the findings of previous studies^{70,71}. Furthermore, Lemke et al.⁷⁰ showed 166 that for $(CO_2)_n$ clusters with n up to 16, the M06-2X functional provides reliable results 167 compared with benchmark calculations at the CCSD(T) level of theory. Therefore, the 168 M06-2X functional is used here for larger clusters up to n = 38. All structures are opti-169 mized without any symmetry constraint. Harmonic vibrational frequencies are calculated 170 to confirm that the optimized structures are real minima, and to simulate infrared spectra 171 of the clusters for comparison with vibrational exciton calculations (see next subsection). 172 In most cases, the most stable isomer generated from the FF search is also the most 173 stable one after optimization at the M06-2X/6-31+G(d) level. The main change of the 174 structures upon optimization is an overall decrease of the intermolecular distances in the 175 cluster with additional rotations of some specific CO_2 molecules in the cluster. Based on 176 these results, we use the lowest energy structure from FF calculations also for the clusters 177 with n = 39-50, for which DFT/M06-2X optimization is computationally too expensive. 178 We also considered the minimum structures of small $(CO_2)_n$ clusters studied in refs.^{44,72}. 179 The global minimum structures identified in our study are either the same or more stable 180 structures compared with this previous investigation. 181

The C=O bond distance of linear CO_2 is optimized to be 1.163 Å, which is in excellent 182 agreement with the experimental value of 1.162 Å^{73} . The antisymmetric stretching mode 183 (ν_3) of CO₂ is calculated to be 2468 cm⁻¹. To match the experimentally measured ν_3 184 of $2349 \,\mathrm{cm}^{-174}$, a scaling factor of 0.9518 has to be applied. This scaling factor is also 185 used to scale the calculated vibrational frequencies of clusters with n = 2-25 in the ν_3 186 region, while for clusters with n = 26-38 a scaling factor of 0.9450 is employed. The latter 187 corrects for the difference between vibrational frequencies of $(CO_2)_{25}$ calculated with the 188 6-31G(d) and 6-31+G(d) basis sets using the M06-2X functional. Note that we do not 189 use different scaling factors for clusters $(CO_2)_n$ with n = 2-13, for which high resolution 190 IR spectroscopy measurements are available 5,6,7,75,76,77,78 . Rather, we focus on the general 191

trends of the infrared band shapes as a function of cluster size. Structures and infrared 192 spectra for the obtained isomers for $(CO_2)_n$ clusters with n = 2-4 are provided in Figs. 193 S1 and S2 in the Supporting Information. Figs. S3 and S4 in the Supporting Information 194 present the optimized most stable structures of $(CO_2)_n$ for n = 5-38 from M06-2X and 195 selected structures for n = 40-600 from the FF calculations, respectively. The Cartesian 196 coordinates of the energetically lowest lying isomers for n = 2-38 and n = 40, 45, and 197 50 are provided in Table S3. Note that the second most stable structures are typically 198 about 2-4 kJ/mol higher in energy than the most stable ones using the M06-2X method. 199

²⁰⁰ 3.2 Vibrational exciton calculations

We have previously shown that infrared spectra of CO_2 clusters are dominated by 201 contributions from resonant dipole coupling and can thus be reliably simulated using 202 vibrational exciton calculations^{31,46,79}. The resonant dipole coupling term is dominant 203 for molecular systems with strong molecular transition dipole moments (> 0.1-0.2 D) and 204 small intermolecular distances (< 5-7 Å). The transition dipole moment of CO₂ in the re-205 gion of the antisymmetric stretching vibration (ν_3 band) is on the order of $0.32 D^{79,80}$ and 206 the intermolecular distances in the clusters are in the range of 3-4 Å^{31,78}. The vibrational 207 Hamiltonian \hat{H} can be written as^{31,79,81}: 208

$$\hat{H} = \hat{H}_0 + \hat{H}_D \tag{1}$$

 \hat{H}_0 is the sum over the vibrational Hamiltonians of the uncoupled molecules and \hat{H}_D includes all pairwise dipole-dipole interactions between molecules in the cluster. \hat{H}_D is given by:

$$\hat{H}_{\rm D} = \sum_{i < j} -\frac{1}{4\pi\epsilon_0} \overrightarrow{\mu_i} \frac{3(\overrightarrow{\mu_j} \cdot \overrightarrow{r_{ij}}) \cdot \overrightarrow{r_{ij}} - (\overrightarrow{r_{ij}} \cdot \overrightarrow{r_{ij}}) \cdot \overrightarrow{\mu_j}}{\overrightarrow{r_{ij}^{5}}}$$
(2)

 $\overrightarrow{r_{ij}}$ is the displacement vector between the centers of mass of the two molecules *i* and *j* and $\overrightarrow{\mu}$ is the dipole moment operator. Up to first order terms in the vibrational coordinates, the model contains only two input parameters in addition to the cluster structure, which are the transition wavenumber of the uncoupled molecule $\widetilde{\nu}_{\rm M}$ and the molecular transition

dipole moment $\delta \mu = \langle 0 | \mu | 1 \rangle$. For the present calculations, we use $\tilde{\nu}_{\rm M} = 2355 \, {\rm cm}^{-1}$ and 216 $\langle 0|\mu|1\rangle = 0.32 \,\mathrm{D}^{46}$. The vibrational eigenvalues and eigenfunctions of the cluster are 217 obtained by diagonalization of \hat{H} or through calculation of the autocorrelation function 218 of the dipole moment^{22,31,79}. For the cluster structures, we use the energetically lowest 219 lying structures as obtained from the FF after further optimization with DFT for n = 2-38, 220 while in the size range n = 39-50 we directly use the energetically lowest lying structures 221 from FF calculations. All larger clusters were modeled as cuboctahedral structures with 222 fcc crystal structure in agreement with the results from previous studies 40,41,43,44,45,72,82 . 223 For this purpose, an fcc crystal structure is constructed by copying a CO₂ unit cell in three 224 directions, from which molecules are removed until a perfect cuboctahedron was obtained. 225 These so-called closed shell cuboctahedra have only very distinct sizes. To model clusters 226 with size between these special closed shell structures, we remove molecules from faces. 227 The removal of complete faces result in subshell closed cuboctahedra. We refer to all 228 these structures simply as fcc cuboctahedral structures. 229

The reliability of the exciton approach for CO_2 clusters was verified in our previous 230 publications^{31,46,79}. Here, we add a more extensive comparison with quantum chemical 231 calculations for the cluster size range n = 2-38 (Fig. 3 and Fig. S5 in the Supporting 232 Information). Fig. 3 shows selected results for n = 13, 19, 28 and 38. The top (black) 233 and the bottom (red) trace are infrared spectra calculated with the exciton approach 234 and with DFT, respectively. The same cluster structures as obtained from optimization 235 with DFT at the M06-2X level of theory are used as input structures for both vibrational 236 calculations. The similar infrared band shapes verify that resonant dipole coupling is 237 able to capture the main features in the infrared spectra (see also Fig. S5 for more data). 238 This is an important result because the exciton approach is the only method that can be 239 applied to even larger clusters containing many thousands of molecules. We mentioned 240 above that the optimization of the FF generated structures with DFT mainly results in a 241 decrease of the intermolecular distances of the molecules in the clusters. To evaluate the 242 influence of this decrease on the infrared spectra we show in the middle (blue) trace of 243 Fig. 3 infrared spectra calculated with the exciton model but this time for FF structures 244

without further optimization by DFT. The agreement with the exciton spectra in the top 245 (black) trace is very good. The shorter intermolecular distances after DFT optimization 246 results in a slightly stronger dipole coupling, which explains the slightly broader overall 247 band width of the spectra in the top trace. This comparison mainly confirms that our 248 approach to use DFT optimized structures for n < 39 and FF structures for n = 39-50249 has almost no effect on the infrared spectra. Based on the favorable comparisons in Fig. 3 250 and Fig. S5 in the Supporting Information, we will use throughout the remainder of this 251 work exclusively exciton calculation for the modeling of infrared spectra for all cluster 252 sizes. The cluster sizes and the relative abundances of different cluster sizes will be taken 253 from the experimental mass spectra, and as mentioned above we will use DFT optimized 254 structures for n < 39, FF structures for n = 39-50, and fcc cuboctahedral structures for 255 larger clusters. 256

²⁵⁷ 4 Results and discussion

²⁵⁸ 4.1 Small clusters and nucleation

We have recently shown that mass spectrometry in the uniform postnozzle flow of a 259 Laval nozzle allows one to capture the very first steps of gas phase nucleation/condensation 260 at the molecular level^{47,48,49}. Infrared spectroscopy could provide additional information 261 on cluster structures in this size range, where the average cluster size < n > and the max-262 imal cluster size n_{max} typically lie below about ten and a few ten molecules, respectively. 263 The thermodynamic requirement for nucleation to take place is that the supersatura-264 tion S is larger than 1, where $S = \frac{p_{\text{cond}}}{p_{\text{eq}(T_{\text{F}})}}$ with the partial pressure of the condensable 265 (here CO₂) $p_{\rm cond}$ and the equilibrium vapor pressure of the condensable $p_{\rm eq(T_F)}$ at the 266 flow temperature $T_{\rm F}$. However, nucleation can only be observed if it occurs in the time 267 window that is accessible by a given experiment. As explained in refs.^{47,48,49}, we thus 268 refer to conditions where S > 1 but nucleation can not yet be observed as *subcritical*, and 269 conditions at which nucleation just becomes observable as *supercritical*. The first steps 270 of nucleation/condensation can then be followed by tuning the conditions in very fine 271

steps from subcritical to supercritical conditions. In the present work this tuning was achieved by adding small amounts of methane gas (maximum of less than 10%) to the argon carrier gas while recording infrared and mass spectra at a constant axial distance. Successive addition of methane gas results in very small (< 0.5 K) increases of $T_{\rm F}$, which in turn results in a continuous decrease of the average and maximum cluster sizes until nucleation/condensation is completely inhibited ^{47,48,49}.

The middle and the lower traces in Fig. 4 show two example infrared spectra recorded 278 at methane concentrations of 5% and 2.46%, respectively, which correspond to maximum 279 cluster sizes of $n_{\text{max}} = 21$ and $n_{\text{max}} = 33$, respectively (see mass spectra in Fig. 5b). 280 Surprisingly, the two spectra look identical even though the cluster sizes differ substan-281 tially. This also holds for infrared spectra (not shown) recorded at the other methane 282 concentrations/cluster sizes (see mass spectra in Fig. 5b). For such small clusters one 283 expects substantially different infrared spectra for different cluster sizes; i. e. just the 284 opposite of the experimental results. The observed independence of the infrared spectra 285 from the cluster size can be explained by comparison with the pure gas phase spectrum in 286 the upper trace of Fig. 4. It reveals that the cluster spectra are dominated by gas phase 287 contributions to such an extent that no cluster features are visible. Under nucleation 288 conditions, the cluster number concentrations lies ~ 3 orders of magnitude below the 289 $\rm CO_2$ monomer number concentration, which is on the order of ~ 10¹⁴ cm⁻³. Given the 290 low infrared monomer signal (low signal-to-noise (S/N) ratio), it is thus not surprising 291 that our infrared experiment is not sensitive enough to detect any cluster signals under 292 these expansion conditions. 293

Even though we cannot record infrared spectra during the first steps of nucleation/condensation, Fig. 5b shows that the higher sensitivity of mass spectrometry allows us to observe the evolution of the cluster size distribution under these conditions. The maximal cluster sizes n_{max} indicated by black arrows vary over the ranges from about 5 to 38 molecules. Note that at methane concentrations higher than the ones used for the top spectrum in Fig. 5b only monomer is observed (subcritical conditions). The detailed experimental information of the cluster size distributions (size and relative abundance) together with

modeling (structure and exciton modeling, see section 3.2) allows us at least to predict 301 the infrared spectra. As mentioned earlier, the transition to fcc cuboctahedral structure 302 is expected in the region of $n \sim 25-55$ molecules^{40,41,42,44,43,45} so that we can safely as-303 sume that with an overall largest cluster size of $n_{\text{max}} = 38$ the dominating cluster sizes do 304 not yet have cuboctahedral structure. We thus used for each cluster size the structures 305 of the energetically lowest lying isomer as predicted by the FF calculation and further 306 optimized by DFT (see section 3.1). The corresponding modeling results are shown in 307 Fig. 5a. The simulated infrared spectra show a pronounced increase by about a factor 308 of four of the band width with increasing $n_{\rm max}$. This broadening can be explained as 309 follows: in the cluster size range n < 38, both the geometrical structure and the infrared 310 spectra of individual cluster sizes change drastically from one cluster size to another (see 311 section 3.1). Therefore, the larger n_{max} becomes, the more different cluster sizes with 312 different infrared spectra contribute to the overall infrared spectrum. We had already re-313 ported on infrared spectra of CO_2 clusters with average sizes of $< n > \leq 100$ in a previous 314 study (see Fig. 5 in ref.³⁴). However, for lack of an accurate sizing method the average 315 size could only be estimated in that work to be likely below 100 without any further 316 specification of the lower bound. The largest average cluster size in the present study is 317 < n >= 9 (see bottom spectrum in Fig. 5b). The spectral differences (band widths and 318 structures) between the present infrared spectra and the spectra in Fig. 5 of ref. 34 thus 319 hint that the average size of the latter was above $\langle n \rangle \sim 10$, finally providing a lower 320 bound for the size estimate of those spectra. 321

In our previous papers on nucleation of water, toluene, and propane ^{47,48,49}, we sug-322 gested that the type of nucleation behavior can be extracted from graphs showing $n_{\rm max}$ 323 as a function of $\ln S$ (see for example Fig. 6a and Fig. 4 in ref.⁴⁷). We found two types of 324 nucleation behavior: a steplike and a gradual increase of the cluster size with increasing 325 supersaturation. For water and propane a systematic trend from a steplike behavior at 326 lower $\ln S$ to a gradual at higher $\ln S$ was found. A steplike increase of n_{\max} with increas-327 ing $\ln S$ was considered to be indicative of the presence of a nucleation barrier, while a 328 gradual increase was suggested to hint at a barrierless condensation process (spinodal 329

decomposition). Our recent study on water nucleation, however, challenges this simple 330 interpretation, indicating that a steplike increase could also be caused by a kinetic bot-331 tleneck other than a free energy barrier⁴⁷. The highest $\ln S$ in all these previous studies 332 was around 104. The current CO_2 data are recorded at an even higher $\ln S$ around 150. 333 Thus, from the previously observed trend one would clearly expect CO_2 condensation to 334 take place in a barrierless regime; i. e. one would expect to observe a gradual increase of 335 $n_{\rm max}$ with increasing $\ln S$. Fig. 6a shows that this is indeed the case and CO₂ also seems 336 to follow the trend observed for the other compounds. It also reveals that the critical 337 supersaturation for CO_2 condensation under these conditions lies at $\ln S \sim 138$. Cluster 338 size distributions recorded as a function of $\ln S$ at a constant nucleation/growth time 339 (constant axial position in the postnozzle flow) provide information on the nucleation 340 behavior (Fig. 6a) and on critical cluster sizes, which for barrierless condensation is the 341 monomer. As described in detail in ref.⁴⁷, the nucleation/growth rate J can be extracted 342 from the total cluster number concentration $N_{\rm cluster,tot}^{\rm CO_2}$ recorded as a function of the nu-343 cleation/growth time t, where t is varied by varying the axial distance in the postnozzle 344 flow by fine steps. $N_{\text{cluster,tot}}^{\text{CO}_2}$ is the sum over all cluster number concentrations. Fig. 6b 345 shows $N_{\text{cluster,tot}}^{\text{CO}_2}$ as a function of t for $\ln S = 160$. At early nucleation times, monomer 346 depletion and more complex growth processes (cluster agglomeration and coagulation) 347 are negligible. At these early t, $N_{\text{cluster,tot}}^{\text{CO}_2}$ is proportional to t^{47} . A linear fit to the data 348 at early t predicts a value of $J \sim 1 - 2 \cdot 10^{15} \,\mathrm{cm}^{-3} \mathrm{s}^{-1}$ at $\ln S = 160$, which in the case 349 of barrierless condensation is rather a growth than a nucleation rate in its usual sense⁴⁷. 350 To the best of our knowledge these are the first data for CO_2 condensation at such low 351 temperatures ($\overline{T}_{\rm F} = 29.4 \pm 1.2 \,{\rm K}$) and high supersaturations. The uncertainty of the 352 nucleation rate constants are estimated to be one order of magnitude (for more informa-353 tion see⁴⁷). CO_2 nucleation rates have previously been determined to lie in the range 354 $J \sim 10^{17} - 10^{21} \,\mathrm{cm}^{-3} \mathrm{s}^{-1}$ at a supersaturation of $S \sim 10$ and temperatures of 160-190 K⁸³. 355 These experiments were also performed in Laval nozzles. However, in contrast to our 356 case condensation most likely takes place in the presence of a nucleation barrier under 357 the conditions of ref.⁸³. 358

359 4.2 Intermediate cluster sizes

In this section, we present infrared and mass spectra of intermediate cluster sizes, 360 which cover the average cluster size range from $\langle n \rangle \sim 20-330$ ($n_{\rm max} \sim 70-710$). This 361 coincides with the size range where the transition to fcc cuboctahedral structures takes 362 place around $n \sim 25-55^{40,41,42,43,44,45}$. The appearance of fcc cuboctahedral clusters is 363 exemplified in the mass spectrum in Fig. 7. For cluster sizes with $n \gtrsim 55$, different 364 minima are observed in the mass spectra, which are labeled with asterisks in the inset 365 in the figure. Such patterns were observed for different substances; e. g. CO_2 , SF_6 , 366 and rare gases; and were attributed to shell and subshell closings^{40,41,42}. These cluster 367 sizes correspond to particularly stable cluster structures (magic clusters), which in the 368 case of CO_2 appear as local minima in the mass spectra because of their lower ionization 369 efficiency. Note that as a consequence of the latter, the relative abundances of these 370 clusters is underestimated from the ion signals in the mass spectra. We have confirmed 371 the cuboctahedral structure of these special clusters for all mass spectra following the 372 same analysis as proposed in refs.^{40,41,42}; and based on the results from refs.^{40,43,44,45,82} 373 we assume fcc crystalline structures. Using all this information, we make the following 374 assumptions for the vibrational exciton calculations presented in Figs. 8a and 10a (see 375 also section 3.2): i) The relative abundance of different cluster sizes are taken from 376 the experimental mass spectra. ii) For clusters with $n \leq 50$, the exciton calculations 377 are performed for cluster structures obtained from FF calculations and for $n \leq 38$ from 378 FF calculations with subsequent optimization by DFT, iii) For clusters with $n \gtrsim 50$, we 379 use fcc cuboctahedral structures for the exciton calculations. Based on the additional 380 knowledge on cluster size, abundances, shape and internal structure, this is the best 381 assumption we can make at this point, and to the best of our knowledge also the most 382 detailed compared with previous infrared simulations of CO_2 clusters. 383

Fig. 8 shows results for the cluster size range $\langle n \rangle \sim 20-60$ ($n_{\rm max} \sim 70-190$); i. e. the range where the transition to fcc cuboctahedral structures takes place. Panel a contains the experimental (black lines) and the calculated (red lines) infrared spectra together with an experimental CO₂ gas phase spectrum (top trace). The comparison of

the experimental spectra with the gas phase spectrum reveals a very high gas phase con-388 tribution in the cluster spectra, which decreases with increasing cluster size. The major 389 gas phase contributions (bands around $2380 \,\mathrm{cm}^{-1}$, $2350 \,\mathrm{cm}^{-1}$ and $2320 \,\mathrm{cm}^{-1}$) are labeled 390 with black arrows in the cluster spectrum with $\langle n \rangle = 21$. We have tried to subtract 391 gas phase spectra from the cluster spectra to compensate gas phase contributions and 392 retrieve pure cluster spectra. However, this was not successful because of the the low 393 S/N ratio of the spectra and the limited spectral resolution $(1.5 \,\mathrm{cm}^{-1})$. Nevertheless, 394 cluster features are visible in the spectra in agreement with the predictions from exciton 395 calculations (red spectra). The clearest cluster feature in the experimental spectra is a 396 peak at ~ 2361 cm⁻¹, which is labeled with a red arrow in the bottom spectrum. This 397 peak becomes more prominent with increasing cluster size and at the same time shifts 398 by $\sim 1 \,\mathrm{cm}^{-1}$ from $\sim 2361 \,\mathrm{cm}^{-1}$ to $\sim 2362 \,\mathrm{cm}^{-1}$. The same trend is also seen in the 399 exciton simulations, where the peak at $2359.5 \,\mathrm{cm}^{-1}$ becomes more prominent and shifts 400 to $2360 \,\mathrm{cm}^{-1}$ with increasing cluster size. Since these infrared spectra cover the range 401 of the transition to increasingly higher contributions from fcc cuboctahedral structures 402 with increasing cluster size we were wondering whether this prominent peak could orig-403 inate from fcc cuboctahedral structures. For this purpose we have performed exciton 404 simulations for cuboctahedral clusters of different sizes (see Fig. 9). These spectra in-405 deed show a pronounced peak at ~ $2361 \,\mathrm{cm}^{-1}$ for clusters with $n \sim 55-90$, which shifts 406 from $2359 \,\mathrm{cm}^{-1}$ to $2362 \,\mathrm{cm}^{-1}$ with increasing size. Since this cluster size range agrees 407 with the average cluster size in the experimental spectra (Fig. 8a) we conclude that the 408 emerging pronounced peak in the experimental infrared spectra is likely a signature of 409 cuboctahedral cluster structures in this size range. 410

The infrared spectra in Fig. 5 of ref.³⁴ were recorded at the same temperature (~ 29 K) as those in Fig. 8a, and were estimated to cover a similar cluster size range ($< n > \le$ 100). Further above, we have determined a lower bound of $< n > \sim$ 10 for the smallest clusters in ref.³⁴ (see top trace in Fig. 5). The spectra in Fig. 5 of ref.³⁴ show indeed similar features as those in Fig. 8a. This holds in particular for the top two spectra in Fig. 5 of ref.³⁴ compared with the calculated spectrum for < n > = 21 in Fig. 8a,

which show similar overall band widths and a main broad band below and an additional 417 pronounced shoulder above $2360 \,\mathrm{cm}^{-1}$, respectively. For larger clusters, the shoulder 418 disappears continuously with increasing cluster size in both studies, and the double band 419 structures evolves into a single band around $2360 \,\mathrm{cm}^{-1}$. In this size range, however, the 420 overall band widths in Fig. 5 of ref. 34 is larger compared with the present spectra. Since 421 the two different studies were performed at the same temperature in the uniform flows of 422 Laval nozzles this thus hints rather at a difference in the cluster size (distribution) than 423 in the cluster structure. While larger clusters do not show further band broadening (see 424 Fig. 10), a higher contribution of small clusters would explain such a broadening (see e. 425 g. bottom spectra in Fig. 5a). It seems thus plausible that the upper bound of $\langle n \rangle =$ 426 100 for the largest clusters provided for Fig. 5 of ref. 34 was too high, which would not be 427 surprising in view of the fact that this was a very crude estimate that was not based on 428 an independent size determination as in the current study. 429

Fig. 10 covers the next higher cluster size range from $< n > \sim 40-330$ ($n_{\rm max} \sim 110-$ 430 710). Again, the spectra of the smaller clusters - in particular that for < n >= 41 in 431 panel a - are dominated by gas phase contributions (see black arrows and the pure gas 432 phase spectrum Fig. 8a). For the larger clusters ($\langle n \rangle \geq 138$), however, the gas phase 433 does no longer dominate and the cluster contribution (broad band around $2360 \,\mathrm{cm}^{-1}$) is 434 clearly visible in the spectra in Fig. 10a, in particular when compared with the exciton 435 simulations (see red spectra in panel a). Furthermore, the S/N ratio in the experimental 436 spectra is now high enough to retrieve decent difference spectra, which was not the case 437 in Figs. 4 and 8. Instead of subtracting the gas phase spectrum (top spectrum in panel a) 438 from the experimental spectra we choose to subtract the experimental spectrum recorded 439 for < n >= 41 from the other experimental spectra for two reasons: i) We found the 440 subtraction of the pure gas phase spectrum to provide worse results compared with the 441 subtraction of a small cluster spectrum. This is likely due to the fact that the expansion 442 conditions must be slightly varied when measuring pure gas phase for which cluster 443 formation must be avoided. ii) The subtraction of a small cluster spectrum removes 444 contributions from the cluster size range where fcc cuboctahedral clusters do not yet 445

dominate and thus allows us to clarify at which size the fcc cuboctahedral features start to dominate. The resulting experimental difference spectra (black lines) are shown in Fig. 10b together with exciton simulations for these difference spectra (red lines). The comparison between experiment and simulations shows good agreement, in particular also with respect to the overall band width. It shows that the disagreement of the band width between experiment and simulation in panel a is mainly a consequence of the uncompensated gas phase.

The comparison of the exciton calculations in panels a and b of Fig. 10 shows that 453 the full calculations and the ones for the difference spectra look very similar for the same 454 < n >. Above an average cluster sizes of $< n > \sim 217,$ they are even identical. This shows 455 that the features from the larger clusters in the size distributions completely dominate 456 these infrared spectra, while the contribution from smaller clusters completely vanishes. 457 Not surprisingly, a comparison with Fig. 9 shows that these spectra are dominated by 458 cuboctahedral features. The simulations for cuboctahedra in this figure shows that the 459 spectral region between ~ $2355-2365 \,\mathrm{cm}^{-1}$ is dominated by a single band for $n \sim 55-90$ 460 (see above) and by a double band for n > 90. Even though the spectra in Figs. 10a and b 461 are sum spectra over different cluster sizes, this double band is still visible in the exciton 462 spectra. Also visible is the systematic decrease of the relative intensity of the band at 463 the higher wavenumber with increasing cluster size, in agreement with the simulations 464 in Fig. 9. In the experimental difference spectra (Fig. 10b), the double band structure is 465 not so clearly visible. However, the asymmetric band shape at wavenumbers higher than 466 $\sim 2360 \,\mathrm{cm}^{-1}$ is consistent with the double band structure. 467

468 4.3 Large clusters

Using higher CO₂ concentrations, we were able to record infrared in combination with mass spectra for even larger clusters. The largest cluster size we were able to detect was on the order of $n_{\text{max}} \sim 4300$, which would correspond to a cluster radius of ~ 3.5 nm assuming a spherical shape. These sizes are comparable to the lower cluster size range that can also be reached in collisional cooling cell experiments^{18,19,21,34}. This is a range

in which a comparison between different cluster generation methods (e. g. collisional 474 cooling with Laval expansions) is in principle possible as demonstrated in ref. 34 . A series 475 of infrared spectra recorded in the uniform Laval expansion for the size range $\langle n \rangle \sim$ 476 140-760 $(n_{\rm max} \sim 730-4300)$ is shown in Fig. 11. In comparison with the previous cases, 477 the gas phase contribution to these spectra is comparatively small (see top spectrum), 478 so that these spectra are dominated by cluster features and not by the gas phase. The 479 double band structure (main band at about $2360 \,\mathrm{cm}^{-1}$ and a shoulder at about $2364 \,\mathrm{cm}^{-1}$) 480 described in Fig. 10 is maintained also for the largest clusters (see also exciton simulations 481 in Fig. 11a). Consistent with the decreasing relative intensity of the shoulder in the 482 exciton spectra with increasing cluster size, the experimental spectra show less structure 483 and a less asymmetric band at wavenumbers higher than $\sim 2360 \,\mathrm{cm}^{-1}$. Based on the same 484 arguments as in the previous chapter, we conclude that the infrared spectra of these larger 485 clusters are also dominated by features arising from fcc cuboctahedral clusters. 486

In Fig. 3a in ref.³⁴, Bonnamy et al. reported infrared spectra of clusters in a similar 487 size range as our Fig. 11. Over the whole size range from $< n > \sim 100-10000$, they 488 observed an almost identical single band with an almost perfect symmetric band shape, 489 which only showed a minor shift of the maximum and a slight narrowing of the band with 490 increasing cluster size. These spectra best match the bottom spectrum in our Fig. 11a 491 with $n_{\rm max} \sim 4300$, while the structureless symmetric band shape in ref.³⁴ is not really 492 consistent with our spectra in Fig. 11a for smaller clusters. A major difference between 493 the present study and ref.³⁴ is the lack of an independent accurate size determination in 494 the latter study. A possible explanation could thus be that the average size indicated in 495 Fig. 3a of ref.^{34,39} was not correct for the smaller clusters, and that these smallest cluster 496 had in fact already average size of more that a few thousand molecules (instead of only 497 hundreds of molecules). This would also explain the almost identical symmetric band 498 shape observed for these spectra in ref.³⁴. 499

500 5 Summary

We present a common infrared spectroscopic and mass spectrometric investigation 501 of CO_2 clusters generated in pulsed Laval expansions over the average cluster size range 502 from $< n > \sim 3-760$ (maximum cluster size $n_{\rm max} \sim 5-4300$). To the best of our knowledge, 503 this is the first study that simultaneously uses infrared spectroscopy and mass spectrom-504 etry for cluster characterization in this size range. Cluster formation in a Laval expansion 505 allows us to cover a broad cluster size range, and by using the uniform postnozzle flow 506 to investigate clusters at known well defined temperatures. A pulsed Laval expansion 507 is required to keep the pressure in the mass spectrometer low enough for sensitive mass 508 spectrometric studies. However, the disadvantage of the pulsed Laval expansions com-509 pared with continuous Laval expansions 34,39 is the limitation it poses on the spectral 510 resolution of the infared spectra. With our rapid scan infrared spectrometer, we are lim-511 ited to a resolution of $\sim 1.5 \,\mathrm{cm}^{-1}$, which makes subtraction of gas phase contributions in 512 the cluster spectra very challenging. 513

Mass spectra provide detailed information on the whole cluster size distribution; i. e. 514 the relative abundance of different clusters and the number of molecules in the clusters. 515 This independent size information is used to simulate infrared spectra, which are then 516 compared with experimental infrared spectra. Furthermore, through magic clusters the 517 mass spectra also provide additional information on preferred cluster structures. Consis-518 tent with previous studies, the preferred structure for CO_2 clusters with $n \gtrsim 50$ is fcc 519 cuboctahedral. The comparison of calculated and experimental infrared spectra reveals 520 that cluster size distributions with average sizes < n > of a few ten molecules show 521 a characteristic band around $2360 \,\mathrm{cm}^{-1}$ that originates from the larger clusters in the 522 distribution with fcc cuboctahedral structures. For average sizes that exceed the range 523 $< n > \sim 140-220$, the infrared spectra are completely dominated by the features of fcc 524 cuboctahedral clusters. Even though we find generally good agreement between simu-525 lated and experimental infrared spectra the bands in the experimental spectra tend to 526 be broader compared with the simulations. Uncompensated gas phase contributions are 527 likely one reason for this. Note that the gas phase spectra are not resolved due to our 528

low spectral resolution. Another reasons might include contributions from other crystal
structures (not fcc) or from surface molecules^{29,44,84,85,86}, which could become considerable
when the ratio of surface to core molecules lies close to one^{25,34,87,88}.

We were not able to record infrared spectra during the very first steps of nucle-532 ation/condensation where the average cluster sizes contain only a few molecules because 533 the number concentration of these nucleation clusters was too low and the gas phase 534 fraction too high. However, because of its higher sensitivity we could record mass spectra 535 under these conditions, which at least allows us to calculate infrared spectra for experi-536 mental size distributions. These vibrational exciton calculations - based on experimental 537 mass spectra and cluster structures from force field and DFT optimization - predict a 538 pronounced broadening by a factor of about four when the average cluster sizes exceeds 539 $< n > \sim 5$ as a consequence of the increasing number of cluster sizes with different infrared 540 spectra that contribute to the overall spectrum. From an analysis of the mass spectra, 541 we have also retrieved the nucleation behavior of CO_2 under these conditions. The barri-542 erless condensation at the very high supersaturation of $\ln S \sim 140-160$ is fully consistent 543 with previous trends found for other compounds (see Fig. 4 in^{47}). In addition, we have 544 also retrieved a nucleation rate for CO_2 of $1-2 \cdot 10^{15} \text{ cm}^{-3} \text{s}^{-1}$ at this high supersaturation. 545 The general goal behind our studies is to provide more information about nucleation and 546 early growth at a truly molecular level. The extension to infrared spectroscopy in the 547 present contribution has provided valuable additional information on cluster structures 548 in the early growth regime, which cannot be obtained from mass spectra alone. 549

⁵⁵⁰ Supporting Information

In the Supporting Information, we provide the FF parameters for CO₂, the benchmarking of the DFT functional and the Cartesian coordinates of the energetically lowest lying isomers for n = 2-38 and n = 40, 45, and 50. In addition, we give the structures of the CO₂ clusters for n = 2-38 from M06-2X and selected structures for n = 40-600 from the FF calculations, respectively and analogous figures to Fig. 3 for all cluster sizes with n = 2-38.

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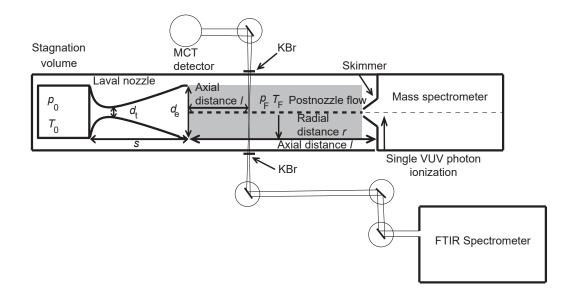


Figure 1: Schematic of the experimental setup ^{49,48}. p_0 , T_0 , p_F and T_F are the stagnation pressure, the stagnation temperature, the flow pressure, and the flow temperature, respectively. d_t , d_e , and s is the throat diameter, the exit diameter, and the length of the Laval nozzle, respectively. r is the radial distance from the center of the expansion. The axial distance l is the distance between the nozzle exit and the skimmer. l can be varied, which corresponds to a variation in the growth time t. The central part of the expansion is sampled into the mass spectrometer by a skimmer, where the clusters are ionized and detected. FTIR measurements were performed in the postnozzle flow of the Laval expansion in positions corresponding to the same axial distance as measured with mass spectrometry.

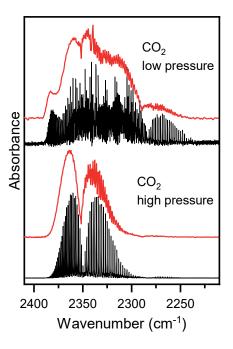


Figure 2: Top: Infrared spectrum of CO_2 at low pressure (< 1 mbar) measured with high (black, 0.25 cm^{-1}) and low (red, 1.5 cm^{-1}) resolution. Bottom: Infrared spectrum of CO_2 at a pressure of about 1 bar measured with high (black, 0.25 cm^{-1}) and low (red, 1.5 cm^{-1}) resolution. The pressure was increased by addition of argon gas. All spectra were measured at room temperature.

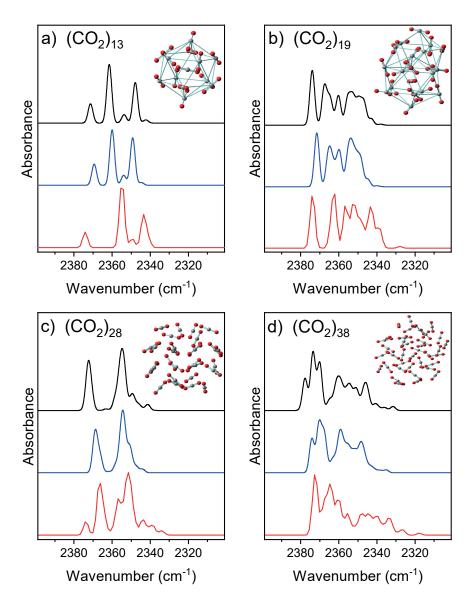


Figure 3: Simulated infrared spectra of the most stable structures of $(CO_2)_n$ (n = 13 (a), 19 (b), 28 (c), and 38 (d)) using Gaussian with optimized M06-2X structures (red, lower), exciton calculations with optimized FF structures (blue, middle), and exciton calculations with optimized M06-2X structures (black, upper) are shown.

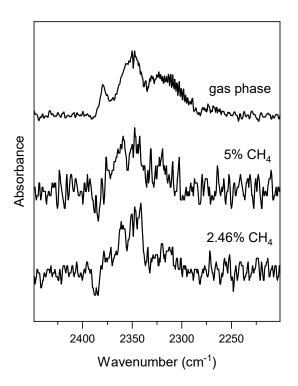


Figure 4: Pure gas phase spectrum (top) and two experimental FTIR spectra under CO_2 nucleation conditions (0.18% CO_2) with 5% (middle) and 2.46% (bottom) methane.

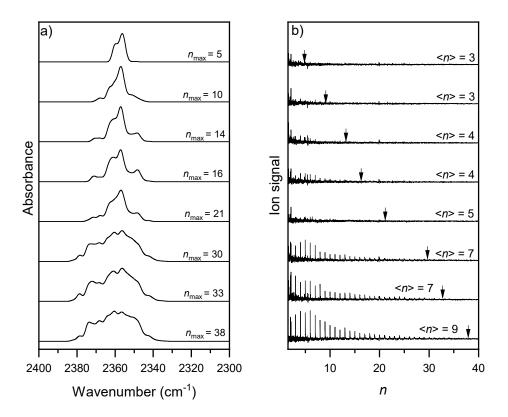


Figure 5: a) Infrared spectra of clusters during nucleation. The spectra are calculated with the exciton model for the cluster size distributions shown in trace b. $n_{\rm max}$ is indicated in the graph. b) Mass spectra of clusters during nucleation at ~ 29 K and 0.18% CO₂ with methane concentrations between 0 and 8.23%. $n_{\rm max}$ is indicated by arrows (values see trace a) in addition to the values of < n >.

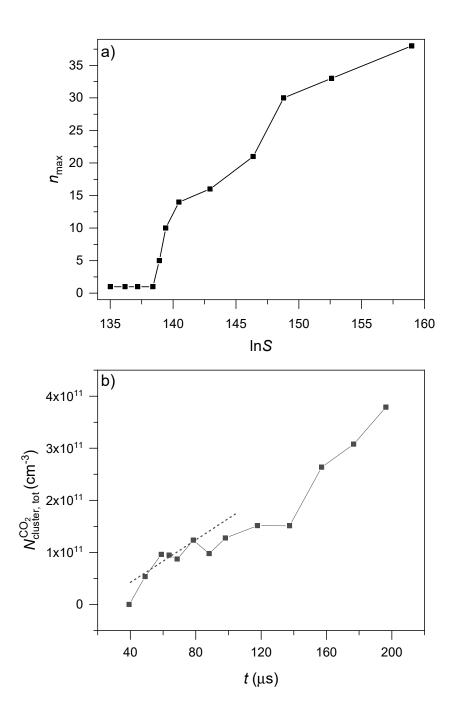


Figure 6: a) $n_{\rm max}$ from Fig. 5b as a function of $\ln S$. The nucleation behavior hints at a barrierless nucleation process which is consistent with the high S value. b) Total cluster number concentration of CO₂ clusters as a function of the nucleation time at constant supersaturation $\ln S \sim 160$. The nucleation/condensation rate is determined by a linear fit (see dashed line) and is on the order of $1-2 \cdot 10^{15} \,\mathrm{cm}^{-3} \mathrm{s}^{-1}$.

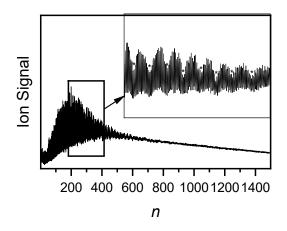


Figure 7: Mass spectrum for 5% CO₂ at ~ 29 K. The inset shows a zoom-in of the part shown by the rectangle. Local minima of the ion signal for cluster sizes $n \gtrsim 55$ are marked with asterisks, these correspond to shell and subshell closings.

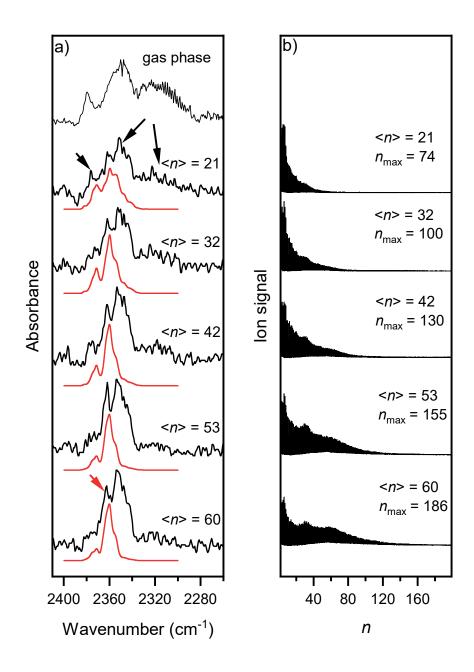


Figure 8: a) Experimental infrared spectra recorded at ~ 29 K for 0.38% CO₂ (black) with respective exciton simulations (red). < n > is indicated for each spectrum. The black arrows in the second top spectrum show where we observe mainly gas phase contributions. The red arrow in the bottom spectrum shows where we observe cluster contributions. A pure gas phase spectrum is shown on top. b) Corresponding mass spectra. < n > and $n_{\rm max}$ are indicated in the figure.

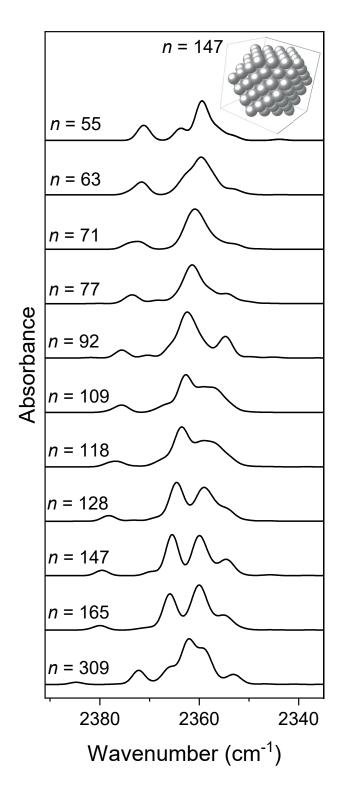


Figure 9: Calculated infrared spectra (exciton calculations) for cuboctahedral structures with n molecules per cluster. A complete shell closed cuboctahedral structure for n = 147 is displayed on top of the graph.

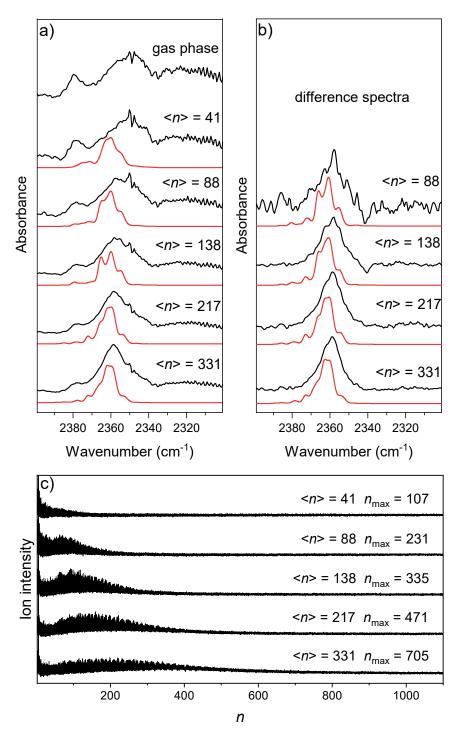


Figure 10: a) Experimental and exciton calculated infrared spectra at ~ 43 K for 2.48% CO_2 for different < n > as indicated for each trace. The experimental spectra are shown in black and the exciton calculations in red. A pure gas phase spectrum is shown on top. b) Experimental difference infrared spectra (black) with corresponding difference exciton simulations (red). The difference spectra were obtained by subtracting the cluster spectrum for < n > = 41 from the spectra with < n > = 88, 138, 217, 331 (see text). c) Corresponding mass spectra.

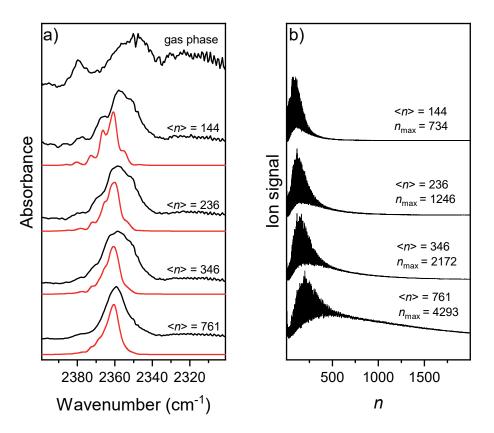


Figure 11: a) Experimental (black) and calculated (red) infrared spectra at ~ 29 K for different concentrations of CO_2 (1, 1.6, 2.3 and 5% from top to bottom). A pure CO_2 gas phase spectrum is shown on top. b) Corresponding mass spectra.

