

How does in situ stress rotate within a fault zone? Insights from explicit modeling of the frictional, fractured rock mass

Working Paper**Author(s):**

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Publication date:

2021

Permanent link:

<https://doi.org/10.3929/ethz-b-000465444>

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Funding acknowledgement:

182150 - In situ stress variations near faults considering fault zone rock rheology - implications for reservoir stimulation and associated seismicity (SNF)

1 **How does in situ stress rotate within a fault zone? Insights from explicit modeling**
2 **of the frictional, fractured rock mass**

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15 **Key Points:**

- 16 • Stress variations in fault zones are explicitly simulated with a multilayer model
17 including macroscopic fracture networks
- 18 • Fracture deformation and specific boundary conditions synergistically
19 contribute to the stress variations and elastic property changes
- 20 • Fracture properties, pore pressure and fracture network affect stress variations
21 by controlling the fracture deformation

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33 **Abstract**

34 We quantitatively investigate the spatial stress variations within fault zones by
35 explicitly incorporating macroscopic fracture networks in a multilayer fault zone model.
36 Based on elastic crack theory, we first derive a unified constitutive relationship for
37 frictional fractures, featuring elastic and plastic shear deformation and shear-induced
38 normal dilatancy. To honor the progressively accumulated damage across a fault zone,
39 we establish a fractured multilayer model including randomly-oriented frictional
40 fractures with varying densities from layer to layer. Under the specific boundary
41 conditions of a fault zone, the global mechanical response of each layer is quantitatively
42 related to the deformation of the interior fractures. Stress variations and effective elastic
43 property changes are systematically studied considering the influences of fracture
44 properties and pore pressure. We show that the major principal stress always rotates
45 toward a limiting angle of 45° with respect to the fault slip direction and that differential
46 stress invariantly decreases with the fracture density. However, mean stress increases
47 for an unfavorably-oriented fault and decreases when the regional major principal stress
48 trends at a small angle ($< 45^\circ$) to the fault slip direction. Accumulated damage also
49 results in a decrease and increase in the effective Young's modulus and Poisson's ratio,
50 respectively. The influences of fracture properties, pore pressure and fracture network
51 can be attributed to their control on the fracture deformation components and relative
52 proportion. Our model can predict continuous variations of stresses and effective elastic
53 properties from intact country rock, through fractured damage zone, to the plastic fault
54 core of a mature fault.

55

56 **1. Introduction**

57 Characterization of the in situ stresses is key to better understand the crustal
58 deformation processes, such as earthquakes (Scholz, 2019) and subsurface engineering
59 (Cornet et al., 2007; Ma and Zoback, 2017). In general, stress field within the intra-
60 plate region is relatively uniform at tectonic scales (Zoback, 1992). However, the
61 ubiquitous discontinuities (e.g., veins, joints, fractures, and faults) at various scales play
62 a crucial role in modifying the local stress fields (Pollard and Segall, 1987). In particular,
63 faults dominate the subsurface processes to great extent due to the jumbo size. They
64 can act as either fluid conduits, advantageous to fluid flow in reservoirs (Zoback et al.,
65 2012), or hazardous seismicity sources (NRC, 2013). Detailed information on the in
66 situ stress conditions around faults is thus essential to relevant scientific and industrial
67 activities.

68 The state of stress is often not adequately determined in the vicinity of faults
69 due to the complexity of the stress conditions and limited measures for stress
70 measurements (Stephansson and Zang, 2012). In general, stress fields at great depth can
71 be only inferred from focal mechanism inversions (Michael, 1984; Vavryčuk, 2014)
72 while from borehole/drillcore measurements at shallow depth (Sjöberg et al., 1997;
73 Haimson and Cornet, 2003; Pierdominici and Heidbach, 2012; Funato and Ito, 2017).

74 These methods have provided ample field evidence that indicates significantly different
75 regional far-field stresses from those near tectonic faults (Zoback et al., 1987; Lin et al.,
76 2010) and reservoir-scale faults (Obara and Sugawara, 2003; Yale, 2003; Tamagawa
77 and Pollard, 2008). For example, focal mechanism inversions of earthquake swarms
78 near San Andreas Fault (SAF) indicate that the major principal stress ($S_1 = S_{Hmax}$) rotates
79 generally from $\sim 90^\circ$ at far-field to a lower angle within the fault zones (Hardebeck and
80 Hauksson, 1999; Provost and Houston, 2001), as shown in Figure 1. The exact reasons
81 for such stress rotation are complicated. However, it is likely the result of a self-
82 adjustment of the stress field, depending on the fault structure, rock rheology and pore
83 pressure, as the fault is approached (Zoback, 2010; Faulkner et al., 2010; Stephansson
84 and Zang, 2012).

85 A mature fault in the Earth's upper crust consists of a fault core and a
86 surrounding fracture damage zone (Chester et al., 1993; Caine et al., 1996; Mitchell and
87 Faulkner, 2009). The fault core is composed by highly comminuted rocks that
88 accommodates most of the cumulative fault slip, whereas the damage zone manifests a
89 decrease in fracture density with distance from the fault core without or with only slight
90 displacement (Faulkner et al., 2003). As approach the interior of a fault, the cumulative
91 damage becomes more pronounced, generally manifesting changing elastic properties.
92 In Table 1, it is found that Young's modulus decreases from the host rock, through
93 damage zone, to fault core, while Poisson's ratio is on the contrary. Based on such
94 characterization, a multilayer model has been proposed to predict stress variations in a
95 strike-slip fault damage zone (Faulkner et al., 2006). In this model, stress rotations are
96 chiefly attributed to the elastic property changes as originally suggested by Casey
97 (1980); but quantitatively related to the gradually increasing microcrack density as
98 getting closer to the fault core. Therefore, cyclic measurements in laboratory (Faulkner
99 et al., 2006; Heap et al., 2010) or crack theory (Healy, 2008) could be utilized to predict
100 stress rotations resulting from accumulating microcrack damage.

101 The multilayer model has been mainly applied to the strike-slip faults oriented at high
102 angles to the far-field S_{Hmax} (Faulkner et al., 2006). It predicts a rotation of S_{Hmax} from
103 a large angle ($\sim 80^\circ$), with respect to the fault strike, to $\sim 40^\circ$ within fault zones, which
104 seems perfectly consistent with the stress rotations associated with the SAF (Figure 1).
105 On the other hand, it also predicts a continuously decreasing angle between S_{Hmax} and
106 fault slip direction from a value less than 45° , together with increasing mean stress
107 towards the fault core. In recent examples, two such fault zones at reservoir-scale have
108 been identified at the Grimsel Test Site (GTS, Krietsch et al., 2018) and Bedretto
109 Underground Laboratory for Geoennergies (BULG, van Limborgh, 2020), respectively,
110 both of which show completely opposite trends of stress variations compared with
111 previous predictions. For example, the subvertical fault zone at the GTS is oriented at
112 $\sim 15^\circ$ with respect to the far-field S_{Hmax} (Figure 1). A series of elaborate stress
113 measurements further unravel an increase in this angle up to $\sim 45^\circ$ near the fault plane,
114 as well as significant magnitude drops in both horizontal stresses. Therefore, the
115 multilayer model entails reexamination and further development to tackle the issues of

116 stress variations near faults.

117 To this end, the goal of this study is to improve the understanding and prediction
118 capability of stress variations around faults oriented at different angles with respect to
119 S_1 . With the multilayer model, we particularly focus on the description of individual
120 layers by discrete fracture networks in terms of macrofractures, rather than microcracks.
121 In addition, we explicitly incorporate the elastic and frictional properties into fractures
122 and quantitatively relate their deformation to stress variations, as well as effective
123 elastic properties. This paper is organized as follows. We first propose a unified
124 constitutive relationship for frictional fracture under both loading and unloading
125 conditions. Then we calculate the deformation of a group of fractal fractures embedded
126 in each layer under specific boundary conditions, and relate it to the corresponding
127 effective elastic properties and stress changes. In particular, we investigate the effect of
128 fracture density, fracture stiffness, fracture friction, and pore pressure on the effective
129 elastic properties and stress variations. Finally, we discuss the assumptions of the model,
130 the stress rotation limit predicted by the classic multilayer model, and provide some
131 implications for the spatiotemporal variations of stress within fault zone.

132

133 **2 Constitutive Behavior of Frictional Fractures**

134 In this section, the mechanical behavior of frictional fractures under plane strain
135 condition (Zhang and Ma, 2020) is extended to include elastic deformation. In particular,
136 complete constitutive relationship for frictional fracture is derived considering loading
137 and unloading conditions, respectively, used to calculate the stress changes inside the
138 multilayer model induced by fracture deformation in Section 3.

139 **2.1 Stress-Displacement Relationship for Fractures under Loading Condition**

140 We consider an elastic body in a state of plane strain with only in-plane
141 displacements for the embedded fracture, shown by its cross-section in Figure 2a. The
142 planar fracture has a normal unit vector \mathbf{n} in the x_n coordinate direction, negligible
143 thickness, and a length of l . The surrounding elastic matrix is linear, homogeneous, and
144 isotropic with Poisson's ratio ν and shear modulus G . Under remote (effective) normal
145 and shear stresses (σ_n and τ), the relative normal and shear displacements (u_n and u_s)
146 between its opposite sides can be quantified by the following theoretical derivations.

147 If the normal stress is compressive ($\sigma_n > 0$), the relative normal displacement is
148 given as:

$$149 \quad u_n = \sigma_n / k_n \quad (1)$$

150 where k_n is the normal stiffness of the fracture walls. When the fracture contains high
151 pore pressure, the resultant normal stress σ_n acting on the fracture wall can be tensional
152 ($\sigma_n < 0$). In this case, pure mode I deformation can be well quantified by elastic crack
153 theory (Pollard and Segall, 1987), which gives the relative normal displacement as:

$$154 \quad u_n = \sigma_n / k_m \quad (2)$$

155 with the matrix resistance to the opening of fracture walls k_m given by:

156
$$k_m = \frac{G}{2(1-\nu)} (\delta^2 - x_s^2)^{-0.5} \quad (3)$$

157 where δ is the half-length of the fracture and the local coordinate $x_s \in [-\delta, \delta]$.

158 Obviously, the matrix resistance k_m varies from fracture to fracture and changes
 159 along the fracture wall. The average matrix resistance for a specific fracture can be
 160 further obtained by integrating Eq. (3) across the whole fracture length:

161
$$\bar{k}_m = \frac{1}{2\delta} \int_{-\delta}^{\delta} \frac{G}{2(1-\nu)} (\delta^2 - x_s^2)^{-0.5} dx_s = \frac{2G}{\delta\pi(1-\nu)} \quad (4)$$

162 Therefore, Eq. (2) can be written as:

163
$$u_n = \sigma_n / \bar{k}_m \quad (5)$$

164 The relationships between normal stress and normal displacement in Eq. (1) and Eq. (5)
 165 are represented in Figure 2b.

166 On the other hand, shear deformation of a fracture is usually believed to be
 167 driven by the stress difference between the remote shear stress τ and the shear stress on
 168 the fracture τ_f (Pollard and Segall, 1987). In this paper, we extend the shear behavior of
 169 fractures by including the elastic shear deformation before the fracture reaches the
 170 frictional sliding. Specifically, when the shear stress on fracture τ_f is less than the
 171 frictional strength $\tau^\mu (= \mu\sigma_n)$, fracture is in the elastic stage, where the relative shear
 172 displacement is:

173
$$u_s = \tau_f / k_s \quad (6)$$

174 where k_s is the fracture shear stiffness, which is assumed to be constant over the whole
 175 fracture plane. Simultaneously, the elastic matrix also experiences the same shear
 176 deformation, leading to the matrix shear stress τ_m :

177
$$\tau_m = \bar{k}_m \cdot u_s \quad (7)$$

178 Considering the concept of shear stress partition (Davy et al., 2018), the remote
 179 shear stress τ can be expressed as the sum of fracture shear stress τ_f and matrix shear
 180 stress τ_m :

181
$$\tau = \tau_f + \tau_m \quad (8)$$

182 By substituting τ_f and τ_m in Eq. (6) and Eq. (7), we further obtain:

183
$$u_s = \frac{\tau}{k_s + \bar{k}_m} \quad (9)$$

184 If τ_f reaches the frictional strength $\tau^\mu (= \mu\sigma_n)$, frictional sliding occurs and the shear
 185 motion is driven by the shear stress difference. Based on elastic crack theory (Pollard
 186 and Segall, 1987), the shear displacement is given as:

187
$$u_s = \frac{\tau - \tau^\mu}{\bar{k}_m} = \frac{\tau - \mu\sigma_n}{\bar{k}_m} \quad (10)$$

188 In Figure 2c, the shear stress - shear displacement law defined jointly by Eq. (9) and
 189 Eq. (10) is shown. In a straightforward way, we propose the following criterion to
 190 estimate whether fracture is in the elastic or the plastic stage:

191
$$\begin{cases} \tau < \tau^\mu \cdot \frac{\bar{k}_m + k_s}{k_s}, & \text{elastic} \\ \tau \geq \tau^\mu \cdot \frac{\bar{k}_m + k_s}{k_s}, & \text{plastic} \end{cases} \quad (11)$$

192 To reflect shear-induced dilatancy commonly observed in the brittle rock mass,
 193 we further utilize dilatancy factor β to relate the normal dilational displacement to the
 194 plastic shear displacement when frictional sliding occurs. The relative normal
 195 displacement defined in Eq. (1) can be modified as:

196
$$u_n = \frac{\sigma_n}{k_n} - \beta \cdot (u_s - \tau^\mu / k_s) \quad (12)$$

197 which further gives the resultant displacement vector:

198
$$\mathbf{u} = -u_n \mathbf{n} + u_s \mathbf{s} \quad (13)$$

199 It should be noted that the normal stiffness k_n for natural fractures is generally much
 200 larger than the shear stiffness k_s . Therefore, we can neglect the compressive normal
 201 displacement for sake of computational efficiency without much loss of accuracy,
 202 which has been numerically verified by Davy et al. (2018).

203 2.2 Stress-Displacement Relationship for Fractures under Unloading Condition

204 Unloading occurs on a fracture due to the decrease of remote shear ($\Delta\tau$) or
 205 normal ($\Delta\sigma_n$) stress. For a fracture in the elastic stage, the corresponding decrease of
 206 shear stress on the fracture $\Delta\tau_f$ is:

207
$$\Delta\tau_f = \frac{\Delta\tau}{k_s + \bar{k}_m} k_s \quad (14)$$

208 For a fracture in the plastic stage, however, two scenarios can be encountered during
 209 the unloading process: (1) The unloaded fracture is still in the plastic stage. The shear
 210 stress change on the fracture $\Delta\tau_f$ is:

211
$$\Delta\tau_f = \mu \Delta\sigma_n \quad (15)$$

212 (2) The unloaded fracture returns to the elastic stage. The shear stress decrease on the
 213 fracture $\Delta\tau_f$ now has a different expression:

214
$$\Delta\tau_f = \mu \sigma_n - \frac{\tau - \Delta\tau}{k_s + \bar{k}_m} k_s \quad (16)$$

215 It is hypothesized that the unloading shear stiffness is the same as the loading
 216 stiffness, as shown in Figure 2c. The shear stress decrease on the fracture defined from
 217 Eq. (14) to Eq. (16) can be adopted to calculate the recovered elastic shear displacement
 218 Δu_s during unloading:

219
$$\Delta u_s = \Delta\tau_f / k_s \quad (17)$$

220 With regard to the normal displacement, it is often assumed that the normal dilational
 221 component is plastic and irreversible. The recovered elastic normal displacement Δu_n
 222 is expressed by:

223
$$\Delta u_n = \Delta\sigma_n / k_n \quad (18)$$

224

225 3 Effective Properties of Fractured Rock Mass within Fault Damage Zone

226 We first briefly review the basic assumptions and boundary conditions of the
227 multilayer model for fault damage zone (Faulkner et al., 2006). For each layer of the
228 model, we then calculate the displacements and strains of individual fractures according
229 to the fracture constitutive relationship, and relate them to the boundary strain response
230 using effective medium theory. Due to the specific boundary conditions, we further
231 propose a new method to update the stress field of each layer to accommodate the
232 incremental strain component induced by fractures. In this way, it is able to obtain the
233 final stress field and effective elastic properties of each layer.

234 3.1 Boundary Conditions of a Fault Damage Zone

235 Both Casey's model (1980) and its extended version, i.e., multilayer model
236 (Faulkner et al., 2006), suggest that the damage zone is subject to constant strain along
237 the slip direction and to constant stress in the off-fault direction. In Figure 3a, the
238 conceptual multilayer model for a strike-slip fault zone is shown schematically as an
239 example. Given far-field stresses, stress components for the outmost intact rock can be
240 resolved based on Mohr diagram, as shown in Figure 3b. For these consecutive layers,
241 normal and shear stresses (S_{xx} and S_{xy}) acting on the interfaces are constant for
242 mechanical continuity, while constant strain ε_{yy} is applied in the fault slip direction
243 assuming no slip between layers. Such boundary conditions also apply to dip-slip faults
244 featuring a fault plane parallel to the intermediate principal stress.

245 Specifically, we set the outmost layer representing intact rock as a benchmark,
246 which gives the following far-field stress components:

$$247 \quad S_{xx} = \frac{S_1 + S_3}{2} - \frac{S_1 - S_3}{2} \cos 2\theta \quad (19)$$

$$248 \quad S_{yy} = \frac{S_1 + S_3}{2} + \frac{S_1 - S_3}{2} \cos 2\theta \quad (20)$$

$$249 \quad S_{xy} = \frac{S_1 - S_3}{2} \sin 2\theta \quad (21)$$

250 where S_1 and S_3 are the far-field maximum and minimum principal stresses, respectively,
251 θ is the angle between the fault slip direction and S_1 . In the following, effective stresses
252 ($\sigma_{xx} = S_{xx} - P_p$, $\sigma_{yy} = S_{yy} - P_p$, with pore pressure P_p subtracted from the total stresses) are
253 used for calculation.

254 3.2 Updating the Stress Component on the Strain Boundary

255 When the model is subject to given external stresses, the mechanical behavior
256 of each layer depends jointly on the elastic matrix and fracture deformation. In other
257 words, the local deformation of individual fractures contributes to the total strain of the
258 model. In Appendix A, we provide the derivations quantifying the fracture contribution
259 (Eq. (A3)) to model's global strain based on effective medium theory. Note that the
260 strain ε_{yy} in the fault slip direction is maintained as constant across all layers (Figure
261 3a). Therefore, the additional strain in the y-direction contributed by fractures entails

262 the adjustment of strain in the elastic matrix. Equivalently, σ_{yy} should be modified to
263 accommodate the strain increments (Zhang and Ma, 2020). Specifically, bisection
264 method (see Appendix B) is used to search for the stress change in σ_{yy} , which gives an
265 updated state of stress of each layer.

266 In Figure 4, we graphically present how the stress state evolves after updating
267 in the scenarios of low θ ($< 45^\circ$) and large θ ($> 45^\circ$), respectively. Note that, all layers
268 in the multilayer model are initially subject to the same boundary conditions as the
269 outmost purely elastic layer. Therefore, the far-field stress/strain conditions are actually
270 the initial conditions for each layer. In Figure 4a, the resolved σ_{yy} is initially larger than
271 σ_{xx} so that fracture deformation induces compressive strain in the y -direction. Because
272 of the constant strain boundary in the y -direction, however, σ_{yy} must decline (to σ'_{yy})
273 to decrease the corresponding strain component in the elastic matrix, accommodating
274 the fracture contribution. As a result, it leads to an increase in θ (to θ'). By contrast,
275 when the resolved σ_{yy} is smaller than σ_{xx} due to a high θ in the latter case, σ_{yy} increases
276 (to σ'_{yy}) and thus θ decreases (to θ'). The boundary conditions require that the shear
277 stresses between layers are continuously equal and maintained constant, which restrict
278 the stress paths associated with y -direction to horizontal lines, as shown by the dashed
279 arrows in Figure 4a and 4b. Moreover, it is worth noting that only the limiting condition
280 that $\sigma_{yy} = \sigma_{xx}$ (zero differential stress) is allowed according to the minimum energy
281 principle, which corresponds to plasticity with Poisson's ratio of 0.5 and Young's
282 modulus of 0. Therefore, the maximum principal stress in either scenario always rotates
283 towards the angle of 45° with respect to the fault slip direction.

284

285 4. Model Experimentation and Results

286 In this section, six sets of representative rock mass volumes are generated with
287 different discrete fracture network densities to characterize different positions within a
288 fault zone. Based on the aforementioned methods, the influences of fracture shear
289 stiffness k_s , fracture frictional coefficient μ , pore pressure P_p , and the far-field angle θ
290 are systematically investigated.

291 4.1 Generation of Discrete Fracture Networks

292 Field observations indicate that fault damage zones often exhibit a broad range
293 of fracture lengths that can be quantified by a power law (Odling et al., 2004;
294 Ostermeijer et al., 2020). Utilizing the classic double power law (Davy et al., 1990;
295 Bonnet et al., 2001), it is able to describe the density fracture length distribution as:

$$296 \quad n(l, L) = \alpha L^D l^{-a}, \quad l \in [l_{min}, l_{max}] \quad (22)$$

297 in which $n(l, L)dl$ is the number of fractures whose length is in the range $[l, l + dl]$ in a
298 representative volume with side length L , α is the density-related term, D is the fractal
299 dimension, and a is the power law length exponent. Numerous 2D outcrop datasets
300 suggest that D falls in the range of 1.3~2 and a varies between 1.3 and 3.5 (Renshaw,
301 1999; Bonnet et al., 2001). In particular, when $a = D + 1$, the fracture network is self-
302 similar and its connectivity is scale invariant (Bour et al., 2002; Darcel et al., 2003).

303 Due to the complexity of fracture network related to fault damage zone and the
 304 limitation of field characterization, there is no generally agreed rule for the distributions
 305 of fracture length and orientation within fault damage zone (Wilson et al., 2003; Healy,
 306 2008; Ostermeijer et al., 2020). In this study, we set $D = 2$ and $a = 3$ to generate six sets
 307 of representative rock mass volumes with scale-independent discrete fracture networks.
 308 For each set, the minimum length of fractures is set to $0.01L$ for normalization. Uniform
 309 distributions of fracture centers and orientation are assigned since fracture clustering
 310 and interaction are not considered here for simplicity. The density term α is set to 4, 3.2,
 311 2.4, 1.6, 0.8, and 0.32, respectively, for each set to achieve decreasing fracture density.
 312 With these parameters, ten realizations are generated for each layer with specific
 313 fracture density, using the multiplicative cascade process (Darcel et al., 2003; Kim,
 314 2007; Moein et al., 2019). In Figure 5, we further show the fractal analysis of the ten
 315 realizations of each layer, where the cumulative number $N(l)$ of fractures with length
 316 greater than l is well captured by the integrated form of Eq. (22):

$$317 \quad \log N(>l/L) = \log\left(\frac{\alpha}{a-1} L^{D-(a-1)}\right) - (a-1)\log(l/L) \quad (23)$$

318 in which fracture length is normalized by the model size. The constant $(a-1)$ of the
 319 second right-hand term represents a fractal dimension of the length distribution.

320 For all fractures, the normal stiffness is set to 12,000 GPa/m, which is several
 321 hundreds of times larger than the shear stiffness, as will be shown in the following
 322 section, and the dilatancy factor β is set to 0.05, corresponding to a constant dilation
 323 angle of 2.86° . Initially, all layers will be loaded instantaneously under the same stress
 324 level ($S_1 = 150$ MPa, $S_3 = 75$ MPa, $P_p = 40$ MPa, corresponding to a depth of ~ 4 km).
 325 Such a state of stress follows that the far-field crust is critically stressed with hydrostatic
 326 pore pressure (Zoback and Townend, 2001). A purely elastic layer without any fractures
 327 is set as reference to emphasize the effect of fracture density in the following analysis.

328 4.2 Effect of Fracture Shear Stiffness on Stress Variations

329 The large normal stiffness precludes remarkable contribution of the normal
 330 fracture deformation. Thus, we first explore the effect of fracture shear stiffness ($k_s =$
 331 10, 20, 30 GPa/m) on stress variations with increasing fracture density, while keep the
 332 μ and P_p constant at 0.6 and 40 MPa, respectively. Figure 6a summarizes the stress
 333 rotations in four series of simulations in which $\theta = 10^\circ, 30^\circ, 60^\circ$ and 80° , respectively.
 334 For all cases, S_1 constantly rotates to the angle of 45° with the increase of fracture
 335 density. As k_s increases, θ' departs further from 45° . Apparently, the increase of k_s
 336 impedes the stress rotation. In general, the increase of fracture density brings higher
 337 uncertainty in our simulations. For constant fracture density, the uncertainty becomes
 338 more substantial when θ is closer to 45° . This is because the stress state is more
 339 symmetric when it is near the pure shear state ($\theta = 45^\circ$), implying that fractures of any
 340 orientations can deform preferentially.

341 To better show the stress variations, the mean values of principal stresses, for k_s
 342 $= 20$ GPa/m, are illustrated in Figure 6b as Mohr circles. It can be seen that the Mohr

343 circles display distinct changes from case to case. For the case of $\theta = 10^\circ$, the stress
344 variations manifest themselves a series of contracting Mohr circles, moving leftwards.
345 In other words, both the mean stress and differential stress decrease with the increase
346 of fracture density. As we assume frictional equilibrium at far-field, the local stress
347 states in the fault zone suggest a more stable fault as we normally expect. To activate
348 such a stable fault, a higher pore pressure or a lower frictional strength or a combination
349 of both are needed. Note that this observation is completely opposite to what is
350 predicted by conventional multilayer model (Faulkner et al., 2006) but consistent with
351 the original Casey's model (Casey, 1980). As for another end-member ($\theta = 80^\circ$), Mohr
352 circle also contracts with the fracture density but moves to a high stress level, indicating
353 reduced differential stress and increasing mean stress as the inner fault is progressively
354 approached. The scenario with high value of θ has been widely studied. The results here
355 are well consistent with previous studies (Faulkner et al., 2006; Healy, 2008; Heap et
356 al., 2010), which can provide static weakening mechanisms by invoking high pore
357 pressure and low friction strength for such unfavorably-oriented active faults.

358 In addition, as quantified in Figure 6a, the middle two cases show a pure shear
359 state for high fracture densities. Unlike the conventional multilayer model, the self-
360 regulated process in our model does not allow S_1 to rotate past 45° . Therefore, S_1 is able
361 to rotate at most to 45° . In this circumstance, the innermost layer corresponds to a
362 plastic rheology as postulated by Coulomb plasticity (Byerlee and Savage, 1992;
363 Lockner and Byerlee, 1993) or by material softening (Rice, 1992). Therefore, our model
364 is able to combine the brittle fault zone, as the conventional multilayer mode, and soft
365 gouge layer. All of cases, the local S_3 has a minimum when $\theta = 30^\circ$ for a constant
366 fracture density and the local S_1 has a maximum when $\theta = 60^\circ$. In particular, faults that
367 are oriented at around 30° to S_1 are believed to be critical according to Coulomb failure
368 theory together with laboratory-derived frictional coefficient (Byerlee, 1978). The
369 results of $\theta = 30^\circ$ case showing that every layer of the model is under a state of failure
370 could demonstrate the criticality but still need to be corroborated by more field evidence.
371 If it is the case in field, we would argue that stress variations may also occur in this
372 critical condition.

373 **4.3 Effect of Fracture Frictional Coefficient on Stress Variations**

374 We further examine the effect of fracture frictional coefficient μ in this section.
375 For all cases, k_s and P_p are set as 20 GPa/m and 40 MPa, respectively. The resultant
376 stress rotations are shown in Figure 7. It can be seen that the decrease of μ from 0.6 to
377 0.4 has no significant effect on the stress rotation for the same fracture density, while a
378 further reduction to 0.2 causes dramatic rotation especially at high fracture density
379 levels. At $\theta = 30^\circ$ and 60° , the decline of μ is relatively less influential. We note that,
380 of all cases, S_1 in the case of $\theta = 60^\circ$ first rotates to $\theta = 45^\circ$ (when normalized fracture
381 density is 0.8), suggesting that the model is prone to plasticity in this configuration.
382 Therefore, a further increase in fracture density does not promote stronger rotation of
383 S_1 . In contrast, the case of $\theta = 30^\circ$ exhibits a nearly plastic rheology in the innermost

384 layer. Furthermore, remarkable μ effect can be found in the two end-members, which
385 display drastic changes, as well as uncertainties, when $\mu = 0.2$.

386 In a different manner from Mohr diagrams, the mean stress and differential
387 stress are plotted versus the fracture density and μ in Figure 8. Similar to Figure 6b, it
388 is clearly seen from Figure 8a-d that the decline of differential stress is monotonic with
389 fracture density in all cases. That is said, fracture deformation always consumes the
390 strain energy of the model, causing differential stress relaxation. When $\theta = 45^\circ$ no
391 fracture deforms due to the equality of σ_{yy} and σ_{xx} , the principal stresses remain
392 unchanged with fracture density. When $\theta < 45^\circ$, the mean stress becomes less
393 compressive with increasing fracture density, and it is more compressive when $\theta > 45^\circ$
394 (Figure 8e-h). As a result, the principal stresses would rotate to be at 45° to the fault
395 slip direction for all values of θ , except for 0° and 90° in which differential stress still
396 relaxes but without stress rotations, i.e., contracting Mohr circles with one end fixed
397 (e.g., Zhang and Ma, 2020). These results are in excellent consistency with those
398 predicted by Casey's model (Casey, 1980) but with physics-based mechanisms.

399 **4.4 Effect of Local Pore Pressure on Stress Variations**

400 Besides the foregoing two factors, pore pressure effect is investigated by
401 performing numerical tests with different pore pressure (40, 50, 60 MPa), while k_s and
402 μ are set as 20 GPa/m and 0.6, respectively. Figure 9 shows that elevated pore pressure
403 has trivial effect on the stress variations in our simulations. Since the fracture density
404 has larger effect, the pore pressure effect is actually masked by the fracture density.

405 The negligible pore pressure effect in this series of simulations can be accounted
406 for by the fracture constitutive behavior. As pointed out by Davy et al. (2018), the
407 mechanical behavior of the fracture network is mainly controlled by the stiffness length
408 l_s , which is defined as the fracture length for which the fracture shear stiffness equals
409 to the average shear stiffness of matrix ($k_s = \bar{k}_m$):

$$410 \quad l_s = \frac{4G}{\pi(1-\nu)k_s} \quad (24)$$

411 which is $0.141L$ for the simulations in this section. For fractures much shorter than l_s ,
412 frictional resistance is dominated by the matrix as \bar{k}_m is much larger than k_s . For
413 fractures much longer than l_s , the plastic limit in Eq. (11) can be simplified as $\tau^u (= \mu\sigma_n)$
414 since $k_s \gg \bar{k}_m$. As seen from Figure 5, only a small fraction of fractures are longer than
415 l_s in this simulations. Therefore, the increase in pore pressure only makes the few long
416 fractures slip frictionally while the remaining vast number of short fractures are
417 completely unaffected. Equivalently, the increased pore pressure only contributes to
418 subtle increase of plastic shear deformation in our simulations, even at a high fracture
419 density level (we expand this argument in Section 4.5). It is thus expected to obtain
420 more significant pore pressure influence with a larger fractal dimension a or in a weaker
421 model.

422 It is worth noting that, the constitutive relationship of fracture we develop here
423 aims for brittle deformation of damage zone. For mature fault core, weak and

424 interconnected foliated microstructures, such as phyllosilicate foliae, might be
425 pervasive (Collettini et al., 2019). Frictional sliding along fault-parallel fabric can be
426 simply described by Coulomb criterion and Eq. (10), so that enormous effect of elevated
427 pore pressure (especially overpressure) can be expected on stress rotations therein.
428 Furthermore, Healy (2008) argued that, the deviatoric effect of pore pressure could
429 exert an important influence on stress rotations when considering microcrack-related
430 anisotropy, which, however, is beyond the scope of this study since fractures are
431 randomly oriented.

432 **4.5. Influences of Fracture Deformation on the Effective Elastic Properties**

433 Our simulations show that the local stress state can be considerably modified,
434 to different extent, by fracture network properties in various scenarios. Since all
435 influence factors in previous sections essentially change the magnitudes of fracture
436 deformation (i.e., global strain increments), we further investigate the influences of
437 fracture deformation on the effective elastic properties. For each layer, we calculate its
438 effective elastic properties by solving Hooke's law, i.e., Eq. (A5), but with the final
439 global stress and strain. In Figure 10, effective elastic properties are plotted against the
440 fracture-contributed strain in the fault slip (y) direction based on all foregoing numerical
441 tests. We also provide the changes of effective elastic properties with fracture density
442 of individual cases in Supporting Information. It can be seen that fracture deformation
443 induces compression in the y -direction when θ is less than 45° while dilatancy emerges
444 when θ is larger than 45° , which result in a decrease and increase in σ_{yy} , respectively,
445 due to constant strain boundary as illustrated in Figure 4.

446 In general, fracture deformation (and the resultant strain increment in y -
447 direction) increases with the fracture density, which leads to increasing Poisson's ratio
448 and decreasing Young's modulus, as often observed in many fault zones (Table 1). We
449 would argue that, the stress variations and modifications of the effective elastic
450 properties are accompanying each other as approach the fault core. Both effective elastic
451 parameters show nonlinear dependence on the fracture-related strain. The nonlinearity
452 becomes more prominent when the fracture density gets higher. The data clusters at low
453 fracture densities (i.e., normalized fracture density of 0, 0.08 and 0.2) indicate that the
454 relative changes in both effective elastic parameters are dramatic. When the fracture
455 density goes higher, the relative changes gradually mitigate but with higher uncertainty.
456 For the same fracture density, in addition, more fracture deformation is induced when
457 θ deviates further away from 45° , which requires larger stress adjustment to maintain
458 the constant strain in the y -direction. When θ is closer to 45° , both effective elastic
459 properties are more sensitive to the fracture deformation. In other words, small amount
460 of fracture deformation results in significant changes of effective elastic properties.
461 Therefore, it also accounts for why it is much easier for the two middle cases ($\theta = 30^\circ$
462 and 60°) to reach a plastic state.

463 Other than fracture density, we further consider the individual influences of
464 other factors. According to the constitutive relationship of fracture, we divide the

465 fracture deformation into two parts: elastic and plastic deformation. Therefore, it is able
466 to quantify the dependence of each type of deformation on fracture shear stiffness,
467 frictional coefficient and pore pressure. In Figure 11, the total strain increment and the
468 plastic component in y -direction, induced by fracture deformation, are plotted as
469 functions of fracture density and each influence factor in the case of $\theta = 10^\circ$. As with
470 Figure 10, the total strain increment constantly increases with fracture density.
471 Regarding each fracture density level, the variation of each influence factor induces
472 different degrees of deformation. Figure 11a illustrates the very control of k_s on the
473 elastic fracture deformation, since all fractures are in the elastic stage (i.e., no frictional
474 slip occurs) in this series of simulations. As k_s increases from 10 to 30 GPa/m, the
475 elastic fracture deformation decreases correspondingly due to the higher resistance. In
476 Figure 11b, it is found that most of the deformation is elastic when $\mu = 0.6$ and 0.4. For
477 certain fracture densities, slightly larger uncertainty of fracture deformation can be
478 found for $\mu = 0.4$ than 0.6. When μ decreases further to 0.2, both the total and plastic
479 fracture strain increase remarkably. It demonstrates that the low level of μ forces many
480 fractures into frictional sliding. The effect of μ , as well as the uncertainty, becomes
481 more significant for the higher fracture density. This elucidates the observations in
482 Section 4.3 that the local stress states of the inner layers are close to pure shear when μ
483 = 0.2. The effect of μ could also explain why the increasing pore pressure brings about
484 trivial changes in our simulations in Section 4.4, in addition to stiffness length. In this
485 series of simulations, μ is set to 0.6. All of the fractures are well below the individual
486 frictional strength. Even when pore pressure increases up to 60 MPa, which is close to
487 the minimum principal stress (75 MPa), only a small fraction of plastic deformation is
488 induced.

489

490 **5. Discussion**

491 **5.1 Model Assumptions and Validity**

492 Our simulations are performed based on the multilayer model extended from
493 Casey's model (Casey, 1980), which has been previously used to assess the changes in
494 stress state resulting from changes in elastic moduli (Faulkner et al., 2006; Healy, 2008;
495 Heap et al., 2010). Instead of directly applying varying elastic properties to each layer,
496 we explicitly relate the deformation of macroscopic fractures to the global mechanical
497 behavior under the long-term quasi-static loads. We argue that both the stress rotations
498 and accompanying elastic property changes result from the synergistic effect of fracture
499 deformation and boundary constraints. Specifically, this bottom-up approach has the
500 following primary assumptions about fractures: (1) The frictional fractures are
501 preexisting without considering the complex seismic history; (2) These fractures exist
502 at different scales, if not all scales, following power law; (3) Fractures are randomly
503 distributed while the clustering and interaction are not considered.

504 Firstly, the off-fault damage is believed to be produced by earthquake ruptures
505 due to transient loading of the stress waves emitted from rupture tips. Such coseismic

506 damage generally occurs over a relatively short time scale. In the context of long-term
507 mechanical response, therefore, we begin with preexisting fractures in our simulations
508 without considering the complex dynamic mechanisms. Secondly, although there are
509 only few field data on the length distribution of fractures within fault damage zones
510 (e.g., Ostermeijer et al., 2020), fracture length is generally found to follow the power
511 law (Bonnet et al., 2001) for different fracture systems in geological media. In addition,
512 Knott et al. (1996) pointed out that secondary fault throw with fault damage zones can
513 also be characterized by power law, and fault length has a linear relationship with the
514 fault throw (Cowie et al., 1996). Consequently, power law distribution is reasonably
515 hypothesized for fracture length within fault damage zones. It should be noted that, we
516 only use self-similar and scale-invariant fracture network in this study, and the largest
517 fracture length is limited by the model size L . Such model configuration gives trivial
518 pore pressure effect due to the control of stiffness length, as elaborated in Section 4.4.
519 More realistic results are expected by larger exponent. As observed by Mello et al.
520 (2010), finally, the maximum strain rate direction rotates, when an earthquake rupture
521 propagates at the sub-Rayleigh wave speed, from fault-parallel to fault-perpendicular
522 direction. Such a dynamic fracturing pattern could support an isotropic damage model.
523 We are also aware of the asymmetry on either side of a fault (Rice et al., 2005) and the
524 heterogeneity along fault or perpendicular to fault (Wilson et al., 2003; Rempe et al.,
525 2018; Ostermeijer et al., 2020), which, however, are beyond the scope of this study.
526 Nonetheless, incorporating anisotropy induced by different fracture patterns in the
527 multilayer model is trivial in the further study. Furthermore, fracture clustering and
528 interaction may further intensify the stress rotations and elastic moduli weakening.
529 Simulations without fracture clustering and interaction can act as an end-member for
530 the estimation.

531 Regarding the mechanical loading, the far-field stress state is initially applied to
532 all layers, under which the fault-parallel strain of the purely elastic (outmost) layer is
533 set as the benchmark. Based on the specific boundary constraints, elastic moduli and
534 their changes could be significantly different from those computed under stress
535 boundary conditions. For example, a fractured rock mass could be characteristic of a
536 bulk Poisson's ratio well above 0.5 under stress boundary conditions (Min and Jing,
537 2004), which is meaningless in the multilayer model. That is said, direct application of
538 elastic moduli, measured under conventional stress boundary conditions, to the
539 multilayer model could be problematic. We would therefore argue that the boundary
540 constraints should not be ignored when using the multilayer model for fault damage
541 zone. Since fracture deformation dominates the stress states and effective elastic
542 properties, one would expect the stress variations and accompanying material
543 weakening even if the unequal principal stresses are oriented orthogonal to the layering,
544 which is different from previous models.

545 **5.2 Stress Rotation Limit Imposed by the Conventional Multilayer Model**

546 In the conventional multilayer model (Faulkner et al., 2006; Healy, 2008; Heap

547 et al., 2010), S_1 is able to rotate past the limiting angle of 45° . For such applications,
548 the mechanical equilibrium gives the solution to the final σ'_{yy} of each layer as:

549
$$\sigma'_{yy} = \frac{E_{\text{eff}}}{1-\nu_{\text{eff}}^2} \varepsilon_{yy} + \frac{\nu_{\text{eff}}}{1-\nu_{\text{eff}}} \sigma_{xx} \quad (25)$$

550 where E_{eff} and ν_{eff} are effective Young's modulus and Poisson's ratio, respectively, of a
551 specific layer, and the parameters ε_{yy} and σ_{xx} are prescribed as those of purely elastic
552 layer, representing far-field. In our simulations, Eq. (25) also applies due to the same
553 model configuration. In the following, we would like to re-examine this equation and
554 its application to stress variations due to elastic moduli changes.

555 In the context of unfavorably-oriented faults ($\theta > 45^\circ$), σ_{xx} is larger than σ_{yy} but
556 the fixed strain ε_{yy} can be either compressive (positive) or dilatant (negative) according
557 to the far-field stresses and elastic moduli. In previous studies considering microcrack
558 damage effect, the outmost layer usually has a relatively small differential stress and
559 high elastic moduli (derived from laboratory samples). Hence the fixed strain ε_{yy} is
560 mostly compressive (positive). As revealed by the cyclic stressing experiments on
561 different rock types (Heap et al., 2010), the elastic moduli evolution with increasing
562 microcrack damage manifest a decrease in E_{eff} by 11 ~ 32% and a drastic increase in
563 ν_{eff} by 72 ~ 600%. Applying such data to stress variations as the fault core is
564 progressively approached, the coefficients of the two right-hand terms in Eq. (25) both
565 increase with ν_{eff} regardless of the decreasing E_{eff} . This probably leads to a value of σ'_{yy}
566 larger than σ_{xx} , especially when ν_{eff} is close to 0.5, i.e., $\nu_{\text{eff}}/(1-\nu_{\text{eff}}) \approx 1$. Consequently,
567 stress can rotate over the angle of 45° corresponding to a minimum differential stress
568 as implied in Figure 4b, and the differential stress starts to increase. However, the
569 exchange of the principal stress axes and the assumption of isotropic properties are
570 incompatible under this circumstance.

571 The analysis also holds for the case with $\theta < 45^\circ$, which is rarely studied
572 previously. In this case, σ_{yy} is always larger than σ_{xx} and the fixed strain ε_{yy} is thus
573 compressive (positive). Applying the laboratory-derived elastic moduli changes, σ'_{yy}
574 could further increase, showing an increasing mean stress and a decreasing angle θ
575 (Faulkner et al., 2006). Also note that, since the second right-hand term is
576 monotonically increasing with ν_{eff} , σ'_{yy} could decrease to some extent if the first right-
577 hand term decreases more. This trend was originally presented by Casey (1980), who
578 set a lower Young's modulus in the weak zone while maintained the Poisson's ratio
579 constant. More generally, more substantially decreasing Young's modulus can be
580 expected as in this study considering macroscopic fracture contribution. In particular,
581 σ'_{yy} could decrease even to the value of σ_{xx} when $\nu_{\text{eff}} = 0.5$ and $E_{\text{eff}} = 0$ GPa,
582 corresponding to the limit of $\theta = c$. In this case, the layer undergoes volume-preserving
583 plastic flow. The plastic layer is stressed under constant compression σ_{xx} , and a small
584 shear stress τ_{xy} suffices to induce plastic flow, leading to extrusion in the fault slip
585 direction. Thus, the constant strain boundary condition is violated in this limiting case.

586 5.3 Spatial-temporal Variations of Stress Within Fault Zones

587 Our model exhibits its capability to predict continuous variations of local stresses
588 and effective elastic properties from the purely elastic country rock, through fractured
589 damage zone, to the plastic fault core of a fault. For faults that are characteristic of
590 fractured damage zones, fracture density generally decreases as either an exponential
591 (Chester and Logan, 1986; Vermilye and Scholz, 1998; Wilson et al., 2003) or a power
592 (Johri et al., 2014) function of distance away from the fault core, either of which depicts
593 a sharp decrease of fracture density. Despite that the fracture density - distance
594 relationship is not explicitly incorporated, the effect of fracture density revealed by our
595 model indicates that drastic changes in local stresses and effective elastic properties are
596 restricted only to the regions near the fault core. In other words, the weakness of a
597 poorly-oriented fault, tending to be active, mainly lies in the core zone and the adjacent
598 limited damage zone.

599 Essentially, stress variations are controlled jointly by fracture deformation and
600 the peculiar boundary conditions of a fault zone. However, the fracture constitutive
601 behavior in this study is defined as time independent. In fact, the time dependency of
602 fracture deformation could be significant (Scholz, 1968; Brantut et al., 2013), which
603 may further promote stress rotations and weaken the fault strength in a temporal sense.

604 In addition, stress variations and effective elastic property changes in the current
605 model are entirely attributed to the fracture deformation. More pronounced
606 modifications are expected when further energy dissipation mechanisms are introduced
607 in both fractures and matrices. For example, the chemically active fluids in the fault
608 zone are able to change stiff mineral phase constituents into weak mineral phases
609 (Wibberley, 1999; Schleicher et al., 2010; Collettini et al., 2019). Such fluid-assisted
610 reaction-softening could weaken the protoliths (especially fault core) in a long term,
611 e.g., interseismic period, generating time-dependent stress rotations. It is also
612 noteworthy that, some other fluid-assisted mechanisms (e.g., mineral deposition and
613 cementation) are operative that lead to healing of fractures and generate low-
614 permeability barriers (Chester and Logan, 1986; Chester et al., 1993; Faulkner et al.,
615 2006). Hence the trapped fluids can be pressurized and maintained at high pressures,
616 also weakening the fault zone in a time-dependent manner until next earthquake occurs
617 (Sleep and Blanpied, 1992).

618

619 **6. Conclusions**

620 In this paper, we numerically investigate damage-induced changes in stresses
621 and effective elastic properties within a fault zone by explicitly incorporating
622 macroscopic fracture networks in the classic multilayer model. By emphasizing the
623 synergistic effect of the specific boundary conditions and fracture deformation, it is
624 found that stress variations, as well as effective elastic property changes, within a fault
625 zone are the common products of a self-adjusted process.

626 Frictional fractures are considered under plane strain condition, featuring elastic
627 and plastic shear deformation and dilatancy in the normal direction. Based on the

628 unified fracture constitutive relationship, a systematic parametric study is conducted to
629 understand the effect of fracture properties (density, shear stiffness, friction) and pore
630 pressure on stress variations. It is found that both the increase of fracture density and
631 pore pressure and the decrease of fracture shear stiffness and friction promote the stress
632 variations to different extents. On one hand, the damage-induced stress variations
633 manifest themselves as principal stress rotations and magnitude changes. The
634 simulation results reveal that the major principal stress always rotates toward the angle
635 of 45°, accompanied by gradually decreasing differential stress. However, the change
636 of mean stress depends closely on the fault setting. The mean stress shows an increasing
637 trend with damage degree when the far-field major principal stress is oriented at an
638 angle larger than 45° with respect to the fault slip direction, which on the contrary
639 decreases when the angle is less than 45°. On the other hand, we also show that stress
640 variations and effective elastic property changes accompany each other. As damage is
641 accumulated, the effective Young's modulus continues decreasing while the effective
642 Poisson's ratio increases.

643 The degrees of stress variations and changes in effective elastic properties are
644 essentially proportional to the deformation of fracture network. It is demonstrated that
645 fracture properties and pore pressure, even the fracture network property itself, are able
646 to alter the elastic and plastic components of fracture deformation to different extents.
647 Under the specific boundary conditions, these factors show remarkably different
648 influences and uncertainties.

649 It is also worth emphasizing that we correlate a limiting condition with the
650 plastic rheology wherein pure shear emerges. Therefore, a limiting angle of 45° is
651 attained for the major principal stress rotation, and the effective Young's modulus and
652 Poisson's ratio reach to their limiting values, i.e., 0 and 0.5, respectively. In other words,
653 our model is able to predict continuous variations of local stresses and effective elastic
654 properties from the purely elastic country rock, through fractured damage zone, to the
655 plastic fault core of a mature fault. In addition, this model applies not only to strike-slip
656 faults but also to dip-slip faults with fault plane parallel to the regional intermediate
657 principal stress. the results of this study have important implications for estimating the
658 state of stress and effective elastic moduli within a fault zone, especially when no focal
659 mechanisms or direct stress measurements are available.

660

661 **Appendix A Relation of Local Fracture Deformation and Global Strain**

662 Instead of directly applying the varying elastic properties to different layers, we
663 initially assign the resolved stress tensor $\boldsymbol{\sigma}$ of the outmost layer to all layers of the
664 multilayer model. For one inner layer with certain fracture density, the remote normal
665 and shear stresses (σ_n and τ) for a fracture with normal unit vector \mathbf{n} can be related to
666 the boundary stress tensor $\boldsymbol{\sigma}$ by:

$$667 \quad \sigma_n = \mathbf{n}^T \cdot \boldsymbol{\sigma} \cdot \mathbf{n} \quad (\text{A1})$$

$$668 \quad \tau = \mathbf{n}^T \cdot \boldsymbol{\sigma} \cdot \mathbf{s} \quad (\text{A2})$$

669 in which P_p is the pore pressure and the in-plane shear unit vector \mathbf{s} defined in Figure

670 2a is adopted when the relative shear motion is right lateral, otherwise the opposite
671 direction is used.

672 Based on the stress-displacement law, we can calculate the displacement vector
673 \mathbf{u} of the fracture, which is further quantitatively related to the global strain at the model
674 boundary according to effective medium theory (Kachanov, 1992):

$$675 \quad \Delta \boldsymbol{\varepsilon} = \frac{a}{A} (\mathbf{u} \otimes \mathbf{n} + \mathbf{n} \otimes \mathbf{u}) \quad (\text{A3})$$

676 with A the cross-section area of the rock mass volume. Considering all fractures in the
677 rock mass volume, the total global strain can be obtained by summing the elastic matrix
678 strain and the additional strain contributed by fractures:

$$679 \quad \boldsymbol{\varepsilon}_{\text{tot}} = \boldsymbol{\varepsilon}^m + \sum_i \frac{a_i}{A} (\mathbf{u}_i \otimes \mathbf{n}_i + \mathbf{n}_i \otimes \mathbf{u}_i) \quad (\text{A4})$$

680 where the subscript i of the second right-hand term denotes the i th fracture under
681 consideration, and $\boldsymbol{\varepsilon}^m$ is the elastic matrix strain given by Hooke's law under plane
682 strain:

$$683 \quad \boldsymbol{\varepsilon}^m = \begin{bmatrix} \varepsilon_{xx}^m \\ \varepsilon_{yy}^m \\ \varepsilon_{xy}^m \end{bmatrix} = \frac{1-\nu}{2G} \begin{bmatrix} 1 & -\nu/(1-\nu) & 0 \\ -\nu/(1-\nu) & 1 & 0 \\ 0 & 0 & 1/(1-\nu) \end{bmatrix} \begin{bmatrix} \sigma_{xx} \\ \sigma_{yy} \\ \sigma_{xy} \end{bmatrix} \quad (\text{A5})$$

684 with the superscript 'm' representing the purely elastic (intact) matrix.

685 As indicated by Eq. (9) and Eq. (10), the shear displacement of any fracture is
686 a function of the average matrix resistance and thus of the effective properties of the
687 model, seeing Eq. (4). Generally, there are two theoretical methods to calculate the
688 effective properties, depending on whether the fracture interaction is considered or not
689 (Kachanov, 1992; Davy et al., 2018). One method is the Non-Interaction
690 Approximation (NIA), which states that each fracture can be regarded as isolated and
691 that its surrounding medium is maintained intact as the initial elastic matrix. The NIA
692 allows a simple summation to calculate the effective properties while keeps high
693 accuracy. Grechka and Kachanov (2006) showed that the NIA still holds up even at
694 high fracture densities, as long as fracture locations are random. The second method,
695 e.g., Self-Consistent Scheme (O'Connell & Budiansky, 1974) and Differential Scheme
696 (Hashin, 1988), suggests that the impact of fracture interactions can be approximated
697 by a reduced effective properties of the surrounding medium. For the i th fracture,
698 therefore, the average matrix resistance can be calculated as:

$$699 \quad \bar{k}_{m,i} = \frac{2G_{i-1}}{a_{i-1}\pi(1-\nu_{i-1})} \quad (\text{A6})$$

700 in which G_{i-1} and ν_{i-1} are the effective shear modulus and Poisson's ratio, respectively,
701 of the rock mass volume resulting from the previous ($i-1$) fractures. In Section 4,
702 randomly distributed fractures are generated within the elastic matrix. In order to
703 investigate the influences of fracture properties on the effective properties and stress
704 variations, we use the NIA for simplicity to quantify the fracture contribution.

705

706 **Appendix B. Bisection method for stress update**

707 Bisection method is utilized to iteratively determine the stress change $\Delta\sigma_{yy}$,
708 before which a continuous function with variable $\Delta\sigma_{yy}$ is established in terms of constant
709 strain:

$$710 \quad f(\Delta\sigma_{yy,j}) = \varepsilon_{yy,0}^m - (\varepsilon_{yy,j}^m + \varepsilon_{yy,j}^{frac}) \quad (B1)$$

711 where $\varepsilon_{yy,0}^m = \varepsilon_{yy}^m$ is the fixed reference strain in the y-direction with ‘0’ being the
712 initial input. $\varepsilon_{yy,j}^m$ and $\varepsilon_{yy,j}^{frac}$ in the parenthesis represent the strain components in the
713 y-direction of elastic matrix and contributed by fractures, respectively, at the j th
714 iterative step. With the trial $\Delta\sigma_{yy,j}$ and a trial stress tensor,

$$715 \quad \boldsymbol{\sigma}_i = \begin{bmatrix} \sigma_{xx} & \sigma_{xy} \\ \sigma_{yx} & (\sigma_{yy} - \Delta\sigma_{yy,j}) \end{bmatrix} \quad (B2)$$

716 $\varepsilon_{yy,j}^m$ is calculated by Eq. (A5) with the trial stress tensor. Note that, the updated normal
717 stress difference, i.e., differential stress $|\sigma_{xx} - \sigma_{yy}|$, is invariably decreased. Therefore,
718 displacements of all fractures should be re-calculated under the trial stress tensor
719 according to the unloading constitutive law in Section 2.2. Based on Eq. (A4), the new
720 elastic matrix strain and new fracture displacements are further combined to update the
721 global strain of each layer. This iteration will continue until Eq. (B1) reaches zero or a
722 sufficiently small value.

723 More specifically, Figure B1 shows the numerical algorithm searching for the
724 root of $f(\Delta\sigma_{yy}) = 0$. At the beginning of the iteration, it is necessary to define an interval
725 $[m, n]$ allowing $f(m) \cdot f(n) < 0$. In the context of stress adjustment, we simply let $m = 0$,
726 which is one end-member case with no constraint of strain boundary, and let $n = |\sigma_{xx} -$
727 $\sigma_{yy}|$, which is the other end-member case where the representative volume is under an
728 isotropic state of stress. Then each iteration performs these steps:

729 **Step-1:** Calculate the midpoint of the interval, $\Delta\sigma_{yy,j} = (m + n)/2$;

730 **Step-2:** Calculate the function value at the midpoint, $f(\Delta\sigma_{yy,j})$;

731 **Step-3:** If $|\Delta\sigma_{yy,j} - m|$ is sufficiently small or $f(\Delta\sigma_{yy,j}) = 0$, return $\Delta\sigma_{yy,j}$ and stop iterating;

732 **Step-4:** If Step-3 is not satisfied, examine the sign of $f(\Delta\sigma_{yy,j})$. Replace either m or n
733 with $\Delta\sigma_{yy,j}$ in order to ensure the root is within the new interval. Then Set $j = j + 1$ and
734 return to Step-1.

735

736 **Acknowledgments**

737 This work is supported by Swiss National Science Foundation (grant No. 182150). This
738 is a theoretical study and contains no collected data. The scripts used to produce the
739 results can be requested from the authors.

740

741

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