An ASM specification of C# threads and the .NET memory model

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Abstract. We present a high-level ASM model of C# threads and the .NET memory model. We focus on purely managed, fully portable threading features of C#. The sequential model interleaves the computation steps of the currently running threads and is suitable for uniprocessors. The parallel model addresses problems of true concurrency on multiprocessor systems. The models provide a sound basis for the development of multi-threaded applications in C#. The thread and memory models complete the abstract operational semantics of C# in [2].

1 Introduction

Modern object-oriented programming languages like Java or C# support multi-threaded programming. They allow several threads to run concurrently sharing objects on the heap in the same address space. Each thread has its own frame stack, program counter, local variables and registers. The languages have special syntactical constructs for synchronization. Java has a synchronized statement and synchronized methods, while C# has a lock statement and several attributes that can be applied to classes and methods to control their run-time synchronization behavior.

Although the C# programming languages supports multi-threaded programming directly via special syntax, the underlying thread model is poorly documented and still considered to be part of the library. The Ecma standards for C# [4] and the Common Language Infrastructure [5] contain only a few paragraphs about threads. For example, the lock statement is defined in [4, §15.22] by a reduction to the library functions Monitor.Enter and Monitor.Exit which are not further specified there. Important issues, such as the order of writes to volatile and non-volatile fields, are just briefly mentioned in two paragraphs in [4, §10.10, §17.4.3]. Hence, a program developer has to rely solely on the class library documentation that comes with Microsoft’s .NET framework Software Development Kit [11]. Unfortunately, that documentation is not very precise with respect to threads, locks and memory issues. Moreover, it is not identical with the (XML) specification of the types that comprise the standard libraries in [5, Partition IV, Profiles and Libraries]. For example, specifications
of \texttt{Thread.Interrupt}, \texttt{Thread.Suspend} and \texttt{Thread.Resume} are not included in [5].

If a programmer cannot rely on a simple and precise thread model, the task of writing reliable multi-threaded applications that are correctly synchronized and free of data races and deadlocks becomes very difficult and tedious. Multi-threaded programs depend on the scheduling policy of underlying run-time system and therefore synchronization errors are difficult to reproduce and to debug. Moreover, certain problems may only occur under heavy threading stress in production environments like web services which cannot be simulated during the development cycle. Tools that statically analyze multi-threaded programs for synchronization problems are in general neither sound nor complete. Nevertheless, in some cases the may report a high percentage of all possible conflicts (see [19]).

The Java Language Specification [7, Ch. 17] devotes a whole chapter to threads and locks. However, that specification has been found to be hard to understand and has subtle, often unintended, implications. Therefore, the Java community has proposed a new specification of the semantics of threads and locks often referred to as the \textit{New Java Memory Model} [10]. Whether the new specification is easier to understand may be doubted. It justifies at least most of the common compiler optimizations which were prohibited by the old one. For a comparison and analysis of the different proposals we refer to [1].

The specification of threads in this article extends the modular definition of the semantics of C# in [2] by a new module C#\_T for multi-threaded C#. We focus on purely managed, fully portable threading features of C# and the .NET common language runtime. We do not consider the .NET equivalents of Win32 threading primitives such as \texttt{WaitHandle} and their derived classes. We also do not model asynchronous delegates and synchronization domains. The starting point of our model has been the thread model for Java in [17]. That model however is only correct for uniprocessor systems and does not address problems of true concurrency.

For basic terminology on Abstract State Machines we refer the reader to [3,8].

## 2 Threads in Microsoft’s .NET framework

The thread related features of C# are collected in the \texttt{System.Threading} namespace (see Fig. 1). The namespace contains the delegate type \texttt{ThreadStart} that denotes the type of functions with zero arguments and return type \texttt{void}. The most important classes of the namespace are the \texttt{Thread} and \texttt{Monitor} classes. Several thread related exception classes derived from \texttt{SystemException} are also declared in the namespace.

A thread can be in one or more states of the \texttt{ThreadState} enumeration (listed in Fig. 1). Unfortunately, the documentation does not state clearly which combinations of states are allowed for a thread and which are not. Moreover, some of the states are not real execution states of a thread but just boolean flags. The \texttt{Background} state, for example, tells the run-time system that it can kill the
thread and exit when all non-background threads have terminated (similar to the Daemon property of threads in Java). Other states, like StopRequested, are for internal use only and should not be exposed to the programmer in a public enumeration. The Aborted state has a rather obscure meaning (see below). If there is an AbortRequested, why is there no InterruptRequested?

The ThreadState property of the Thread class returns a snapshot containing the states of a thread as a bitset. This information, however, cannot be used for synchronization purposes, since it may already been outdated when it is obtained. Therefore, we do not model the ThreadState property below and use a different set of execution states in our model.

Threads are represented in C# by instances of class Thread in Fig. 2. Unlike in Java, this class is sealed (final in Java terminology) and cannot be subclassed. The constructor of the class takes a pointer to a ThreadStart function which will be executed when the new thread is started. The two static methods of the class, Sleep and ResetAbort, are implicitly called on the current thread.

The constructor of class Monitor in Fig. 2 is private, which means that no instances of this class can be created. The reason is, that in C# (like in Java) every object reference can be used as a monitor and therefore there is no need to create special monitors. The Monitor class contains only static methods. Its Wait, Pulse and PulseAll methods are similar to Java’s wait, notify and notifyAll methods of class java.lang.Object.

The Enter and Exit methods of the Monitor class are used to syntactically reduce the lock statement of C# (where o is a fresh local variable):

\[
\text{lock (exp) } \text{stm} \quad \Rightarrow \quad \begin{cases} 
\text{object } o = \text{exp;} \\
\text{Monitor.Enter}(o); \\
\text{try } \{ \text{stm} \} \\
\text{finally } \{ \text{Monitor.Exit}(o); \}
\end{cases}
\]

Unlike in Java, the Monitor.Enter and Monitor.Exit methods can be called explicitly in C# programs and hence C# cannot guarantee that a thread holds no more locks when it has terminated.

3 An ASM model for threads on uniprocessors

Whenever in C# an object is created on the heap, it gets two additional overhead fields associated with it. The first field is a pointer to the object’s method table. This pointer makes it possible to obtain the run-time type (exact type) of the object. The second field contains an index of a SyncBlock. SyncBlocks are associated with an object on the fly when the object is used as a monitor. A SyncBlock structure contains information that is used for thread synchronization (cf. [14]).
namespace System.Threading {

delegate void ThreadStart();

enum ThreadState {
    Running = 0,
    StopRequested = 1,
    SuspendRequested = 2,
    Background = 4,
    Unstarted = 8,
    Stopped = 16,
    WaitSleepJoin = 32,
    Suspended = 64,
    AbortRequested = 128,
    Aborted = 256
}

sealed class Thread {
    Thread(ThreadStart start);
    void Start();
    bool Join(int msec);
    static void Sleep(int msec);
    void Abort();
    static void ResetAbort();
    void Interrupt();
    void Suspend();
    void Resume();
    ...
}

sealed class Monitor {
    private Monitor() { }
    ...
    static void Enter(object obj);
    static void Exit(object obj);
    static bool Wait(object obj, int msec);
    static void Pulse(object obj);
    static void PulseAll(object obj);
    ...
}

Fig. 1. The System.Threading namespace and the ThreadState enumeration.

Fig. 2. The Thread class and the Monitor class.

3.1 The vocabulary for threads and monitors

We abstract from implementation details and assume that the dynamic function
\texttt{runTimeType: Ref} \rightarrow \texttt{Type}\) returns for every object reference its run-time type. The set of threads can then be defined as follows:

\[ Thread = \{ \texttt{ref} \in \texttt{Ref} \mid \texttt{runTimeType}(\texttt{ref}) = \texttt{Thread} \} \]

The subuniverse \texttt{Monitor} \subseteq \texttt{Ref} is equipped with a dynamic function \texttt{lockOwner} which returns the thread that currently owns the lock of the monitor, a \texttt{lockCount} which counts how many times a thread has to exit the monitor before the lock is released, a \texttt{readyQueue} (also known as \texttt{lock queue}) which holds the ordered queue of blocked threads that are ready to acquire the lock, and a \texttt{waitQueue} which holds the ordered queue of threads that are waiting on the monitor.

\texttt{lockOwner: Monitor} \rightarrow \texttt{Thread} \cup \{\texttt{None}\}
\texttt{lockCount: Monitor} \times \texttt{Thread} \rightarrow \mathbb{N}
\texttt{readyQueue: Monitor} \rightarrow \texttt{List(Thread)}
\texttt{waitQueue: Monitor} \rightarrow \texttt{List(Thread)}
When an object \( \texttt{ref} \) is used as a \textit{Monitor} the functions are initialized as follows:

\[
\begin{align*}
\text{lockOwner}(\texttt{ref}) & := \texttt{None} & \text{readyQueue}(\texttt{ref}) & := [] \\
\text{lockCount}(\texttt{ref}, \texttt{thread}) & := \texttt{Undef} & \text{waitQueue}(\texttt{ref}) & := []
\end{align*}
\]

The possible execution states of a thread (explained in detail below) are:

\[
\text{ExecState} := \text{Unstarted} \mid \text{Active} \mid \text{Suspended} \mid \text{Sleeping} \mid \text{Joined} \\
\mid \text{Syncing} \mid \text{Waiting} \mid \text{Pulsed} \mid \text{Dead}
\]

The function \texttt{execState} returns the unique execution state of a thread.

\[
\texttt{execState}: \text{Thread} \rightarrow \text{ExecState}
\]

Every thread has a \texttt{joinSet} that comprises the threads that are joined to it and are waiting for its termination, a \texttt{wakeupTime} that stores the time when the thread expires, a \texttt{monObj} with the monitor a thread is waiting for or wants to acquire, a \texttt{joinedThread} in case the thread is joined, and several flags indicating whether an abort has been requested or initiated, whether an interrupt has been requested, or whether a suspend has been requested.

\[
\begin{align*}
\text{joinSet}(\texttt{ref}) & := \emptyset & \text{abortRequested}(\texttt{ref}) & := \texttt{False} \\
\text{wakeupTime}(\texttt{ref}) & := \texttt{Undef} & \text{abortInitiated}(\texttt{ref}) & := \texttt{False} \\
\text{monObj}(\texttt{ref}) & := \texttt{Undef} & \text{interruptRequested}(\texttt{ref}) & := \texttt{False} \\
\text{joinedThread}(\texttt{ref}) & := \texttt{Undef} & \text{suspendRequested}(\texttt{ref}) & := \texttt{False} \\
\text{execState}(\texttt{ref}) & := \texttt{Unstarted}
\end{align*}
\]

The local state of a thread comprises a frame stack of activation records, the currently executed method, the current position in the method body (program counter), the local environment and the already computed values of expressions (operand stack).

\[
\begin{align*}
\text{frames}: \text{Thread} \rightarrow \text{List(\text{Frame})} & & \text{locals}: \text{Thread} \rightarrow (\text{Loc} \rightarrow \text{Adr}) \\
\text{meth}: \text{Thread} \rightarrow \text{Meth} & & \text{values}: \text{Thread} \rightarrow (\text{Pos} \rightarrow \text{Result}) \\
\text{pos}: \text{Thread} \rightarrow \text{Pos} & & 
\end{align*}
\]

The current thread is denoted by \texttt{‘self’} in the ASM rules below.

Fig. 3 shows a classification of the execution states of a thread and relates them to the items of the \textit{ThreadState} enumeration in Fig. 1. A thread is \textit{Running} if it is not \textit{Unstarted} and not already \textit{Dead}. A thread is considered to be \textit{Passive} (or \textit{WaitSleepJoin}) if it is \textit{Running} but neither \textit{Active} nor \textit{Suspended}.  

5
Fig. 3. The execution states of a thread.

Running\( (\text{thread}) \) ⟺ \text{execState}(\text{thread}) \notin \{\text{Unstarted}, \text{Dead}\}

Passive\( (\text{thread}) \) ⟺ \text{WaitSleepJoin}(\text{thread}) ⟺ \text{execState}(\text{thread}) \in \{\text{Syncing}, \text{Waiting}, \text{Pulsed}, \text{Sleeping}, \text{Joined}\}

The items \text{Stopped} and \text{Aborted} of the \text{ThreadState} enumeration can be obtained as follows:

\[ \text{Stopped}(\text{thread}) \iff \text{execState}(\text{thread}) = \text{Dead} \land \neg \text{abortRequested}(\text{thread}) \]

\[ \text{Aborted}(\text{thread}) \iff \text{execState}(\text{thread}) = \text{Dead} \land \text{abortRequested}(\text{thread}) \]

The reason for this separation is not known to us.

3.2 The methods of the \text{Thread} class

Fig. 4 and 5 contain diagrams for the execution states of a thread. Methods that are invoked by another thread on the current thread are displayed in grey boxes, whereas methods invoked by the current thread itself are put into white boxes. If there is no outgoing arrow for a thread method from an execution state, then this can mean either that such an invocation is not possible, e.g. since a static method can only be invoked by an active thread, or that the invocation is not allowed and throws a \text{ThreadStateException}.

When a thread is created by invoking the constructor of the \text{Thread} class its execution state is \text{Unstarted}. The new thread is later started by invoking the \text{Thread.Start} method. A thread can only be started once, otherwise a \text{ThreadStateException} exception is thrown. If there has already been an abort requested for the thread, its execution state is immediately changed to \text{Dead}. Otherwise, the execution state of the thread is updated to \text{Active} and its local state is initiated. The new thread now runs concurrently with the thread that invoked the \text{Thread.Start} method. The \text{YIELDUP(Norm)} means that the \text{Thread.Start} methods returns without blocking.
Thread.Resume
Thread.Start
Thread.Abort
Thread.Start
Thread.Interrupt
Thread.Abort
Thread.Interrupt
Thread.Abort
Thread.Abort
SetInterruptRequest
SetSuspendRequest
Active
Dead
SetInterruptRequest
SetAbortRequest
Suspended
SafePoint?
Fig. 4. Methods invoked by other threads on the current thread.

ThreadStart(thread) ≡
  if \text{execState}(thread) \neq Unstarted then FailUp(ThreadStateException)
  else
      if \text{abortRequested}(thread) then \text{execState}(thread) := Dead
      else \{ThreadInit(thread), \text{execState}(thread) := Active\}
      YieldUp(Norm)

When a thread is created, a delegate of type ThreadStart has to be provided to the constructor of the Thread class. This delegate is later invoked, when the thread is started. Technically, this means the new thread executes the Invoke method of the ThreadStart delegate. If the invocation list of that delegate consists of a single method, then this method is executed. Otherwise, the methods of the invocation list are executed sequentially.

ThreadInit(thread) ≡
  let d = getField(thread, Thread::delegate)
  let m = ThreadStart::Invoke() in
    thread.frames := []
    thread.meth := m
    thread.pos := body(m)
    thread.values := ∅
    thread.INITLocals(m, [d]) // this is the delegate d

The Thread.Join methods puts the current thread into the join set of the other thread and changes the execution state of the current thread from Active to Joined. Like every thread method that takes a timeout argument it checks first
Fig. 5. Methods invoked by the current thread.
whether the argument is in the correct range. If an interrupt has been requested, then it throws a \texttt{ThreadInterruptedException} instead of joining (Mono 0.26 ignores the interrupt request \cite{12}).

\begin{verbatim}
\texttt{ThreadJoin(\textit{thread}, \textit{msec})} ≡
    \begin{cases}
      \texttt{FailUp(\textit{ArgumentOutOfRangeException})} & \text{if } \textit{msec} < -1 \\
      \texttt{FailUp(\textit{ThreadStateException})} & \text{else if } \texttt{execState(\textit{thread}) = Unstarted}
      \begin{cases}
        \texttt{FailUp(\textit{ThreadStateException})} & \text{elseif } \texttt{execState(\textit{thread}) = Dead}
        \texttt{YieldUp(True)} & \text{ elseif } \texttt{interruptRequested(\textit{self})}
        \texttt{THROW_INTERRUPTED_EXCEPTION} & \text{else}
      \end{cases}
      \texttt{SetWakeupTime(\textit{msec})}
      \texttt{joinSet(\textit{thread}) := \textit{joinSet(\textit{thread}) ∪ \{self\}}
      \texttt{joinedThread(\textit{self}) := \textit{thread}}
      \texttt{execState(\textit{self}) := Joined}
    \end{cases}
\end{verbatim}

The thread will become active again, when the other thread has terminated or \textit{msec} milliseconds have passed. An argument of $-1$ milliseconds means an infinite amount of time.

\begin{verbatim}
\texttt{SetWakeupTime(\textit{msec})} ≡
    \begin{cases}
      \texttt{wakeupTime(\textit{self}) := \infty} & \text{if } \textit{msec} = -1 \\
      \texttt{currentTime(\textit{self}) + \textit{msec} & \text{else}}
    \end{cases}
\end{verbatim}

When an \texttt{ThreadInterruptedException} is thrown, the interrupt request of the current thread is cleared.

\begin{verbatim}
\texttt{THROW_INTERRUPTED_EXCEPTION} ≡
    \begin{cases}
      \texttt{FailUp(\textit{ThreadInterruptedException})} & \text{ if }
      \texttt{interruptRequested(\textit{self}) := False}
    \end{cases}
\end{verbatim}

When the \texttt{Thread.Join} method returns, it indicates with a boolean result, whether the other thread is dead. If the other thread is not dead, then it follows from the definition of the predicate \textit{Expired} and the \texttt{Wakeup} rule in Sect. 3.4 that the amount of time has expired.

\begin{verbatim}
\texttt{ThreadJoinReturn} ≡
    \begin{cases}
      \texttt{YieldUp(True)} & \text{ if } \texttt{execState(\textit{joinedThread(\textit{self})) = Dead}
      \texttt{YieldUp(False)} & \text{ else}
    \end{cases}
\end{verbatim}

The \texttt{Thread.Sleep} method puts the current thread to sleep for the specified amount of milliseconds. The execution state of the current thread is changed from \texttt{Active} to \texttt{Sleeping}. If an interrupt has been requested, the current thread throws a \texttt{ThreadInterruptedException} instead of going to sleep.

\begin{verbatim}
\texttt{ThreadSleep(\textit{msec})} ≡
    \begin{cases}
      \texttt{FailUp(\textit{ArgumentOutOfRangeException})} & \text{if } \textit{msec} < -1 \\
      \texttt{THROW_INTERRUPTED_EXCEPTION} & \text{else if } \texttt{interruptRequested(\textit{self})}
      \texttt{else}
        \begin{cases}
          \texttt{execState(\textit{self}) := Sleeping} & \texttt{SetWakeupTime(\textit{msec})}
          \texttt{YieldUp(Norm)} & \texttt{else}
        \end{cases}
    \end{cases}
\end{verbatim}
In order to abort another thread with the `Thread.Abort` method, the current threads needs the appropriate security permission. If the other thread is suspended, a `ThreadStateException` is thrown, although the documentation [11] says that in that case the other thread is resumed by the system. The `Thread.Abort` sets an abort request for the other thread. The effect of this request is that a `ThreadAbortException` is thrown asynchronously in the other thread (see Sect. 3.4).

\[
\text{ThreadAbort}(\text{thread}) \equiv \\
\begin{align*}
& \text{if } \neg \text{SecurityPermission}(\text{self}, \text{ControlThread}) \text{ then} \\
& \quad \text{FailUp}(\text{SecurityException}) \\
& \text{elseif execState}(\text{thread}) = \text{Suspended} \text{ then} \\
& \quad \text{FailUp}(\text{ThreadStateException}) \\
& \quad \text{else} \\
& \quad \quad \text{if } \neg \text{abortRequested}(\text{thread}) \land \neg \text{abortInitiated}(\text{thread}) \text{ then} \\
& \quad \quad \quad \text{abortRequested}(\text{thread}) := \text{True} \\
& \quad \quad \text{YieldUp}(\text{Norm})
\end{align*}
\]

The static method `Thread.ResetAbort` can be invoked by the current thread to cancel the automatic re-throwing of a `ThreadAbortException` at the end of catch blocks. It clears the flag that indicates that the abort has been initiated. Only threads that have the appropriate security permission can cancel an abort. The documentation [11] says that the method throws a `ThreadStateException` if the method was not invoked on the current thread. This can never happen, since it is a static method.

\[
\text{ThreadResetAbort} \equiv \\
\begin{align*}
& \text{if } \neg \text{SecurityPermission}(\text{self}, \text{ControlThread}) \text{ then} \\
& \quad \text{FailUp}(\text{SecurityException}) \\
& \quad \text{elseif } \neg \text{abortInitiated}(\text{self}) \text{ then } \text{FailUp}(\text{ThreadStateException}) \\
& \quad \quad \text{else } \{ \text{abortInitiated}(\text{self}) := \text{False}, \text{YieldUp}(\text{Norm}) \}
\end{align*}
\]

The `Thread.Interrupt` method sets an interrupt request for another thread. The effect of the request is that a `ThreadInterruptedException` is injected into the other thread, if it is in a passive state (see Sect. 3.4). Otherwise, the exception is thrown by the other thread, when it changes its execution state from running into a passive state. If the other thread stays active forever, the interrupt request is ignored.

\[
\text{ThreadInterrupt}(\text{thread}) \equiv \\
\begin{align*}
& \text{if } \neg \text{SecurityPermission}(\text{self}, \text{ControlThread}) \text{ then} \\
& \quad \text{FailUp}(\text{SecurityException}) \\
& \quad \text{else} \\
& \quad \quad \text{if } \neg \text{interruptRequested}(\text{thread}) \text{ then} \\
& \quad \quad \quad \text{interruptRequested}(\text{thread}) := \text{True} \\
& \quad \quad \text{YieldUp}(\text{Norm})
\end{align*}
\]

The `Thread.Suspend` method sets a suspend request for another thread, if it is running. The request will asynchronously be processed by the run-time system (see Sect. 3.4).
ThreadSuspend(thread) ≡
  if ¬SecurityPermission(self, ControlThread) then
    FailUp(SecurityException)
  elseif execState(thread) ∈ {Unstarted, Dead} then
    FailUp(ThreadStateException)
  else
    if ¬suspendRequested(thread) ∧ execState(thread) ≠ Suspended
      then suspendRequested(thread) := True
    YieldUp(Norm)

A thread can be resumed by invoking Thread.Resume only if it is suspended or a suspend request is pending. If the thread is suspended, then its execution state is changed back to active such that it can be scheduled for execution by the run-time system again. If a suspend has been requested, the request is cleared.

ThreadResume(thread) ≡
  if ¬SecurityPermission(self, ControlThread) then
    FailUp(SecurityException)
  elseif execState(thread) ≠ Suspended ∧ ¬suspendRequested(thread)
    then FailUp(ThreadStateException)
  else
    if execState(thread) = Suspended then execState(thread) := Active
    if suspendRequested(thread) then suspendRequested(thread) := False
    YieldUp(Norm)

If a ThreadSuspend(t) is executed in parallel with a ThreadResume(t) on a thread t that already has a suspend request, the resume has priority over the suspend.\footnote{One could as well forbid the parallel execution by a run constraint (see Sect. 4.1).}

3.3 The methods of the Monitor class

The methods of the Monitor class are static and are used to acquire and release locks of monitors. If they are invoked with the null reference, an exception is thrown. The Monitor.Enter method is used to acquire the lock of a monitor. If the current thread already owns the lock, the lockCount is increased. If the lock is free and the readyQueue of the monitor is empty, the thread immediately gets the lock. Otherwise, the thread changes its state from Active to Syncing and the thread is added to the readyQueue of the monitor. In case of a pending interrupt, a ThreadInterruptedException is thrown.

MonitorEnter(mon) ≡
  if mon = Null then FailUp(ArgumentNullException)
  elseif lockOwner(mon) = self then
    lockCount(mon, self) := lockCount(mon, self) + 1
    YieldUp(Norm)
  elseif lockOwner(mon) = None ∧ Empty(readyQueue(mon)) then

\[
\text{ThreadSuspend}(\text{thread}) \equiv \\
\quad \text{if } \neg \text{SecurityPermission}(\text{self, ControlThread}) \text{ then} \\
\quad \quad \text{FailUp}(\text{SecurityException}) \\
\quad \text{elseif } \text{execState}(\text{thread}) \in \{\text{Unstarted, Dead}\} \text{ then} \\
\quad \quad \text{FailUp}(\text{ThreadStateException}) \\
\quad \text{else} \\
\quad \quad \text{if } \neg \text{suspendRequested}(\text{thread}) \land \text{execState}(\text{thread}) \neq \text{Suspended} \\
\quad \quad \quad \text{then } \text{suspendRequested}(\text{thread}) := \text{True} \\
\quad \quad \text{YieldUp}(\text{Norm})
\]

A thread can be resumed by invoking Thread.Resume only if it is suspended or a suspend request is pending. If the thread is suspended, then its execution state is changed back to active such that it can be scheduled for execution by the run-time system again. If a suspend has been requested, the request is cleared.

\[
\text{ThreadResume}(\text{thread}) \equiv \\
\quad \text{if } \neg \text{SecurityPermission}(\text{self, ControlThread}) \text{ then} \\
\quad \quad \text{FailUp}(\text{SecurityException}) \\
\quad \text{elseif } \text{execState}(\text{thread}) \neq \text{Suspended} \land \neg \text{suspendRequested}(\text{thread}) \\
\quad \quad \text{then } \text{FailUp}(\text{ThreadStateException}) \\
\quad \text{else} \\
\quad \quad \text{if } \text{execState}(\text{thread}) = \text{Suspended} \text{ then } \text{execState}(\text{thread}) := \text{Active} \\
\quad \quad \text{if } \text{suspendRequested}(\text{thread}) \text{ then } \text{suspendRequested}(\text{thread}) := \text{False} \\
\quad \quad \text{YieldUp}(\text{Norm})
\]

If a ThreadSuspend(t) is executed in parallel with a ThreadResume(t) on a thread t that already has a suspend request, the resume has priority over the suspend.\footnote{One could as well forbid the parallel execution by a run constraint (see Sect. 4.1).}
To lock a monitor means to update the lockOwner of the monitor.  

\[
\text{LOCK}(\text{self}, \text{mon})
\]

\[
\text{lockCount}(\text{mon}, \text{self}) := 1
\]

\[
\text{YIELDUP}(\text{Norm})
\]

\[
\text{else if} \quad \text{interruptRequested}(\text{self}) \quad \text{then} \quad \text{THROWINTERRUPTEDEXCEPTION}
\]

\[
\text{else}
\]

\[
\text{readyQueue}(\text{mon}) := \text{readyQueue}(\text{mon}) \cdot [\text{self}]
\]

\[
\text{monObj}(\text{self}) := \text{mon}
\]

\[
\text{execState}(\text{self}) := \text{Syncing}
\]

\[
\text{YIELDUP}(\text{Norm})
\]

The Monitor.Exit method decrements the lock count by one. If the lock count becomes 0, the lock is released.

\[
\text{MONITOREXIT}(\text{mon}) \equiv
\]

\[
\text{if} \quad \text{mon} = \text{Null} \quad \text{then} \quad \text{FAILUP} (\text{ArgumentNullException})
\]

\[
\text{elseif lockOwner}(\text{mon}) \neq \text{self} \quad \text{then}
\]

\[
\text{FAILUP} (\text{SynchronizationLockException})
\]

\[
\text{else}
\]

\[
\text{if} \quad \text{lockCount}(\text{mon}, \text{self}) = 1 \quad \text{then}
\]

\[
\text{UNLOCK}(\text{self}, \text{mon})
\]

\[
\text{lockCount}(\text{mon}, \text{self}) := \text{lockCount}(\text{mon}, \text{self}) - 1
\]

\[
\text{YIELDUP}(\text{Norm})
\]

To release a lock means to update the lockOwner of the monitor to None.

\[
\text{UNLOCK}(\text{thread}, \text{mon}) \equiv \text{lockOwner}(\text{mon}) := \text{None}
\]

The documentation [11] says that a thread can only exit a monitor if it owns the lock. The following code, however, runs in the .NET framework 1.1 as well as in Rotor [16] without throwing a SynchronizationLockException.

\[
\text{Object o = new object();}
\]

\[
\text{Monitor.Enter(o);}
\]

\[
\text{Monitor.Exit(o);}
\]

\[
\text{Monitor.Exit(o);} \quad // \text{Bug. Thread does not own lock.}
\]

The Monitor.Wait method appends the current thread to the waitQueue of the monitor and temporarily releases the lock of the monitor. The execution state of the current thread is changed from Active to Waiting.

\[
\text{MONITORWAIT}(\text{mon}, \text{msec}) \equiv
\]

\[
\text{if} \quad \text{mon} = \text{Null} \quad \text{then} \quad \text{FAILUP} (\text{ArgumentNullException})
\]

\[
\text{elseif msec < −1} \quad \text{then} \quad \text{FAILUP} (\text{ArgumentOutOfRangeException})
\]

\[
\text{elseif lockOwner}(\text{mon}) \neq \text{self} \quad \text{then}
\]

\[
\text{FAILUP} (\text{SynchronizationLockException})
\]

\[
\text{elseif interruptRequested}(\text{self}) \quad \text{then} \quad \text{THROWINTERRUPTEDEXCEPTION}
\]

\[
\text{else}
\]

\[
\text{SETWAKEUPTIME}(\text{msec})
\]

\[
\text{waitQueue}(\text{mon}) := \text{waitQueue}(\text{mon}) \cdot [\text{self}]
\]
Unlock(self, mon)
monObj(self) := mon
execState(self) := Waiting

The thread remains in the \textit{waitQueue} of the monitor until the monitor is pulsed or \textit{msec} milliseconds have passed. At the return, the method indicates with a boolean result whether the time has expired.

\textbf{MonitorWaitReturn} ≡
if \textit{wakeupTime}(self) < \textit{currentTime} then YieldUp(True)
else YieldUp(False)

The \textbf{Monitor.Pulse} method moves the first element of the \textit{waitQueue} of the monitor to the \textit{readyQueue}. If the \textit{waitQueue} is empty, the method just returns. Note, that we allow also that a thread with an abort or an interrupt request can be pulsed (this point is discussed also in [10]).

\textbf{MonitorPulse}(mon) ≡
if mon = Null then FailUp(ArgumentNullException)
elseif lockOwner(mon) \neq self then
  FailUp(SynchronizationLockException)
else
  if \neg Empty(waitQueue(mon)) then
    MoveToReadyQueue(first(waitQueue(mon)), mon)
  YieldUp(Norm)

When a thread is moved from the \textit{waitQueue} to the \textit{readyQueue}, its execution state is changed from \textit{Waiting} to \textit{Pulsed}.

\textbf{MoveToReadyQueue}(thread, mon) ≡
readyQueue(mon) := readyQueue(mon) \cdot [thread]
waitQueue(mon) := delete(thread, waitQueue(mon))
execState(thread) := Pulsed

The \textbf{Monitor.PulseAll} methods moves all waiting threads into the \textit{readyQueue} of the monitor.

\textbf{MonitorPulseAll}(mon) ≡
if mon = Null then FailUp(ArgumentNullException)
elseif lockOwner(mon) \neq self then
  FailUp(SynchronizationLockException)
else
  forall thread ∈ waitQueue(mon) do execState(thread) := Pulsed
  readyQueue(mon) := readyQueue(mon) \cdot waitQueue(mon)
  waitQueue(mon) := []
  YieldUp(Norm)

In Java, the wait and the ready queues are not FIFO queues but unordered sets. The \textbf{Object.notify} method of Java chooses an arbitrary element from the wait set of an object and it is not guaranteed that every thread in the wait set is ever chosen. The proposal for the new Java memory model [10] even allows so-called \textit{spurious wake-ups}. This means that the system is allowed to remove a
thread from the wait set of an object without any reason. Note, that the POSIX thread function `pthread_cond_signal()` is also allowed to wake up more than one thread.

3.4 Scheduling of threads, timing, locking and asynchronous exceptions

Although priorities can be assigned to threads in C#, it is not guaranteed that they are honored by the scheduling algorithm. The main ASM rule for sequential C# therefore chooses repeatedly one of the possible threads and executes one (small) step in the computation of the thread. In this way the computation steps of the currently running threads are interleaved.

\[
\text{ExecSequentialCsharp} \equiv \\
\text{choose } \text{thread } \in \text{Thread} \text{ do ExecStep(thread)}
\]

The next computation step of a thread depends on its current execution state.

\[
\text{ExecStep(thread)} \equiv \\
\text{if } \text{execState(thread)} = \text{Active} \text{ then ExecActive(thread)} \\
\text{elseif Expired(thread) then Wakeup(thread)} \\
\text{elseif CanAcquireLock(thread) then AcquireLock(thread)} \\
\text{elseif Passive(thread) } \land \text{ HasRequest(thread) then} \\
\text{AbortOrInterruptPassive(thread)}
\]

A thread is expired, if its wakeup time has been passed. The system time in milliseconds is given by the monitored function \(\text{currentTime}\).

\[
\text{Expired(thread)} \iff \text{execState(thread)} \in \{\text{Waiting, Sleeping, Joined}\} \land \\
\text{wakeupTime(thread)} \leq \text{currentTime}
\]

A thread can acquire the lock, if it can acquire the lock of its current monitor object \(\text{monObj}\) that was set in \text{MonitorEnter} or \text{MonitorWait}.

\[
\text{CanAcquireLock(thread)} \iff \text{CanAcquireLock(thread, monObj(thread))}
\]

The lock of a monitor can be acquired, if the lock is free and the thread is the first thread in the \text{readyQueue} of the monitor.

\[
\text{CanAcquireLock(thread, mon)} \iff \\
\text{execState(thread)} \in \{\text{Syncing, Pulsed}\} \land \text{lockOwner(mon)} = \text{None} \land \\
\text{thread} = \text{first(readyQueue(mon))}
\]

A thread has a request, if it has an abort or an interrupt request.

\[
\text{HasRequest(t)} \iff \text{abortRequested(t)} \lor \text{interruptRequested(t)}
\]

When the execution state of the chosen thread is \text{Active}, the next step in the computation of the thread is executed by the rule \text{ExecCsharp(thread)}. In case of a pending abort the system waits until the thread has left any finally block or catch clause before it aborts the threads. In case of a pending suspend, the system waits until the thread reaches a so-called safe point before suspending the thread. Safe points are points that are also safe for garbage collection.
A thread aborts by throwing a `ThreadAbortException`. The fact that the thread is responding to the abort request is recorded in the `abortInitiated` flag.

\[
\text{Abort}(\text{thread}) \equiv 
\begin{align*}
\text{Fail}(\text{thread}, \text{ThreadAbortException}) \\
\text{ClearAbortRequest}(\text{thread}) \\
\text{abortInitiated}(\text{thread}) := \text{True}
\end{align*}
\]

When the abort request is cleared, any pending interrupt request is also cleared.

\[
\text{ClearAbortRequest}(\text{thread}) \equiv 
\begin{align*}
\text{abortRequested}(\text{thread}) := \text{False} \\
\text{if interruptRequested}(\text{thread}) \text{ then} \\
\text{interruptRequested}(\text{thread}) := \text{False}
\end{align*}
\]

Like any other exception, a `ThreadAbortException` is propagated upwards in the frame stack of the thread. If it crosses a try block with catch clauses and a possible finally block, the catch clauses are searched for a matching handler. If there exists one, the corresponding catch block is executed. The finally block is executed afterwards. At the end of the catch block, however, the `ThreadAbortException` is re-thrown by the system. More precisely, if an abort has been initiated and a catch block terminates but not with an exception, then a new `ThreadAbortException` is thrown at the end of the catch block. If the catch block terminates abruptly with an exception, that exception is propagated upwards. Hence, the rules for exception handling of C# of [2] have to be refined. If the current position of the thread (indicated by the black triangle) is at the end of a catch block with result `res` and `res` is not an exception, a `ThreadAbortException` is thrown. Hence a `ThreadAbortException` cannot be swallowed unless the `Thread.ResetAbort` method is called (see Sect. 3.2).

\[
\text{ExecCsharpStm}_T \equiv \text{match } \text{context}(\text{pos}) \begin{align*}
\text{try } \text{Exc}(\text{ref}) \ldots \text{catch}(\ldots) \triangleright \text{res} \ldots \rightarrow \hspace{1cm} \\
\text{execStack} := \text{pop}(\text{execStack}) \\
\text{if } \text{abortInitiated}(\text{self}) \land \text{res} \notin \text{Exc} \text{ then} \\
\text{FailUp}(\text{ThreadAbortException}) \\
\text{else } \text{YieldUp}(\text{res})
\end{align*}
\]

When a suspend request is pending and the thread has reached a safe point, the system changes its execution state from `Active` to `Suspended` and clears the request.

\[
\text{Suspend}(\text{thread}) \equiv 
\begin{align*}
\text{execState}(\text{thread}) := \text{Suspended} \\
\text{suspendRequested}(\text{thread}) := \text{False}
\end{align*}
\]
If a sleeping, joined or waiting thread has expired, the system has to wake up the thread. If the thread is **Sleeping**, its execution state is changed to **Active**. If the thread is **Joined**, it is removed from the **joinSet** and returns from the **Thread.Join** method (see Sect. 3.2). If the thread is **Waiting** it is moved to the **readyQueue** of the monitor and has to re-acquire the lock (its state is changed to **Pulsed**).

\[
\text{Wakeup}(\text{thread}) \equiv \\
\begin{array}{l}
\text{if } \text{execState}(\text{thread}) = \text{Sleeping} \text{ then } \text{execState}(\text{thread}) := \text{Active} \\
\text{if } \text{execState}(\text{thread}) = \text{Joined} \text{ then let } t = \text{joinedThread}(\text{thread}) \text{ in} \\
\qquad \text{joinSet}(t) := \text{joinSet}(t) \setminus \{\text{thread}\} \\
\qquad \text{execState}(\text{thread}) := \text{Active} \\
\text{if } \text{execState}(\text{thread}) = \text{Waiting} \text{ then} \\
\qquad \text{MoveToReadyQueue}(\text{thread}, \text{monObj}(\text{thread}))
\end{array}
\]

If a thread can acquire the lock, it becomes the owner of the lock. Its execution state is changed from **Pulsed** or **Syncing** to **Active**. If it acquires the lock for the first time, the **lockCount** is initialized to 1. Otherwise, when the thread has temporarily released the lock by invoking the **Monitor.Wait** method, the old lock count is still valid.

\[
\text{AcquireLock}(\text{thread}) \equiv \\
\begin{array}{l}
\text{let } \text{mon} = \text{monObj}(\text{thread}) \text{ in} \\
\qquad \text{Lock}(\text{thread}, \text{mon}) \\
\qquad \text{if } \text{execState}(\text{thread}) \neq \text{Pulsed} \text{ then } \text{lockCount}(\text{mon}, \text{thread}) := 1 \\
\qquad \text{readyQueue}(\text{mon}) := \text{tail}(\text{readyQueue}(\text{mon})) \\
\qquad \text{execState}(\text{thread}) := \text{Active}
\end{array}
\]

If a passive thread has an abort or an interrupt request, an exception is injected into the thread. If both, an abort request and an interrupt request are pending, the abort request has priority (unless the thread executes catch or finally code).

\[
\text{AbortOrInterruptPassive}(\text{thread}) \equiv \\
\begin{array}{l}
\text{if } \text{abortRequested}(\text{thread}) \land \neg \text{CatchFinallyCode}(\text{thread}) \text{ then} \\
\qquad \text{InjectException}(\text{thread}, \text{ThreadAbortException}) \\
\qquad \text{ClearAbortRequest}(\text{thread}) \\
\qquad \text{abortInitiated}(\text{thread}) := \text{True} \\
\text{elseif } \text{interruptRequested}(\text{thread}) \text{ then} \\
\qquad \text{InjectException}(\text{thread}, \text{ThreadInterruptedException}) \\
\qquad \text{interruptRequested}(\text{thread}) := \text{False}
\end{array}
\]

When a **ThreadAbortException** or a **ThreadInterruptedException** is injected into a passive thread, the execution state of the thread is changed to **Active** in order that the exception can propagate upwards and probably terminate the thread. If the thread is waiting, it is moved to the **readyQueue** and has to re-acquire the lock, since in this case the thread is still in a critical section of code and possible exception handlers and finally block should only be executed under the exclusive control of the monitor.

\[
\text{InjectException}(\text{thread}, \text{exception}) \equiv \\
\quad \text{Fail}(\text{thread}, \text{exception})
\]

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if \( \text{execState}(thread) \in \{\text{Syncing}, \text{Sleeping}, \text{Joined}\} \) then
\[
\text{execState}(thread) := \text{Active}
\]
if \( \text{execState}(thread) = \text{Waiting} \) then
\[
\text{MoveToReadyQueue}(thread, \text{monObj}(thread))
\]

A thread terminates when the frame stack of the thread is empty again and the \text{Invoke} method of the delegate of the thread terminates. The method can terminate normally or abruptly with an exception. In any case, the execution state of the thread is updated from \text{Active} to \text{Dead} and the threads that are joined are notified by changing their states from \text{Joined} to \text{Active} such that they can return from the \text{Thread.Join} method. If the thread terminates with an exception, the exception may or may not be reported as unhandled exception to the console.

\[
\text{ExecCsharpStm}_T \equiv \text{match context}(pos) \\
\text{res} \rightarrow \text{if } pos = \text{body}(\text{meth}) \land \text{Empty(frames)} \text{ then} \\
\text{forall thread} \in \text{joinSet}(\text{self}) \text{ do execState}(thread) := \text{Active} \\
\text{joinSet}(\text{self}) := \emptyset \\
\text{execState}(\text{self}) := \text{Dead} \\
\text{if exception}(\text{res}) \text{ then ReportUnhandledExc}(\text{res})
\]

When a thread is \text{Dead}, it remains in this execution state and cannot be reactivated (see also Fig. 4).

4 A parallel model for C# threads

On a multiprocessor system different threads can execute code concurrently on different processors. We model this case using a special kind of distributed ASMs that are executable in tools like AsmL [6]. The main rule for the parallel thread model chooses repeatedly an arbitrary set of possible threads and executes \text{in parallel} the next computation step for each of the chosen threads.

\[
\text{ExecParallelCsharp} \equiv \text{choose } T \subseteq \text{Thread} \text{ do} \\
\text{forall thread} \in T \text{ do ExecStep}(\text{thread})
\]

The ExecStep rule is the same as in the sequential model. However, since the computation steps are executed in parallel, conflicts can occur if the same location is updated by different threads to different values. Updates of the local state of a thread (frame stack, program counter, local environment, operand stack) are not critical, since the local state is parameterized by the thread (see Sect. 3.1). Updates to the shared memory are discussed in Sect. 5 below. An analysis of the transition rules shows that the following conflicts have to be avoided by imposing run constraints on \text{ExecParallelCsharp}.

4.1 Run constraints for the parallel thread model

1. The rule \text{ACQUIRELOCK}(thread) is not allowed to run in parallel with the rule \text{MONITORENTER}(\text{mon}), if \( \text{monObj}(thread) = \text{mon} \). Otherwise, there would be a conflict for \text{lockOwner}(\text{mon}).
2. It is not allowed that two different threads execute `MonitorEnter(mon)` in parallel. Otherwise, conflicts for `lockOwner(mon)` and `readyQueue(mon)` could occur.

3. The rules `AcquireLock(thread)` and `MoveToReadyQueue(t, mon)` are not allowed to run in parallel, if `monObj(thread) = mon`. Otherwise, there is a conflict for `readyQueue(mon)`.

4. The rule `MonitorPulse(mon)` or `MonitorPulseAll(mon)` is not allowed to run in parallel with the rule `MoveToReadyQueue(t, mon)`. Otherwise, there would be a conflict for `readyQueue(mon)`.

5. `MoveToReadyQueue(t_1, mon)` and `MoveToReadyQueue(t_2, mon)` are not allowed to run in parallel for `t_1 \neq t_2`. Otherwise, there would be a conflict for `readyQueue(mon)`.

6. The rules `Suspend(thread)` and `ThreadResume(thread)` are not allowed to run in parallel. Otherwise, the `ThreadResume(thread)` would be ignored by the system.

Note, that `MoveToReadyQueue(t, mon)` is used in the rules `Wakeup(t)` and `AbortOrInterruptPassive(t)` in case that the execution state of `t` is `Waiting`.

5 The .NET memory model

The .NET memory model is outlined in [5, Partition 1, §11.6.5, §11.6.7]. According to [13,15], it gives the following (weak) guarantees about the ordering of memory reads and writes:

- Reads and writes from the same thread to a location cannot be re-ordered.
- No read can move before a lock acquire (or volatile read).
- No write can move after a lock release (or volatile write).
- Writes cannot cross a `Thread.WriteMemoryBarrier()`.
- Neither reads nor writes can cross a `Thread.MemoryBarrier()`.

To application programmers the memory model is often (wrongly) explained in a stronger form. Each thread has its local cache. After acquiring the lock the thread’s cache is invalidated, so that reads afterward are done from the main memory. After releasing the lock the thread’s cache is flushed to main memory. Note that in .NET a read or write of a volatile location affects also the ordering of reads and writes of other locations.

For the ASM specification of the .NET memory model we follow the ASM specification of the Local Consistency Memory Model for Java in [1] and use a universe of events that is divided into disjoint subuniverses as follows:

\[
\text{Event ::= WriteEvent | LockEvent | UnlockEvent | ReadVolatileEvent | BarrierEvent | WriteBarrierEvent}
\]

Events are ordered during a run of a multi-threaded C# program by a dynamic predicate $\prec$. We denote by $\prec^+$ the transitive closure and by $\prec^*$ the reflexive, transitive closure of $\prec$. Each `WriteEvent` has two attributes, an address and a
class Foo {
    private Helper helper;
    public Helper GetHelper() {
        if (helper == null) // quick check
            lock (this)
                if (helper == null) { // double check
                    Helper o = new Helper();
                    Thread.MemoryBarrier();
                    helper = o;
                }
        return helper;
    }
}

Fig. 6. The double checked locking pattern.

value, \(adr: WriteEvent \rightarrow Address\), \(val: WriteEvent \rightarrow Value\). The latest event of a thread is recorded in \(latest: Thread \rightarrow Event\).

The memory model is now reduced to the question: “Which write event(s) can be seen by a memory read?” When a thread writes a value to an address, a new \(WriteEvent\) is created.

\[
WRITE(adr, val) \equiv \text{let } e = \text{new}(WriteEvent) \text{ in} \\
\{ adr(e) := adr, \ val(e) := val \}
\]

\(\text{INSERTAFTERLATEST(self, e)}\)

The new \(WriteEvent\) is inserted in the event order immediately after the latest event of the current thread.

\[
\text{INSERTAFTERLATEST(thread, e)} \equiv \\
\text{if } latest(thread) \neq \text{Undef} \text{ then } latest(thread) \prec e := \text{True} \\
\text{latest(thread) := e}
\]

Reading a value from an address means choosing an appropriate \(WriteEvent\) for that address and returning the value that has been written to that address.

\[
\text{READ(adr)} \equiv \\
\text{choose } e \in WriteEvent \text{ with } adr(e) = adr \land \neg Overwritten(self, e) \text{ do} \\
\text{return } val(e)
\]

A read cannot see arbitrary write events but only those that are not overwritten with respect to the latest event of the current thread or any memory barrier.

\[
\text{Overwritten}(t, e) \iff \\
\exists w \in WriteEvent \text{ such that } adr(w) = adr(e) \land e \prec^+ w \land Previous(t, w))
\]

\[
\text{Previous}(t, w) \iff w \prec^* latest(t) \lor \exists b \in BarrierEvent \ (w \prec^* b)
\]

When a monitor is locked a new \(LockEvent\) is created and inserted in the event order after the latest \(UnlockEvent\) of the monitor as well as after the latest event of the current thread (in this way the write events of the last thread that owned the lock are synchronized with the current thread).
\[
\text{Lock}(\text{thread}, \text{mon}) \equiv \begin{array}{l}
\text{let } e = \text{new}(\text{LockEvent}) \in \\
\text{if } \text{latestUnlock}(\text{mon}) \neq \text{Undef} \text{ then latestUnlock}(\text{mon}) \prec e := \text{True} \\
\text{INSERTAFTERLATEST}(\text{thread}, e) \\
\text{forall } b \in \text{WriteBarrierEvent} \text{ do } b \prec e := \text{True} \\
\text{lockOwner}(\text{mon}) := \text{thread}
\end{array}
\]

The function \(\text{latestUnlock}: \text{Monitor} \rightarrow \text{UnlockEvent}\) records the latest unlock event of a monitor. The \(\text{UnlockEvent}\) created at the monitor exit prevents overwritten write events from being seen by the next thread that acquires the lock of the monitor.

\[
\text{Unlock}(\text{thread}, \text{mon}) \equiv \begin{array}{l}
\text{let } e = \text{new}(\text{UnlockEvent}) \in \\
\text{latestUnlock}(\text{mon}) := e \\
\text{INSERTAFTERLATEST}(\text{thread}, e) \\
\text{lockOwner}(\text{mon}) := \text{None}
\end{array}
\]

The function \(\text{Thread.MemoryBarrier}\) creates a new \(\text{BarrierEvent}\) which is inserted in the event order after the latest event of the current thread. (Barrier events are used in the definition of the \(\text{Overwritten}\) predicate above.)

\[
\text{MemoryBarrier} \equiv \begin{array}{l}
\text{let } e = \text{new}(\text{BarrierEvent}) \in \\
\text{INSERTAFTERLATEST}(\text{self}, e)
\end{array}
\]

The function \(\text{Thread.WriteMemoryBarrier}\) creates a \(\text{WriteBarrierEvent}\) which are inserted in the event order before any future lock event.

\[
\text{WriteMemoryBarrier} \equiv \begin{array}{l}
\text{let } e = \text{new}(\text{WriteBarrierEvent}) \in \\
\text{INSERTAFTERLATEST}(\text{self}, e)
\end{array}
\]

A read of a volatile field creates a new \(\text{ReadVolatileEvent}\). The chosen write event (which was a volatile write) is inserted in the event ordering before the read event.

\[
\text{ReadVolatile}(\text{adr}) \equiv \begin{array}{l}
\text{let } r = \text{new}(\text{ReadVolatileEvent}) \in \\
\text{INSERTAFTERLATEST}(\text{self}, r) \\
\text{forall } b \in \text{WriteBarrierEvent} \text{ do } b \prec r := \text{True} \\
\text{choose } e \in \text{WriteEvent} \text{ with } \text{adr}(e) = \text{adr} \land \neg \text{Overwritten}(\text{self}, e) \text{ do } e \prec r := \text{True} \\
\text{return } \text{val}(e)
\end{array}
\]

A write to a volatile field uses the normal Write rule.

The so-called \(\text{double-checked locking pattern}\) in Fig. 6 uses a memory barrier to prevent another thread from seeing a non-null value of the \text{helper} field while the fields of the \text{Helper} object itself still contain their default null values which are overwritten in the constructor of the \text{Helper} class. (The constructor may be inlined by the JIT compiler.) Instead of using the memory barrier the \text{helper} field could be declared \text{volatile}. 

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```csharp
class Account {
    private decimal balance = 0.0M;

    public void Deposit() {
        lock (this) {
            try { Monitor.Wait(this); }
            finally { balance += 100.00M; }
        }
    }

    public static void Main() {
        Account a = new Account();
        Thread t = new Thread(new ThreadStart(a.Deposit));
        t.Start();
        Thread.Sleep(100);
        lock (a) {
            Console.WriteLine(a.balance); // Output: 0
            Monitor.Pulse(a);
            t.Interrupt();
            Thread.Sleep(100);
            Console.WriteLine(a.balance); // Output: 100.00 (bug)
        }
    }
}
```

**Fig. 7.** A bug in Microsoft’s .NET Framework version 1.1

It is not clear to us, whether the following example is allowed by the Ecma .NET memory model. Consider two threads that concurrently execute the following instructions, where initially \( p.x = 0, p.y = 0 \):

Thread 1  Thread 2
\( r1 = p.x; \quad r2 = p.y; \)
\( p.y = 1; \quad p.x = 2; \)

Is the result \( r1 = 2 \) and \( r2 = 1 \) possible? According to our specification of the memory model, it is not possible. However, if we allow the compiler to switch the assignments in both threads (under the assumption that \( p.x \) and \( p.y \) are independent variables), the result is plausible. Maybe the result is justified by the paragraph about execution order in [4, §10.10].

### 6 Conclusion

The ASM method forces the person who writes a specification to think in terms of an abstract implementation. This leads to questions and cases that are usually forgotten in other formal or informal approaches. Fig. 7 contains a bug in Microsoft’s .NET Framework 1.1 [11] which was detected during the construction
of our thread model. The bug shows a situation where two threads execute at the same time code in two critical sections protected by the same monitor. This should not happen.

The main function in Fig. 7 creates an account, starts another thread with the Deposit method of the account and sleeps for 100 milliseconds. During the sleep, the deposit thread acquires the lock of the account and waits on the account in order to later deposit 100 dollars when it is pulsed. After the sleep, the main thread locks the account and executes its critical section. At the beginning, the balance is still 0. The main thread pulses the account and moves the deposit thread from the wait queue into the ready queue of the account. Then it interrupts the deposit thread and sleeps again for 100 milliseconds (still holding the lock of the account). When it awakes, the balance has changed to 100.0. Why?

The change of the balance is only possible if the deposit thread executes the finally block, which is in its critical section, without owning the lock of the account. The same problem occurs if Thread.Interrupt is replaced by Thread.Abort.

The Rotor SSCLI implementation [16] correctly prints 0 at the end of the lock statement in the main function. After that, however, it deadlocks for unknown reasons.

References


13. V. Morrison. The DOTNET Memory Model. dotnet@discuss.develop.com mailing list, 2002.